

Financial Prospect Relativity: Context Effects in Financial Decision-Making Under Risk[†]

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ABSTRACT

We report three studies in which methodologies from psychophysics are adapted to investigate context effects on individual financial decision-making under risk. The aim was to determine how the range and the rank of the options offered as saving amounts and levels of investment risk influence people's decisions about these variables. In the range manipulation, participants were presented with either a full range of choice options or a limited subset, while in the rank manipulation they were presented with a skewed set of feasible options. The results showed that choices are affected by the position of each option in the range and the rank of presented options, which suggests that judgments and choices are relative. Copyright © 2006 John Wiley & Sons, Ltd.

KEY WORDS prospect relativity; decision-making; judgment; investment risk; saving decisions; context effects; perception

INTRODUCTION

Two goals of the research are presented here: the first is theoretical, while the second is applied. The theoretical goal is to test the robustness of empirical phenomena in judgment and decision-making research, which concern the context malleability of human decision-making under risk. The applied objective of the three experiments outlined below is to develop ways of stimulating financial consumers to save more for retirement and be less risk averse in relation to their retirement savings investments. This objective is in consumers' interest and relates to government concerns that people in the UK and other industrialized countries save too little and do not take enough financial risk (e.g., Oliver, Wyman & Company, 2001). Our article presents laboratory experiments in which investment decisions were manipulated by the context in which they were presented.

In particular, our research focused on studying the effects of the choice option set when asking people to express their preferences in relation to different retirement savings and investment scenarios. The crucial

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practical question here is how to enable people to make better investment decisions, by presenting the financial information in such a way that they are motivated to save more and encouraged to increase the proportion of investments in risky products. The experimental design and method are based on the prospect relativity phenomenon (Stewart, Chater, Stott, & Reimers, 2003) and the rank dependence effect (Birnbau, 1992), both of which demonstrate the dependence of human preferences and decisions on the set of choice options they are presented with, and the lack of stable underlying preference function. The robustness and practical relevance of these two phenomena can, therefore, be better assessed in the light of the results obtained with realistic decision situations used here, as opposed to the abstract choice scenarios with which both effects were initially tested.

PREVIOUS EXPERIMENTAL RESEARCH

Much of human behavior is a consequence of decision-making which involves some judgment of the potential rewards and risk associated with each action. Deciding how to invest one's savings, for example, involves balancing the risks and likely returns of the prospects available. Understanding how people trade-off financial risk and return and make choices on the basis of these trade-offs is a central question for both psychology and economics, because the foundations of economic theory are rooted in models of individual decision-making. So in order to explain the behavior of investors, we need a model of the decision-making behavior under risk and uncertainty.

Most of economic theory has been based on a normative theory of decision-making under risk and uncertainty, expected utility theory, first axiomatized by von Neumann and Morgenstern (1947). Expected utility theory specifies certain axioms of rational choice, and then shows that if people obey these axioms, they can be characterized as having a cardinal utility function. In essence, people are assumed to make choices that maximize their utility, and they value a risky option or a strategy by the expected utility this option will provide (the expected utility is modeled as the expected payoffs weighted by their respective probabilities). Deviations of real behaviors from this theory have been seen as primarily due to lack of experience and opportunity for learning, confusion, and lack of enough information (see Shafir & LeBoeuf, 2002, for discussion). Psychologists and economists have been trying to empirically verify the assumptions of rational choice theory, revealing ever increasing evidence that human behavior diverges from the predictions of the theory (e.g., Kagel & Roth, 1995; Kahneman & Tversky, 2000; and also Camerer, 1995, for a review).

Loomes (1999) suggests that the evidence accumulated so far in the literature is much more easily reconciled with a world where most individuals have only rather basic and fuzzy preferences (even for quite familiar sums of money). This evidence is contrary to the fundamental rational choice assumption that individuals have reasonably well-articulated values that are successfully applied to all types of decision tasks. The view that each version of the decision problem triggers its own preference elicitation is similar to the claim that preferences are constructed, (i.e., not elicited or revealed), in the generation of a response to a judgment or choice task (Bettman, Luce, & Payne, 1998; Fischhoff, 1991; Slovic, 1995; Tversky, Sattath, & Slovic, 1988).

Effects of the choice set have been demonstrated in consumer choice (i.e., trade-offs without risk) and the basic finding is that the choice set can influence how much variety consumers select (Simonson, 1990). Simonson suggests that this behavior might be explained by variety seeking serving as a choice heuristic. That is, when asked to make several choices at once, people tend to diversify. This result has been called the diversification bias by Read and Loewenstein (1995). Benartzi and Thaler (1998, 2001) have found evidence of the same phenomenon by studying how people allocate their retirement funds across various investment vehicles. In particular, they find some evidence for an extreme version of this bias that they call the $1/n$ heuristic. The idea is that when an employee is offered n funds to choose from in her retirement plan, she divides the money evenly among the funds offered. Use of this heuristic, or others even more sophisticated,

implies that the asset allocation an investor chooses will depend strongly on the array of funds offered in the retirement plan. Thus, in a plan that offered one stock fund and one bond fund, the average allocation would be 50% stocks, but if another stock fund were added, the allocation to stocks would jump to two-thirds. Benartzi and Thaler found evidence supporting just this behavior in real-world pension choices. In a sample of US 401 k pension plans, they regressed the percentage of the plan assets invested in stocks on the percentage of the funds that were stock funds and found a very strong relationship. Note that these are real-world data on the distribution of assets across pension funds with different levels of risk (i.e., different numbers of stocks and bonds offered by each particular employer) and thus, this study creates a natural experiment that allows us to compare the effects of offering more stocks and fewer bonds versus fewer stocks and more bonds. The results showing the strong effect of the choice set on actual behavior highlight difficult issues regarding the design of retirement saving plans, both public and private,¹ as it is not clear that people can consistently select a “preferred” mix of fixed income and equity funds. For example, Benartzi and Thaler point out that if the plan offers many fixed-income funds, the participants might invest too conservatively, while if the plan offers many equity funds, the employees might invest too aggressively.

The findings by Benartzi and Thaler (1998, 2001) illustrate that investors have ill-formed preferences about their investments, which again is consistent with the idea that preferences are constructed (Slovic, 1995). In another study, Benartzi and Thaler (2002) asked individuals to choose among investment programs that offer different ranges of retirement income (for instance, a certain amount of \$900 per month vs. a 50–50 chance to earn either \$1100 per month or \$800 per month). When they presented individuals with three choices ranging from low risk to high risk, they found a significant tendency to pick the middle choice. For instance, people viewing choices A, B, and C, will often find B more attractive than C. However, those viewing choices B, C, and D, will often argue that C is more attractive than B. Simonson and Tversky (1992) illustrated similar behavior in the context of consumer choice, which they dubbed extremeness aversion and also the compromise effect. These results confirm that choices between alternatives depend on other irrelevant options available. This again illustrates that choices are not rational according to standard economic criteria and when choice problems are difficult, people may resort to simple “rules of thumb” to help them cope, such as the rule that it is best to avoid extremes.

Several other studies have also shown similar types of effects. For example, the range of frequencies in response options (measures of frequency of behavior or other events) can have an effect on the response process, and on answers to questions that follow (e.g., Menon, Raghurir, & Schwarz, 1995; Schwarz & Bienias, 1990; Schwarz, Hippler, Deutsch, & Strack, 1985). For example, in an experimental investigation of response option ranges in a “somatic complaints” scale, respondents who were presented with a high frequency range of responses (from “4 or less” to “9 or more”) were much more likely to report feeling “low or emotionally depressed” on five or more occasions during the past month than respondents presented with the low range of response options (from “0” to “5 or more”; Harrison & McLaughlin, 1996). Apparently, the response ranges in this example must have influenced respondents’ interpretation of the intensity of emotional experience. Similar effects were observed in responses to the nine other items of the scale. In general, such bias effects appear in a wide range of experimental contexts. For example, even such a basic quality like the perceived size of a physical object systematically varies with the method of measurement (Poulton, 1989), which can be numerical estimates, drawings, or matching something to a variable target.

Our research presented here is based on a particular study of constructed risk preferences conducted by Stewart et al. (2003) who tested whether the attributes of risky prospects behave like those of perceptual

¹Diversification bias can be costly because investors might pick the wrong point along the frontier. Brennan and Torous (1999) considered an individual with a coefficient of relative risk aversion of 2, which is consistent with the empirical findings of Friend and Blume (1975), and then calculated that the loss of welfare from picking portfolios that do not match the assumed risk preferences is 25% in a 20-year investment horizon and 35–40% for 30 years horizon. For an individual who is less risk averse and has a coefficient of 1.0, the welfare costs of investing too little in equities can be even larger.

stimuli and found similar context effects between decision-making under risk and perceptual identification. Their experiments demonstrated the notable effect of the available options set, suggesting that prospects of the form “ p chance of x ” are valued relative to one another. The idea behind this experiment was that some of the factors that determine how people assess magnitudes like payoff and probability might be analogous to factors underlying an assessment of psychophysical magnitudes, such as loudness or weight. Specifically, psychophysical experiments have shown that people cannot provide stable absolute judgments of such magnitudes, and are heavily influenced by the options available to them (Garner, 1954; Laming, 1997). In particular, Stewart et al. found that the set of options from which an option was selected almost completely determined the choice. They demonstrated this effect in a certainty equivalent estimation task (the amount of money for certain that is worth the same to the person as a single chance to play the prospect) and in the selection of a risky prospect.

There have been other experiments that have also investigated the effect of the set of available options in decision under risk. Birnbaum (1992) demonstrated that the skew of the distribution of options offered as certainty equivalents for simple prospects (while the maximum and minimum are held constant) influences the selection of a certainty equivalent. In particular, prospects were less valued in the positively skewed option set where most values were small, compared to when the options were negatively skewed and hence most values were large. Similar results were obtained by Mellers, Ordóñez, and Birnbaum (1992) who measured participants’ attractiveness ratings and buying prices (to obtain the opportunity to play the prospect for real and have a chance to receive the outcome) for a set of simple binary prospects of the form “ p chance of x .”

The experiments by Birnbaum (1992) and Stewart et al. (2003) still lack, however, the link with the real-world context in which people make the actual risky choices that are relevant to their financial futures. This gap motivated us to investigate whether using decision situations that people encounter in their real lives would produce effects similar to Birnbaum’s and Stewart et al.’s findings. In the three experiments reported below, we found large and systematic effects of choice set (consisting of alternative saving and investment prospects) on the choice of saving and investment plans. These effects are compatible with the prospect relativity hypothesis proposed by Stewart et al. and also those models that discard the assumption that the value of a choice option is independent of other available options (contrary to standard models of rational choice).

In summary, the findings presented above show the importance of the effects of the choice set on people’s preferences in various decision domains. One natural way to attempt to explain these effects is by assuming that people’s representations of the relevant dimensions (e.g., level of risk) are not stable, but are influenced by context. Two classic theories, originating from the psychophysical literature, have been proposed to explain this type of effect—adaptation level theory (Helson, 1964) and range–frequency theory (Parducci, 1965, 1974). As we shall see below, both of these accounts of the contextual dependency of judgment can be used as the foundation for explaining context effects in choice; and we shall model the data gathered in this paper using implementations of both types of model.

Adaptation level theory is based on the assumption that judgments, for example, of loudness, brightness, or, here, say, riskiness, are not absolute but relative to an “adaptation level,” which is a weighted sum of recent stimuli. Thus, an option is viewed as risky not by comparison with any absolute standard, but in relation to other recently encountered stimuli. Intuitively, the idea is that the perceptual or cognitive system “adapts” to the values of recent stimuli, and the subjective judgment of the magnitude of a new stimulus is made in comparison with this adaptation level. Note, in particular, that by focusing on the adaptation level (which will be related to an average of the distribution of recent items), the account assumes that there is no direct impact of other aspects of the distribution of past items, such as variance, skew, and range.

Range–frequency theory, by contrast, predicts that the subjective value given to a magnitude is a function of its position within the overall range and rank of distribution of magnitudes that have been observed. Specifically, the impact of range is captured by expressing the current magnitude as a fraction of the interval

from the lowest to the highest magnitude that has been encountered. This fraction will be a number between 0 and 1. The impact of rank is captured by the rank position of the item, in relation to the distribution of all contextually relevant items and this rank position is also normalized to be between 0 and 1. The predictions of range–frequency theory are then obtained by a weighted average of these quantities, where the relative contribution of the two is a free parameter.

Parducci (1965, 1974) developed range–frequency theory as an alternative to adaptation level theory, to account for his observation that the neutral point of the scale does not correspond to the mean of the contextual events, as adaptation level theory predicts (Helson, 1964), but rather to a compromise between the midpoint and median of the distribution of contextual events. The contribution of the midpoint, for Parducci, is captured by measuring the range of the distribution; the contribution of the median is measured by capturing rank.

Both adaptation level and range–frequency theory assume that people judge magnitudes not according to any absolute scale, but in relation to other contextually relevant magnitudes. Both theories imply that judgments will be invariant to certain transformations of the stimuli. In particular, if all stimuli in an auditory experiment are increased or decreased in intensity by, say, ten decibels, the relative positions of the stimuli will be unchanged, and according to both theories judgments concerning those stimuli should be identical. (Of course, influences of absolute stimulus intensity can still be accounted for, either by noting that there is implicit comparison with extrinsic stimuli, such as ambient noise, or internal noises, e.g., from within the listener’s body; and that invariance to such transformations breaks down at extremes, where the perceptual apparatus does not function effectively e.g., where the stimulus is inaudible).

Range–frequency theory also predicts that there should be no effect of the variance of the stimuli—that is, it assumes that if the spacing between stimuli were increased by, for example, a factor of two, people’s judgments of the relevant magnitudes would be unchanged. This is because each stimulus is evaluated by the range of items and the rank position of each item, and these quantities are not modified by linearly stretching out, or compressing, the items. Range–frequency theory, unlike adaptation level theory, does predict that changing the skew of a distribution, while leaving its mean invariant, will affect judgments. For example, the midpoint of the range will be perceived as “greater” for a negatively skewed distribution (because most items will be below it in rank position), whereas it will be perceived as “lower” for a positively skewed distribution (because most items will be above it in rank position).

How can these theories of the impact of context on *judgment* be employed to explain how context can affect the *choices* people make between options. We follow previous work (e.g., Wedell & Pettibone, 1999) in proposing that judgment affects attractiveness—and that attractiveness in trade-offs (such as the trade-off between risk and return) can be viewed as depending on the nearness to a single “ideal” standard. The probability of choosing an option is then assumed to be proportional to the attractiveness of that option. (This is Luce’s (1959) choice rule, in its simplest form. See below.)

The classical ideal point approach proposed by Coombs (1964) falls into this category of models of attractiveness (see also Risky, Parducci, & Beauchamp, 1979; Wedell & Pettibone, 1999). According to this model, people represent “ideal points” and judge the attractiveness of a stimulus by its distance from the ideal point. Norm theory (Kahneman & Miller, 1986) follows a similar approach. However, the standard here is called the “norm” and is constructed on the spot rather than retrieved from long-term memory. (A comparison set is constructed in working memory, consisting of known exemplars, and its norm is computed, usually by deriving the mean of the presented values and the context is usually assumed to shift the ideal towards this mean.) In norm theory, as indeed in adaptation level theory, there is no assumption that the “standard” is preferred—that is, viewed as the most attractive option.

Ideal point models appear promising in the present context, because attractiveness in the context of trade-offs may naturally be viewed as involving something akin to a bell-shaped relationship between attractiveness and the trade-off between trade-off stimulus dimensions (here, saving and risk). In other words, more saving and risk is not always better and the relationship between preference and value in these two

domains is characterized by a single-peaked preference curve in which the ideal lies at an intermediate value between the extremes. Too much risk is not attractive because it leads to high variability and potential losses. Too little risk cannot bring good future returns. Likewise, too much saving reduces current consumption, but too little saving will reduce future consumption. That is, it seems natural to assume single-peaked preferences when the ideal is located at an intermediate value (Coombs, 1964; Coombs & Avrunin, 1977). Where this is not the case—for example, where one dimension entirely dominates to the exclusion of the other—then it would not seem to be appropriate to speak of a trade-off between dimensions at all.

An ideal point model, of some kind, could possibly account for the choice set effects we expect to observe. Thus, the influence of the choice set on the ideal might explain why the same option can be perceived and judged differently in different context conditions. Prior research on perceptual judgments would suggest that such ideals might depend on the range and the skew of the distributions (according to Parducci's range–frequency theory, 1965, 1974) and the mean (according to Helson's adaptation level theory, 1964). Therefore, we expect the ideals to be affected by such contextual factors as the range, rank, and mean of the stimuli included in the choice set.

SUMMARY OF EXPERIMENTS

In the experiments presented here, we adapted particular methods and models from psychophysics (Garner, 1954; Parducci, 1965, 1974), which were first applied in research on decision-making under risk by Birnbaum (1992) and Stewart et al. (2003), in order to investigate the possibility that context effects influence decision-making under risk in realistic financial situations. In particular, we investigated whether context effects arise in choices between options in which one or more related variables are varied. These variables were amount of savings, investment risk, expected retirement income, variability of retirement income, and retirement age. The sequence of questions prompted decisions about individual variables without showing the effects on all other related variables (e.g., only deciding how much to save), and also decisions about combination of variables (e.g., investment risk versus expected retirement income). Thus, in some cases, one dimension was varied and its effects on other dimension(s) was also shown, and the goal was to trade-off these variables.

The aim of Experiment 1 was to determine whether the set of choice options, offered as the potential amount to be saved and investment risk, influence people's judgments and decisions about these variables. In Experiment 2, we investigated whether the skew of the distribution of the options offered affects judgments and decisions about these options. In Experiment 3, we further investigated whether the effects of the skew and the rank are different for saving and risk, and also whether other values of the context would produce the same significant result for risk. Finally, we modeled the experimental data using ideal point-based versions of range–frequency theory and adaptation level theory. The model fits show how implementing each theory can capture these data.

EXPERIMENT 1

Participants were asked to select among a predefined set of values related to five variables: (a) the desired percentage of the annual income that will be saved for retirement, (b) the investment risk expressed as the percentage of the savings that will be put into risky assets, (c) retirement age, (d) expected retirement income, and (e) possible variability of the retirement income.

Table 1. Figures for saved amount (£), investment risk (%), and retirement age in the three conditions of Experiment 1

Full context			Low context			High context		
Save	Risk	Retire	Save	Risk	Retire	Save	Risk	Retire
500	0	48	500	0	48			
1000	10	50	1000	10	50			
1500	20	52	1500	20	52			
2000	30	54	2000	30	54			
2500	40	56	2500	40	56			
3000	50	58	3000	50	58	3000	50	58
3500	60	60				3500	60	60
4000	70	62				4000	70	62
4500	80	64				4500	80	64
5000	90	66				5000	90	66
5500	100	68				5500	100	68

There was a control condition, called the *full context* condition, in which the participants had to freely decide the value of each one of these variables when selecting from the full range of options. In two other context conditions, participants were asked to select these values from a sub-set of the set of options offered by the experimenter in the full context condition. Thus, there were three between-participant conditions in the experiment presented here, that is, with separate groups for the full context, low context, and high context conditions. Table 1 presents the values for savings and risk in the three conditions. In the full context condition, all options were presented. In the two other conditions, the choice of prospects was limited to either the first or second half of the prospects available in the full context condition, so that the participant in the high context condition was presented with a range of values, the lowest of which coincided with the highest option in the low context condition. In the full context condition for savings, the options were presented in monetary terms and varied from 2 to 22% of the hypothetical salary (£25 000) increasing with 2% between the options. Thus, there were 11 options to choose among, while the low context condition spanned from 2 to 12% and the high context condition was from 12 to 22%. The same design was applied for the other choice variables in the test. The values in the full context condition for the other four key variables were the following. For investment risk, the options varied from 0 to 100%, increasing with 10% between the choice options. For retirement age, the options were varied from 48 to 68, increasing with 2 years between the choice options. Note that for retirement income and its variability, the values were different for every question depending on the combination of saved amount, investment risk, and retirement age.

If participants are not influenced by the set of options, then their choices of each value in the high and low context conditions should be independent of the other values in the set and the chosen values should be the nearest to their free choice in the full context condition (where they saw all possible options). The key prediction is that if people are not influenced by the context (i.e., the other available options), then the lowest option in the high context condition should not be chosen to a significantly lesser degree than the same option plus other options lower than that in the full context condition (i.e., the options that are missing in the high context condition). In other words, the proportion of times the lowest option in the high context condition was selected should not be less than the total proportion of times the same option plus some other below it was selected in the full context condition.

If participants are mainly influenced by the set of options presented to them, then the distribution of responses across options should be similar between the low and the high context conditions, and there will not be a tendency towards the distribution of responses in the full context condition.

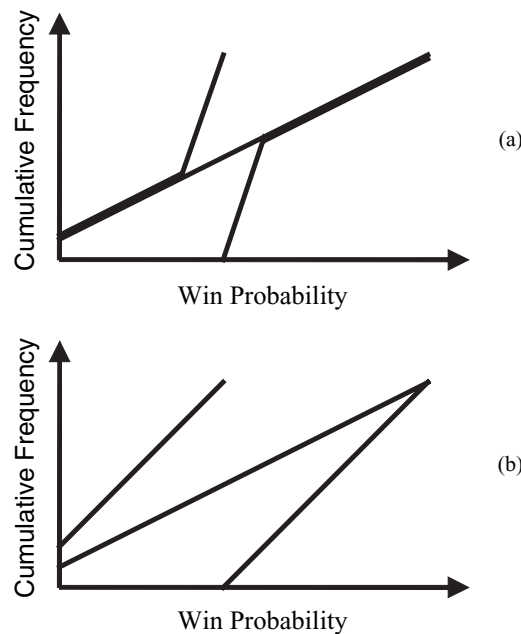


Figure 1. Predictions in terms of cumulative frequencies of choices, which would be expected, if people have (a) fixed, and (b) relative, level of risk aversion

It is helpful to consider the predictions (represented in terms of cumulative frequencies of choices) that would be expected if people have a fixed and absolute level of risk aversion (or any other preferences) which they use to make their choices. If we suppose that where the full set of choices is available, people make each choice roughly equally, then the cumulative frequency is an increasing linear function of win probability, shown as a straight line in the upper part of Figure 1a. If the choice set is restricted to the lower win probability options only (i.e., high reward, high risk options), then all the participants who would, in the full context condition, have chosen one of the higher win probability options, were they still available, should instead choose the highest available option. The choices of all other participants should be unchanged. (This follows on the assumption that people choose according to a fixed absolute risk preference, and hence the availability of non-preferred options should not affect their choices.) Thus, the cumulative frequency should, in the lower win probability condition, follow the linear function of the absolute condition and all remaining participants should choose the highest available option, so that this point goes directly to 1, and stays there. Similarly, in the case where only the upper range of options is available, the cumulative frequency is clearly at 0 for all the non-available options. If people's judgments are absolute, then participants who would otherwise have chosen the low win probability options that are now not available will choose the lowest of the available high options. Specifically, the cumulative frequency should jump directly to the linear function appropriate in the full range condition and, as other choices in the high range should be unaffected by the presence or absence of non-preferred lower options, the function should then follow the linear function of the full context condition thereafter.

By contrast, the lower part of Figure 1b shows the predictions from the extreme opposite assumption: instead of people choosing gambles on the basis of fixed, absolute risk preferences, they assess risk purely in relative terms. If this is correct, then the pattern of response should have the same distribution, whether the responses are distributed across the full context, or just the lower and upper context. So, if we assume that

response is even in the full context condition (and hence that the cumulative probability function is linear), then in the lower and upper contexts, the cumulative distribution should also be linear, but compressed over a smaller number of choices items (i.e., with an increased slope).

Method

Participants

Twelve participants took part in each condition of this study (i.e., 36 participants in total) recruited from the University of Oxford student population via the experimental economics research group mailing list of people who have asked to be contacted. All were paid £5 for their participation.

Design

The questions were formulated as long-term saving/investment decision tasks related to retirement income provision. The participants had to make decisions about five key variables. These variables were the saved proportion of the current income, the risk of the investment expressed as the proportion invested in risky assets,² the retirement age, the desired income after retirement, and the preferred variability of this income (participants were told that this variability is due to the uncertainty of economic conditions).

The experimental materials were designed as 10 independent hypothetical questions, in which we varied each of the 5 key variables. Five of the questions focused only on savings while the other five questions focused on risk and some questions showed how changing savings or risk would affect another variable or set of variables. For example, one question showed how changing the investment risk can affect the projected retirement income and its variability—with higher risk offering not only higher expected income on average, but also wider spread of the possible values.³ Figure 2 presents this question in the full context condition, in which the participants were asked to choose their preferred level of investment risk by selecting one of the rows in the table (note that in this format, the key variable is in the first column of the table below, while the other columns are showing the effects on the other variables like the minimum, average, and maximum retirement income shown here):⁴

The high context condition was derived by deleting the lower five rows of the table for each question in the full context condition and the low context condition was derived by deleting the higher five rows in the tables in the full context condition (i.e., the same was done for each question). Therefore, in the full context condition, the participants had to choose among 11 possible answer options for each question while in the high and low context conditions, there were only 6 available answer options.

²There are various types of risky assets, like bonds and equities, for example, but in reality, these various investment vehicles differ mainly in their risk-return characteristics.

³In order to derive plausible figures for the various economic variables, we implemented a simple econometric model into a spreadsheet simulator that calculates the likely impact of changes in each variable on the other four variables. For example, this model can derive what retirement income can be expected from certain savings, investment risk, and retirement age, or what are the possible potential investment options that could lead to the preferred retirement income. Note also that all figures are in pounds and the participants knew this.

⁴Most of the questions showed the expected retirement income and its variability like in the example above. The possible variability of the retirement income was explained by referring to the 95% and respectively 5% confidence intervals of the income variability, that is, maximum and minimum possible values of the income, for which there is 5% chance to be more than the higher or less than the lower value, respectively. On each row of the table, these two values were placed on both sides of the average expected retirement income. The confidence intervals were expressed also in verbal terms using the words “very likely.” For example, the participants were informed that *it is very likely (95% chance) that their income will be below the higher value and above the lower value*, and that these two values change depending on the proportion of the investment in equities.

Assume that you will retire at 65 and decided to save 11% of your current salary (£2750) in order to provide for your retirement income. The following options offer different ranges of retirement income (in pounds) depending on the percentage of your savings allocated to shares (in the stock market) and you can see the effects on the expected average retirement income and its variability (minimum and maximum). Note that you are very likely (have 95% chance) to be between the minimum and maximum figures indicated in the table below. Please select one of the following options.

<i>Invest</i>	<i>Minimum</i>	<i>Average</i>	<i>Maximum</i>
0 %	16,000	16,000	16,000
10 %	17,000	19,000	22,000
20 %	17,000	21,000	23,000
30 %	17,000	23,000	29,000
40 %	16,000	26,000	35,000
50 %	15,000	29,000	42,000
60 %	14,000	33,000	51,000
70 %	11,000	37,000	62,000
80 %	7,000	41,000	76,000
90 %	2,000	47,000	92,000
100 %	0	53,000	112,000

Figure 2. A question in the full range condition, in which the participants are asked to choose their preferred level of investment risk

The 10 questions were presented in different orders in the various conditions. In Appendix A, there is a detailed description of each question and its purpose (the questions are grouped by the key variable that participants are asked to select savings or investment risk).

Procedure

Participants were given a booklet with 10 questions. They received written instructions explaining that the purpose of the experiment was to answer a series of questions about savings and investment related to retirement income provision, and that there were no right and wrong answers and they were free to choose whatever most suits their preferences. It was explained that the choice options are predetermined as these are the outcomes that can be realistically accomplished according to a standard economic model and that the task was to choose the option nearest to the participant's preferences. The participants were also informed that if

they found all these options unsatisfactory, then they could indicate values outside these ranges. (We found that none of the participants indicated such values.)

The questions and the answer options were presented in the same way as the example question presented in Figure 2. The participants had to choose one of the values in the first column of the table (which were either savings or investment risk values) and they were provided with a separate answer sheet to write their answers. Participants were informed that their answers did not need to be consistent between the questions, and that they could freely change their preferences on each question and choose different savings and risk values.

Results

Participants took approximately 30 minutes to answer all questions. Note that although the questions related to saving and to risk asked the participants to trade off different variables (e.g., savings versus retirement income in one question, and savings versus risk in another question), we used the weighted average of the answers of each participant across all five questions related to saving and all five questions related to risk in order to derive the mean values for saving and risk in each condition. It is these averaged results that are presented here. This was done because the results showed no difference (i.e., the general pattern was the same) across the five questions for saving and risk, respectively.

Savings

The cumulative proportion of times each saving option (percentage) was chosen in the low context, full context, and high context conditions is plotted in Figure 3. The results were averaged over all participants.

The pattern of responses shown in Figure 3 is very similar to the co-linear pattern presented in Figure 1b indicating purely relative preferences, and is markedly dissimilar to Figure 1a showing fixed and absolute preferences. Also, the proportion of times the lowest option in the high context condition (the £3000

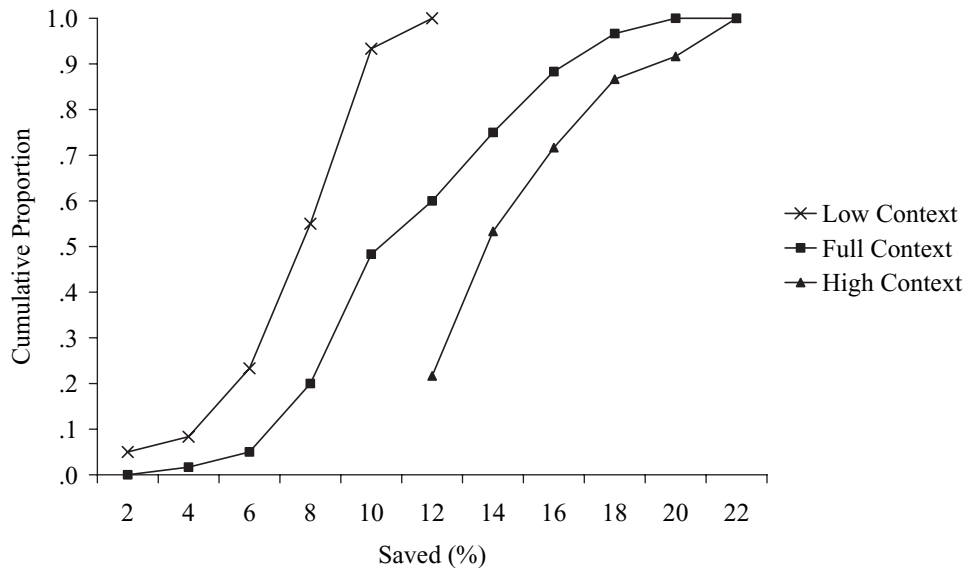


Figure 3. Cumulative proportion of times each saving option was chosen in the low range, full range, and high range conditions, Experiment 1

option) was selected was 0.22 and was significantly lower than 0.60, which is the proportion of times the same option plus another option below it was selected in the full context condition, $t(22) = 3.86, p = 0.001$. This result indicates that the context has significantly affected choices in the high context condition. The proportion of times the highest option in the low context condition (again the £3000 option) was selected was 0.07 and this value was significantly lower than 0.52, which was the proportion of times the same option plus some other option above in the full context condition was selected, $t(22) = 3.76, p = 0.001$. This result also means that the hypothesis that participants' choices were unaffected by context should be rejected. At the same time, the greatest proportion of responses in the low range and high context conditions were concentrated around the middle options of the whole context, which indicates that people seemed to prefer moderate saving amounts.

Investment risk

The cumulative proportion of times each investment risk option was chosen in the full context, low context, and high context conditions is plotted in Figure 4.

Here again, the pattern of responses (shown in Figure 4) is more similar to the co-linear pattern presented in Figure 1b indicating purely relative preferences. However, the distributions of responses in the full context and low context condition are approximately the same, while in the high context condition, the distribution is heavily skewed towards the lower options, pointing to the supposition that overall, people still prefer lower risk levels. This result indicates that people are clearly risk averse and prefer lower levels of investment risk. The proportion of times the lowest option in the high context condition (the 50% option) was selected was 0.47 and this value was significantly lower than the proportion of times the same option plus another option below it was selected in the full context condition, which was 0.93, $t(22) = 5.60, p < 0.0001$. The proportion of times the highest option in the low context condition (again the 50% option) was selected was 0.03 and this result was significantly lower than 0.20 which was the proportion of times the same option or another option

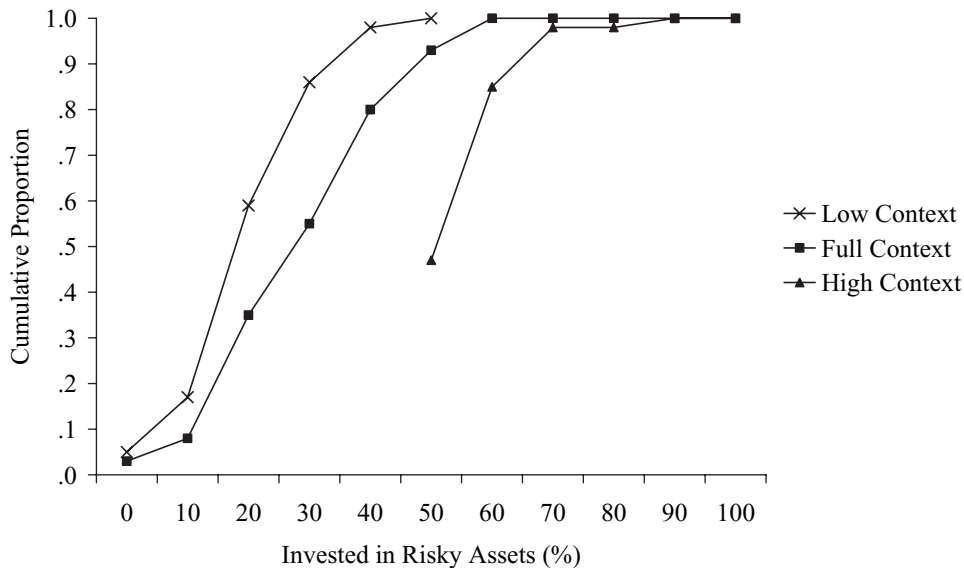


Figure 4. Cumulative proportion of times each investment risk option was chosen in the low range, full range, and high range conditions, Experiment 1

above it in the full context condition was selected, $t(22) = 2.93, p = 0.008$. These results show that context has significantly biased people's responses away from their likely choices in the full context condition.

Discussion

The results clearly demonstrate that the choices were strongly influenced by the set of offered choice options. The skewed results clearly show that there is a tendency towards certain preferred values for savings and risk. This result suggests that people's preferences are not completely malleable by the context and choices are not absolutely relativistic and context dependent as the prospect relativity principle claims. This result might arise, however, because the options are too far apart from each other. It is possible that if the options are closely spaced, then people are more likely to be indifferent between them, and then the responses would be less skewed and the relativity effect will arise. We conducted an additional experiment investigating the effect of decreasing the spacing of the choice options and the results demonstrated that halving the spacing of the options did not make the responses more evenly distributed and the effects of the choice set were the same as in Experiment 1.

In Experiment 1, the ranks and the range of the choice options were manipulated at the same time when comparing the high and low context condition versus the full context condition, which implies that the effects could be due to either ranks or ranges [here, we mean range and rank as postulated by range–frequency theory (Parducci, 1974)]. In other words, frequency values and range values as calculated strictly on the stimuli presented are completely confounded. Thus, it does not make sense to claim that the effects of Experiment 1 are due to range rather than rank. However, the context effect can be observed even if we compare only the low context and the high context condition, where all the corresponding options have the same rank and then the context effects would appear even stronger. For example, if the majority of choices in the low context condition are below the highest option, then in order to demonstrate context effects, we just need to show that the total proportion of responses below the highest option in the low context is significantly higher than the proportion of choices of the lowest option in the high context. This is evident from Figures 1 and 2. These comparisons suggest the possibility that the results are not mainly due to rank effects.

Yet another alternative explanation of Experiment 1 could be that when participants are repeatedly presented with trials containing too-high or too-low options, they learn to readjust their judgments to fit their responses within the alternatives given (the same point was raised also by Stewart et al., 2003). In order to rule out this alternative explanation, we conducted an additional experiment using a within-participants design, in which each participant was presented with both high context and low context conditions (following Stewart et al.). This design was supposed to test whether the participants could learn to adjust their judgments up or down to fit into the response scale, which would also cause the observed effect of the choice set. Thus, these effects should have disappeared when the participants were presented with both low and high contexts. However, the pattern of results demonstrated in Experiment 1 was replicated, which suggests that the effect was caused only by the options available on every trial (the data from this study are available on request).

In summary, the prospect relativity effect appeared when people were faced with familiar (most likely previously experienced) situations, including saving, consumption, pension plans, and investment in the capital markets (at least the media provide enough information on the last issue). It seems, however, that people might have also developed some more stable preferences for risk, although their responses were still malleable to context effects. In other words, the results showed that people were more context sensitive when they made decisions about savings, which implies that they might not have a clear idea how much they need to consume and save, respectively. This is a plausible conclusion as all participants in our experiments were students who do not earn real income and therefore, are unlikely to have stable preferences concerning consumption-savings ratios (in our hypothetical scenarios we just asked them to imagine that they earn £25 000 per year).

EXPERIMENT 2

Experiment 1 demonstrated the significant effects of the set of offered values on risky choices, which suggests that choice options are judged relative to each other when reaching a decision. There is substantial evidence in the literature on perceptual judgment and also on risky decision-making that the skew of the distribution of stimuli (i.e., their rank order) also affects the responses: stimuli with higher rank in the distribution (absolute values held constant) are judged to have higher subjective values (e.g., Birnbaum, 1992; Brown, Gardner, Oswald, & Qian, 2003; Janiszewski & Lichtenstein, 1999; Parducci, 1965, 1974). Recall that Birnbaum has already demonstrated that when the options offered as certainty equivalents for simple prospects are positively skewed and hence most values are small, then prospects are undervalued, while when the options are negatively skewed and most values are large, then the prospects seem to be overvalued.

In order to investigate these effects on saving and investment decisions, we manipulated the skew of the distribution of values so that in one condition, the distribution of options was positively skewed and in another condition, the distribution of options was negatively skewed. There was one target option common to both conditions, which had a higher rank in the positively skewed condition and a low rank in the negatively skewed condition. Experiment 1 demonstrated a tendency for people to prefer lower risk options, and in order to account (and control) for this tendency, we selected the common option to be equal to the natural mean in the full context condition in Experiment 1 (i.e., the value that on average was most preferred by the participants). So in this case, if there is a difference between the two groups in the proportion of times this option was selected, then it is unlikely to be due to the fact that people prefer lower investment risk. The preferred value for the saving questions was estimated to be 12% and 30% for the investment risk questions. Therefore, we expected these two options to be perceived as lower values when they had a lower rank, which could motivate people to select them more often compared to the condition in which they had a higher rank.

Method*Participants*

Twenty-four different volunteers participated in this study. Twelve participated in the positive skew condition and 12 in the negative skew condition. All participants were students from the University of Oxford and none had participated in Experiment 1. They were paid £5 for taking part in this experiment.

Design and procedure

The design and procedure were the same as in Experiment 1, except that the new investment risk values for the positive skew condition included the options 0, 10, 20, 30, 60%, while for the negative skew condition, the values were 0, 30, 40, 50, 60%. Note that 30% is the comparison option between the conditions, and in the positively skewed distribution, it is fourth in rank compared to the negatively skewed distribution where it is second in rank. Thus, this design included only five choice options per question. In order to keep the number of options restricted to five for the savings questions as well, we deleted the two lowest and two highest options from the answer table for every such question. Hence, for these questions, in the positive skew condition we included only the values £1500 (6%), £2000 (8%), £2500 (10%), £3000 (12%), and £4500 (18%), while in the negative skew condition, the included values were £1500 (6%), £3000 (12%), £3500 (14%), £4000 (16%), £4500 (18%). As a result, in the positively skewed distribution, the 12% option is fourth in rank while in the negatively skewed distribution, it is second in rank. For retirement age, the values were from 61 to 67: 61, 62, 63, 64, 67 in the positive skew condition and 61, 64, 65, 66, 67 in the negative skew condition. Table 2 presents the figures for saved amount, investment risk, and retirement age in the positive and negative skew conditions.

Table 2. Figures for saved amount (£), investment risk (%), and retirement age in the two conditions of Experiment 2

Low context			High context		
Save	Risk	Retire	Save	Risk	Retire
1500	0	61	1500	0	61
2000	10	62			
2500	20	63			
3000	30	64	3000	30	64
			3500	40	65
			4000	50	66
4500	60	67	4500	60	67

Results

Savings

The proportion of times each saving option was chosen in the positive skew and negative skew conditions is plotted in Figure 5. The error bars represent the standard error of the mean.

The distribution of responses in each condition seems to be skewed towards the central option, similar to the full context condition in Experiment 1. There was no significant difference between the proportion of times the option £3000 (12%) was selected in the two groups (0.33 in the negative skew condition versus 0.30 in the positive skew condition), $t(22) = -0.28$, $p = 0.780$, which means that the rank order of options did not have an effect on the common saving option. Note that we expected that the 12% option would be perceived as less attractive in the positively skewed distribution, where it was fourth in rank compared to the negatively skewed distribution, where it was second in rank. The results did not support this prediction.

Note also that although this can be interpreted as a lack of context effect on the perception of a particular item, there is still a huge context effect in terms of the cumulative analysis we presented in Experiment 1. In the negatively skewed context, nearly all participants saved 12% or more, while in the positively skewed context, only around 75% did so. Such a difference indicates a strong difference in evaluations and choices related to amount of savings as a function of context.

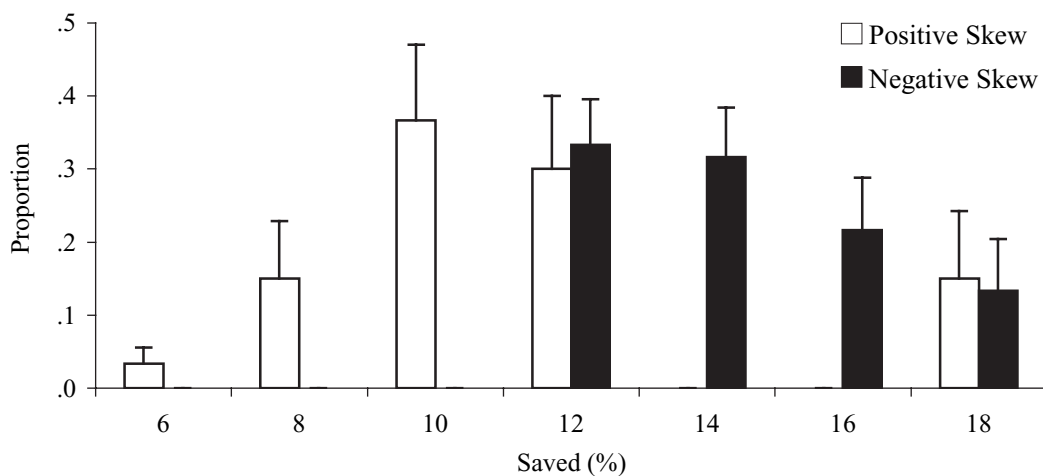


Figure 5. Proportion of times each saving option was chosen in the positive skew and negative skew conditions, Experiment 2. (Error bars are standard error of the mean)

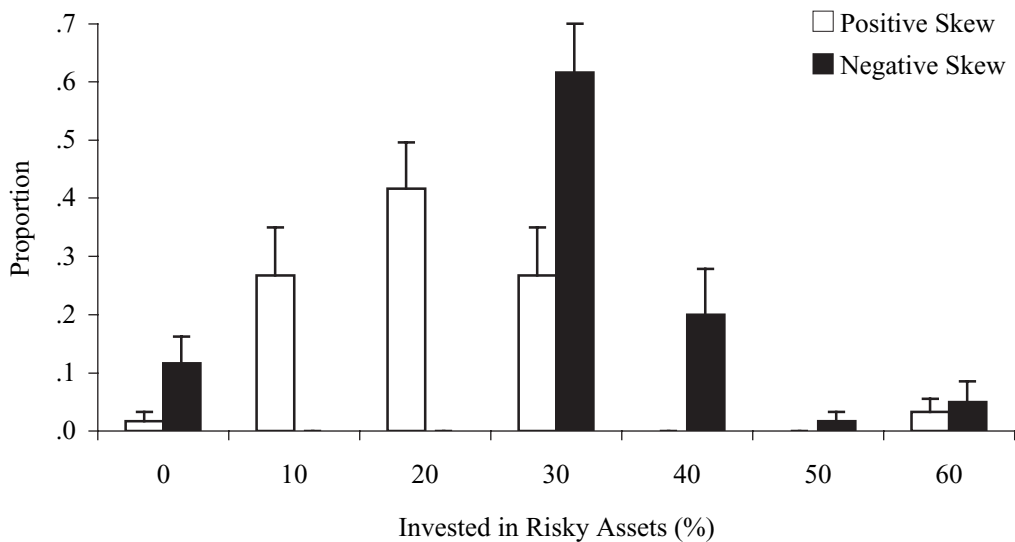


Figure 6. Proportion of times each investment risk option was chosen in the positive skew and the negative skew conditions, Experiment 2. (Error bars are standard error of the mean)

Risk

The proportion of times each investment risk option was chosen in the positive skew and the negative skew conditions is plotted in Figure 6. The error bars represent the standard error of the mean.

The distribution of responses was very much skewed towards the lower options. The proportion of times the option 30% was selected in the negative skew condition was 0.62, which was significantly higher than the proportion of times this option was selected in the positive skew condition, which was 0.27, $t(22) = 2.91$, $p = 0.008$. It appears that when the 30% option was higher in rank in the positive skew condition compared to the negative skew condition, it was perceived as more risky and hence less attractive. Since 30% was the most attractive option in the full context condition in Experiment 1, we can rule out the possibility that the rank effect was due to participants' natural preference for lower levels of risk, and conclude that the rank order had a significant effect on the choice of risk. Note also that in the positive skewing context in Experiment 2, 97% of choices in investment risk were at a rate of 30% or less, whereas in the negative skewing context, 73% of choices were at a rate of 50% or less. Thus, the contextual set of alternatives had an effect on overall risk percentages across all risk options (similar to the global effects on saving).

Discussion

The results show that the rank order of the options within the choice set selectively affects only the choices of the test option for investment risk, while the choice proportions for the common savings alternatives did not differ. In particular, the common investment risk options that had a higher rank were perceived as more risky. However, the preferences for saving were altered by the rank manipulation because there were large context effects on savings when viewed cumulatively. In the positive skewing context, 85% of participants chose to save at a rate of 12% or less, whereas in the negative skewing context, only 36% of participants saved at a rate of 12% or less. Thus, the contextual set of alternatives had an extremely large global effect on overall savings percentages.

An interesting difference is that the effect of the choice set was stronger for the savings than for the risk-related decisions in Experiment 1, while the reverse result was evident for the effects of the skew on the target common option in Experiment 2, where the context effect on this option was stronger for the risk than for the saving decisions. One possible interpretation of this particular result is that there might be different weighting on the range and rank factors for the different dimensions of judgment, which was originally proposed by the range–frequency theory (Parducci, 1965, 1974). Thus, there is a parameter that specifies the relative contributions of rank and range, and it is possible that for certain attributes, the contributions of range and rank are exclusively weighted towards one of these two factors (by setting the weight of the other factor equal to 0). Therefore, it is possible that in Experiment 2, there has been differential weighting of the impact of rank (skew) on the judgments related to saving and risk. One possible interpretation is that rank is more strongly affecting the choices of risk (and hence no effect on the common test option). However, the large context effects on savings when viewed cumulatively suggest also the interpretation that there is no local effect on the particular item (as we expected), but there is a global effect across the whole range of options. In order to further test the validity of these ad hoc explanations, we conducted Experiment 3.

EXPERIMENT 3

In order to test the hypothesis that savings and risk receive different weights, we next further manipulated the skew of the distribution of values. One possible reason for the lack of an affect upon savings in Experiment 2 is that the range of presented values was too narrow and the 12% saving option was only fourth in rank. This ranking might not have been enough to make the participants rate this option as high (although it worked for risk, but this could simply mean that people are more sensitive to changes in risk and variability). Thus, a direct way to test the relative weighting of the rank is simply to conduct an experiment testing whether one or another dimension of judgment is more or less affected by manipulation of the rank of the test options.

In this experiment, the 12% saving option was sixth in rank. The range of values spanned from 0 to 100% for risk and from 2 to 22% for savings (as in the full context condition in Experiment 1). The comparison options between the positive and negative skew conditions were again the 12% savings option and this time, the 50% risk option (because the test options should be positioned in the middle of the range of presented values). If the effects of the choice set were the same as in Experiment 2, that is, no effect on the 12% saving option, while the 50% risk option was again significantly more attractive in the negatively skewed condition (when it was second in rank), then this is plausible evidence that the rank does not have a significant local effect on individual common items.

In summary, for the savings options in the positively skewed distribution, the offered values were: 2, 4, 6, 8, 10, 12, 22%; while in the negatively skewed distribution, the offered values were: 2, 12, 14, 16, 18, 20, 22%. In the positively skewed condition, the option 12% has a higher rank by being sixth in the rank order of options, compared to the same option in the negatively skewed condition. Thus, we assumed that if we used a wider range of possible values, this would further corroborate the results in Experiment 2.

The same principles applied in the design of the investment risk options. Thus the condition with the positive skew contained the values 0, 10, 20, 30, 40, 50, 100%; while the negative skew condition included the options 0, 50, 60, 70, 80, 90, 100%. Here, the key comparison between the two groups was the option 50%, which had different rank in the two conditions: in the positive skew, it was sixth in rank, while in the negative skew, it was second in rank. Table 3 presents the figures for saved amount, investment risk, and retirement age in the positive and negative skew conditions.

This design of the risk options can also help us to resolve an interpretation problem with the results for risk in Experiment 2. Specifically, it allows us to see if the very high preference for the 30% option in the negative skew in Experiment 2 could have arisen from an ideal (natural) risk preference of around 20% amongst most participants (and hence, given the limited choice options, they should choose the 30% option). The current

Table 3. Figures for saved amount (£), investment risk (%), and retirement age in the two conditions of Experiment 3

Low context			High context		
Save	Risk	Retire	Save	Risk	Retire
500	0	48	500	0	48
1000	10	50			
1500	20	52			
2000	30	54			
2500	40	56			
3000	50	58	3000	50	58
			3500	60	60
			4000	70	62
			4500	80	64
			5000	90	66
5500	100	68	5500	100	68

design allowed us to check that possibility, for if people naturally prefer 20% (although the most preferred value in the full context condition was around 30%), then most choices now should be on the 50% option (and in Experiment 2, almost all choices were on the 0, 30, and 40% options anyway). However, if a reasonable proportion of choices in this experiment appeared to be above the 50% option, then this would refute the possibility that in Experiment 2, most people naturally preferred risk values around 20% and would also demonstrate significant context dependence.

Method

Participants

Twenty-four different volunteers participated in this study. Twelve participated in the positive skew condition and 12 in the negative skew condition. All participants were students from the University of Oxford and none had participated in Experiments 1 and 2. They were paid £5 for taking part in this experiment.

Design and procedure

The general design and procedure were the same as in Experiment 2. The option values for the answer tables for each question were derived by simply deleting four choice options (rows) from each table in the free choice condition. Thus, the positive skew condition was derived by deleting four rows from the upper half of each table for the questions related to savings and investment risk, while the negative skew condition was derived by deleting four rows from the lower half of each table.

Results

Savings

The proportion of times each savings option was chosen in the positive skew and negative skew conditions is plotted in Figure 7.

The distribution of responses in each condition seems to be skewed towards the central option as in the full context (free choice) condition of Experiment 1. There was no significant difference between the proportions of choices of a 12% saving rate in the two groups (0.22 in the negative skew vs. 0.25 in the positive skew), $t(22) = 0.37$, $p = 0.717$, which means that the rank order of options again did not have a particular effect on

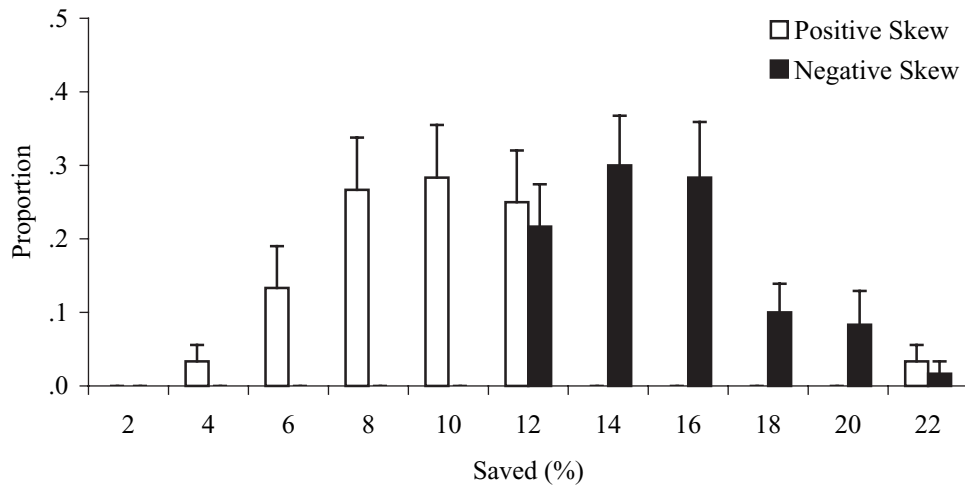


Figure 7. Proportion of times each saving option was chosen in the positive skew and negative skew conditions, Experiment 3. (Error bars are standard error of the mean)

the common savings test option. Again, however, the preferences for savings were altered by the rank order because there were large set contextual effects on savings when viewed cumulatively. In the positive skewing context, 97% of participants chose to save at a rate of 12% or less, whereas in the negative skewing context, only 22% of participants saved at a rate of 12% or less.

Risk

The proportion of times each investment risk option was chosen in the positive skew and the negative skew conditions is plotted in Figure 8.

The distribution of responses in the negative skew condition was very much skewed towards the lower options. The proportion of times people selected an investment risk of 50% in the negative skew condition (0.55) was significantly higher compared to the proportion of times this option was selected in the positive skew condition (0.13), $t(22) = -4.17$, $p = 0.0001$. This demonstrates a clear context effect of the rank order on the 50% option. Also, as Figure 8 demonstrates, around 34% of the choices are above the 50% option, which suggests that there are considerable context effects and people do not naturally prefer risk lower than 30% (thus counting against the possible interpretation of the results of Experiment 2 that are considered above). There was also an overall shift of risk preferences due to the change in the contextual set of alternatives. In the positive skewing context, 100% of choices of investment risk were at a rate of 50% or less, whereas in the negative skewing context, 67% of choices were at a rate of 50% or less.

Discussion

The choice proportions for the common savings alternatives did not differ, but the savings rates for the two groups differed dramatically because the contextual set of alternatives had an extremely large effect on overall savings percentages. Thus, we replicated the strong global context effect on the savings dimension, although there was no significant local context effect on the individual test items. Only on the choices of risk was there a significant effect of the rank order on the common test option in the choice set. This result corroborates the finding in Experiment 2 that the savings dimension is affected differently by the rank. The

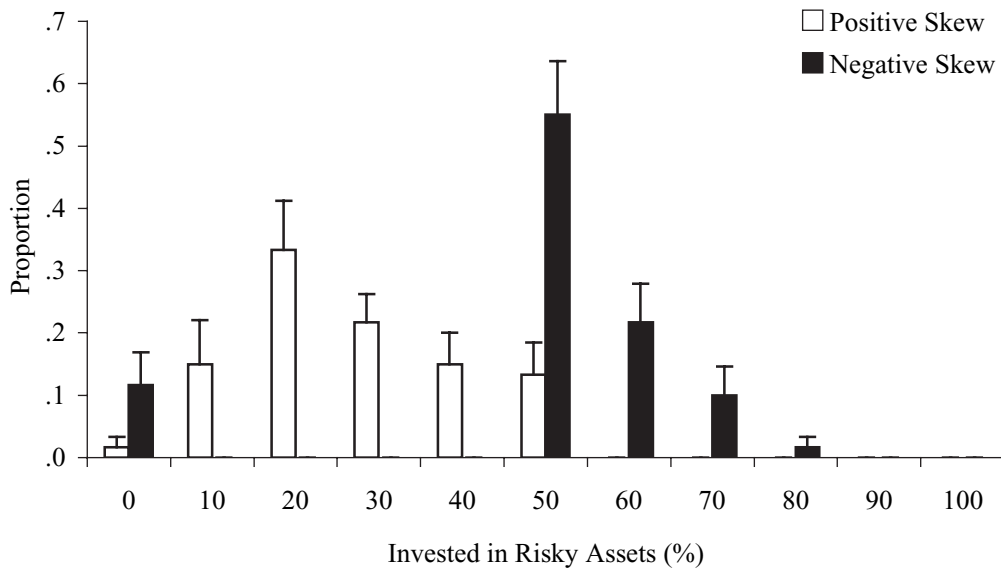


Figure 8. Proportion of times each investment risk option was chosen in the positive skew and the negative skew conditions, Experiment 3. (Error bars are standard error of the mean.)

results also show that a considerable proportion of the choices are in the band of risk options above 50%, which rejects the possibility that people naturally prefer very low-risk values. Therefore, the results in Experiment 2 suggest that the effects are due to the rank order of options in the choice set.

MODELING THE DATA

In order to directly test and compare the different accounts of our results, we decided to model the data. As described briefly above, we assumed that the probability of choosing an option is proportionate to its attractiveness (the simplest form of Luce's (1959) choice rule); and so we modeled attractiveness using the framework of ideal point models (Coombs, 1964; Risky et al., 1979; Wedell & Pettibone, 1999) as a basis for a theory of the attractiveness of savings and risk options. This class of models is broad enough for us to instantiate both adaptation level and range–frequency accounts of how people represent the underlying risk–return values in the judged options. That is, our modeling framework was able to capture the two different models of the nature of distortions of judgment by context, and thus to encapsulate how these contextual manipulations might lead to modifications of people's choices of risk–return trade-off.⁵ As a result, we could show explicitly how the equations implementing each theory can directly predict our data. Such mathematical modeling could provide a stronger, clearer, and more compelling analysis of any effects we observed by specifying our model and also by comparing competing models. In this way, the analysis could hopefully provide clearer boundaries for our interpretation. If, on other hand, several models explained the data equally well, that should also be recognized and future research could determine conditions that might distinguish these models.

⁵We thank an anonymous reviewer for suggesting this line of inquiry and for very detailed guidance and feedback.

The hope, then, was that this framework would allow us to see how far modification of an ideal point constructed by the current set could possibly account for the choice-set effects that were observed in Experiments 1–3—whether from an adaptation level theory or a range–frequency theory perspective. For example, having such a constructed ideal point could possibly account for the choice set effects in Experiment 1, where the mean was relatively high in the high context, average in the full context, and low in the low context; and also for skew effects as in Experiment 2, where the mean was higher in the negative skew condition, in which the comparison options were above the mean, while in the positive skew condition, the key options were below the mean. The position and the malleability of the ideal could also possibly reveal why there was no rank effect on the comparison options (12%) for savings in Experiment 3. If we assume that the ideal has not changed between the context conditions and is fixed on the comparison option, this would imply that there would be no difference between the comparison options across context conditions.

There are several ways that a modeling framework for data of this kind may be constructed. One is given in a recent paper by Cooke, Janiszewski, Cunha, Nasco, and De Wilde (2004). These authors show one way to combine range–frequency scales to determine preference judgments. Another approach is presented by Wedell and Pettibone (1999), who show that a Gaussian ideal point model can use the range–frequency scale or the stimulus scale with shifting adaptation levels. We chose this latter method to do a data fit, as it allows us to compare with ease the two main theoretical contenders, range–frequency theory and adaptation level theory.

Following the simplest form of Luce’s choice rule, that the probability of choosing an option i , in context k , is proportional to its attractiveness, our basic assumption is:

$$\Pr(\text{Choose}_{ik}) = \frac{\text{Attract}_{ik}}{\sum_j \text{Attract}_{jk}} \quad (1)$$

We modeled a single-peaked preference for savings and risk with a Gaussian similarity function of the form:

$$\text{Attract}_{ik} = a + b \cdot e^{-c(\text{Rep}_{ik} - \text{Ideal}_k)^2} \quad (2)$$

where the attractiveness of stimulus i in context k is a rapidly decreasing function of the distance between the subjective value, Rep_{ik} , of stimulus i in context k (i.e., Rep denotes its representation on a putative internal psychological scale) and the Ideal (i.e., ideal point or most preferred value on the particular dimension) in context k . The b parameter of Equation 2 was not used, as it is just a multiplicative constant (determining the height of the function when mapping it onto the stimulus scale) and the Luce rule is invariant under multiplicative constants. The additive constant a was also dropped, as it is almost 0.0 for all the fits. In other words, we fixed parameters $a=0$ and $b=1$. The discriminability parameter c (determining the width or narrowness of the rating function), the scale value, and the ideal point (Ideal_k), were allowed to differ with context. Thus, the differences between contexts were captured by variation of these three parameters.

The range–frequency-based model assumes that the relevant magnitudes (here risk–return values) are not represented in absolute terms, but according to the range–frequency theory. Ideal values are then estimated as free parameters. More specifically, range–frequency theory uses the following equation:

$$\text{Rep}_{ik} = wR_{ik} + (1 - w)F_{ik} \quad (3)$$

where Rep_{ik} is the internal representation of stimulus i in context k . R_{ik} is the range value and F_{ik} is the “frequency” (or more accurately “rank”) value of stimulus i in context k , while w represents the relative

weighting of range and frequency values. Range values are calculated by the following equation:

$$R_{ik} = \frac{S_i - \text{Min}_k}{\text{Max}_k - \text{Min}_k} \quad (4)$$

where S_i is the objective scale value of the stimulus, and Min_k and Max_k are scale values defining the subjective range. Frequency values are calculated using the following equation:

$$F_{ik} = \frac{\text{rank}_{ik} - 1}{N_k - 1} \quad (5)$$

where rank_{ik} is the rank in the stimulus context, and N_k is the total number of stimuli making up the context.

In order to implement adaptation level theory as outlined by Helson (1964), we decided to fix the scale value as equal to the stimulus value (i.e., assuming no subjective transformation, as in range–frequency theory), that is, $\text{Rep}_{ik} = S_i$. We then let the ideals be determined by a version of adaptation level theory that weights the mean of the stimulus series with a background value:

$$\text{Ideal}_k = w^*(\text{Background}) + (1 - w^*)S_{\text{mean}_k} \quad (6)$$

where *Background* is the adaptation level with which participants begin the experiment and S_{mean_k} is the mean of the stimuli in context k ; w^* represents the relative weighting of the two. Thus, adaptation level is a weighted average of a background value and the mean of the values experienced (Helson, 1964). This model has three free parameters— c , w^* , and the *Background* adaptation level.

Method

Equation 1 was used in the fitting procedure using a maximum likelihood fit to the proportion data. By fitting the proportions directly rather than using conventional least squares fit to means, the maximum likelihood procedure would yield more accurate estimates. As these are proportions, they must sum to 1.0 so that for six data points (choice proportions) in a distribution (e.g., in the low context condition in Experiment 1), only five are free to vary as the last one must equal one minus the sum of other proportions. This constraint is part of Equation 1 and was reflected in the fitting procedure and degrees of freedom.

Our initial approach was to fit a single model to the data across the contextual conditions and free up parameters if this provided a better fit. There was a *baseline* model with just two parameters, c , and *Ideal*, which was compared to hierarchically nested models that allow the ideal point to vary with context or to have a separate parameter c , for each context condition. Thus, for the savings results in Experiment 1, this meant fitting the 23 data points (proportions) for full, low, and high context conditions (shown on Figure 3) with a single equation. This was done by dummy coding the contextual conditions and then multiplying the dummy codes by a unique parameter for each condition, (e.g., *ideal—high*, *ideal—low*, etc.) in order to fit that parameter to that condition, whilst holding the other parameters of the model constant all conditions. Thus, there is a loss of one degree of freedom for each distribution (i.e., condition) included in the fitting procedure. For example, in fitting Experiment 1, we lose 3 degrees of freedom because there are three choice sets (conditions) fitted simultaneously with the same set of parameters.

Using this hierarchical approach, we tested the need for the free parameters by looking at change in the Akaike information criterion (AIC, which is a statistical model fit measure developed by Akaike (1974); see also Burnham & Anderson, 2002; though see Pitt, Myung, & Zhang, 2002, for an alternative approach). It quantifies the relative goodness-of-fit of various previously derived statistical models, given a sample of data. It uses a rigorous framework of information analysis based on the concept of entropy. The driving idea behind

the AIC is to examine the complexity of the model together with the goodness of its fit to the sample data, and to then produce a measure which balances the two. Its formula is:

$$\text{AIC} = 2k - 2 \ln(L) \quad (7)$$

where k is the number of parameters, and L is the maximum likelihood function. A model with many parameters will provide a very good fit to the data, but will have fewer degrees of freedom and be of limited utility. This balanced approach discourages overfitting (i.e., favoring parsimony and simplicity). The preferred model is that with the lowest AIC value. The AIC methodology attempts to find the minimal model that correctly explains the data, which can be contrasted with more traditional approaches to modeling, such as starting from a null hypothesis. Variations of AIC include AICc, which is better than AIC when sample size (the number of observations), n , is small (i.e., $n/k < \sim 40$). The formula for AICc is:

$$\text{AICc} = \text{AIC} + \frac{2k(k+1)}{n-k-1} \quad (8)$$

Since AICc converges to AIC as n gets large (the last term of the AICc approaches zero), it is recommended to practically use AICc in any case (Burnham & Anderson, 2002, 2004).

There is one simple measure associated with the AIC, which can be used to compare models: the delta AIC. It is easy to compute, as calculations remain the same regardless of whether the AIC or AICc is used, and also has the advantage of being easy to interpret (another good measure is the more complicated Akaike weight which we do not consider here). The delta AIC (Δ_i), is a measure of each model relative to the best model, and is calculated as

$$\text{Delta AIC} = \Delta_i = \text{AIC}_i - \text{minAIC} \quad (9)$$

where AIC_i is the AIC value for model i , and minAIC is the AIC value of the best model. As a rule of thumb, a $\Delta_i < 2$ suggests substantial evidence for the model, values between 3 and 7 indicate that the model has considerably less support, whereas a $\Delta_i > 10$ indicates that the model is very unlikely (Burnham & Anderson, 2002). Note that the AIC is not a hypothesis test, does not have an α -value, and does not use notions of significance. Instead, the AIC focuses on the strength of evidence (i.e., Δ_i), and gives a measure of uncertainty for each model. We decided to compare the performance of the two models on the basis of AICc as it provides a better balance between the complexity of the model and the goodness of its fit to the sample data.

The method described above tests the more generic and important question of whether context effects in Experiments 1–3 can be adequately described as a shift in ideal points along a single continuum, following the basic assertion by Coombs in his portfolio theory (Coombs, 1969, 1975) that there is an ideal risk value. In addition, this method could in principle allow us to test between models, such as the adaptation level model and range–frequency valuation.

As we show in Equation 6, the adaptation level model is developed by simply substituting into Equation 2 the right side of Equation 6 for the Ideal_k parameter. Note this should be done under the constraint that the parameters *Background* and w are held constant for individuals within an experiment so that any changes in contextual shifts of ideals are attributed to differences in the means of the distributions. (The other parameters merely set an intercept and a limit on the modulation of the ideal by the change in context.) Here, we simultaneously fitted the model across contextual conditions and constrained the parameters across these conditions. For example, to fit Experiment 1, we hold c , w^* , and *Background* constant so that the 23 proportions (or frequencies, as we used the maximum likelihood fitting method) are fitted by 3 parameters. This 3-parameter model allows weighting of the mean of the contextual series (via fitting w) and thus, different ideal points can be predicted by the differences in means.

The range–frequency model can be fitted in a similar way, but there are some differences. First, as we explained before, the scale values are determined by the range–frequency equation. However, the judgment-mediated model makes predictions about the location of the ideal point as well. The basic version of the model has parameters for c , w , and Ideal_k . Here, Ideal_k is the value on the range–frequency subjective scale that is preferred. We can assume that the value of the Ideal_k in this version is fixed on the judgment scale (e.g., the ideal risk could be 0.50 on the judgment scale running from 0 to 1). Note that contextual changes predict different ideals because the same ideal value on the subjective scale corresponds to different values on the objective stimulus scale in each context condition (due to the range and rank-based transformations). If the subjective range is now equated with the stimulus series range (i.e., the current context), then frequency (rank) values and range values are the same (i.e., range values become useless in this implementation of the range–frequency theory). In order to overcome this problem, we assumed that people enter the lab with the full range of possible savings and risk values. For risk, it is natural to assume that people anchor the possible percentage of their retirement savings that can be invested in risky assets on between 0 and 100% (obviously people cannot have negative savings, or invest more than 100% of their savings). For the range of possible savings values, it is equally easy to imagine that the lower boundary is fixed at 0%, while the upper limit depends on many factors such as legal requirements, cost of living, etc. We fixed the savings range across all conditions at values 0% and 22% (the range for the full range condition) because 22% approximates the upper bound for the retirement savings rate in UK due to legal and tax restrictions (higher values produced similar modeling results).

Results

Model fit

Table 4 presents the best fitting range–frequency model and adaptation level model for savings and risk choices in Experiments 1–3. In summary, in three out of six cases, range–frequency theory had a better fit (for risk in Experiment 1, and saving and risk in Experiment 3). The difference was big enough ($\Delta_i > 3$) only for

Table 4. Results from modeling of the data in each choice domain and in each condition of Experiments 1–3 by fitting versions of adaptation level theory (AL) and range–frequency theory (RF). Only the best-fitting versions of each model are presented here

Experiment	Domain	Model	AICc	k	n	df	Ideal ₁	Ideal ₂	Ideal _{full}	w/w*	c
1	Saving	RF	−647.76	3	23	20	9%	15%	12%	0.59	10.6
	Risk	RF	−534.93	3	23	20	24%	52%	33%	0.61	20.7
2	Saving	RF	−346.54	3	10	8	12%	14%		0.85	15.3
	Risk	RF	−309.29	3	10	8	24%	24%		0.99	28.5
3	Saving	RF	−386.26	3	14	12	10%	15%		0.58	13
	Risk	RF	−352.95	3	14	12	28%	35%		0.81	18.1
1	Saving	AL	−644.99	3	23	20	9%	15%	12%	0.47	373.4
	Risk	AL	−539.36	3	23	20	23%	45%	34%	0.55	25.7
2	Saving	AL	−345.77	3	10	8	13%	14%		0.68	477.9
	Risk	AL	−308.43	3	10	8	25%	25%		1	28.5
3	Saving	AL	−390.18	3	14	12	12%	14%		0.73	312.2
	Risk	AL	−353.37	3	14	12	28%	33%		0.82	19

Note: df indicates the degrees of freedom. Ideals are the inferred ideal-point values by the model. The range–frequency model predicts the ideals on a transformed (subjective) scale between 0 and 1. The values of these ideals on the (objective) stimulus scale are derived via linear approximation rounding up to the nearest percentage point. Ideal₁ is the ideal in the low-context condition in Experiment 1 and the positive skew conditions of Experiments 2 and 3. Ideal₂ is the ideal in the high-context condition in Experiment 1 and the negative skew conditions of Experiments 2 and 3. Ideal_{full} is the ideal in the full context condition in Experiment 1.

risk in Experiment 1 and saving in Experiment 3, which supports the conclusion that in these two cases, the range–frequency model had considerably more support. The adaptation level model had higher AICc also in three cases: for saving in Experiment 1 and saving and risk in Experiment 2. However, the difference (Δ_i) was not bigger than 3, which implies that adaptation level theory does not have considerably more support in these cases. In general, the adaptation level theory had AICc similar to that of the range–frequency theory and we cannot categorically conclude that one or the other theory had a better overall fit. In other words, these results indicate substantial evidence for both models (i.e., we cannot unambiguously distinguish these models).

We were not able to obtain a better fit by a 5-parameter model that allowed the parameter c to be fitted separately for each condition for both models, as these model versions had AICc higher ($\Delta_i > 3$) than the AICc of the 3-parameter versions. Therefore, we concluded that adding new parameters does not sufficiently improve the models' goodness of fit to compensate for the increase in their complexity. (Remember that the information criteria are based on parsimony and penalize models with additional parameters.)

We also considered a version of range–frequency theory that allows the ideal point to vary with context. This was done by dummy coding the contextual conditions and then multiplying the dummy codes by a separate parameter for each context condition (e.g., in Experiment 1, these were $\text{Ideal}_{\text{high}}$, $\text{Ideal}_{\text{low}}$, $\text{Ideal}_{\text{full}}$) to fit that parameter only to that condition while holding the other parameters constant across conditions.⁶ However, in all experiments, this 5-parameter model showed a worse fit, as measured by AICc, in comparison with the 3-parameter version which had one ideal that fitted across all contextual conditions.

The usefulness of the model fitting is more evident in explaining the lack of effect on the common test option for saving in Experiments 2 and 3. First, the w values in the range–frequency fit are consistently higher for risk than for saving. This is consistent with the assertion that risk is not as rank-dependent as saving. Also, the w values in the adaptation level fit are also consistently higher for risk than for saving. This is consistent with the assertion that risk is not as context-dependent as saving (recall that here w reflects the importance of the *Background*, that is, the adaptation level with which participants begin the experiment, relative to the mean of the stimuli in the current context). This result suggests that due to the strong context effect on saving, most choices in the positively skewed condition would be distributed across the lower options, while in the negatively skewed condition, the majority of choices would be distributed across the higher options. According to this scenario, the common saving option (12%) would receive a relatively lower proportion of choices in both conditions and as a result, this option might end up with similar proportions across both conditions. In summary, bigger displacement of choices due to stronger context effects on saving could better explain the lack of effect on the common saving option in the rank manipulation in Experiments 2 and 3.

How “ideal points” change across conditions

Table 4 shows that the range–frequency model and the adaptation level model inferred very similar ideal points in each condition. The ideals inferred by range–frequency theory shifted with context in all domains (both savings and risk) and experiments except for risk in Experiment 2. For example, in Experiment 1, the ideal for saving in the low context condition (9%) is slightly lower than the ideal in the full context condition (12%), while the ideal in the high context condition (15%) is higher than in the full context condition (see Table 4). Similarly for risk, the ideal in the high context condition (52% mix of risky/fixed return) is higher than in the full context condition (33%), which is in turn higher than in the low context condition (24%). These results are a clear indication that the context (choice set) has affected the ideal-points on each attribute dimension, which captures the results in Experiment 1 and also implies that there are no stable internal preference scales for saving (consumption) and risk. In summary, the range–frequency-based ideals for saving and risk in Experiments 2 and 3 are lower in the positive skew condition, which is a clear

⁶We thank an anonymous reviewer for suggesting this approach.

demonstration that the ideal points for saving and risk are affected by the skew manipulation. This general pattern demonstrates the usefulness of the ideal point approach in explaining this type of context effects.

The inferred ideals for saving and risk in Experiments 2 and 3 reaffirm the previous conclusion that the rank context had a stronger effect on saving, because the ideals for risk appear to be much more stable (less malleable) and closer to each other. Thus, for example, in Experiment 2, the ideal for saving moves from 12% in the positive skew condition to 14% in the negative skew, while the ideals for risk are 24% in both conditions. In Experiment 3, the ideals for saving inferred by range–frequency theory moved from 10 to 15%, which is a 23% shift on a 0–22% scale, while the ideals for risk moved only by 7% based on a 28–35% shift on 0–100% scale. In summary, our model fits suggest that the rank order manipulations must have shifted the ideals up and down to a greater degree on the savings dimension than on the risk dimension. This might be caused by the ideals for savings being more malleable to context effects.

The inferred ideals for savings and risk in Experiments 2 and 3 could also help us understand why there was no effect of rank on the key comparison (test) option for savings (the 12% option). Recall that the farther away an option is from the ideal, the less attractive it is. The general pattern shown in Table 4 is that the ideals for risk in the negative skew conditions are all below the comparison option (30% in Experiment 2 and 50% in Experiment 3), which makes this option most attractive; while the ideals for savings in the negative skew conditions are all above the comparison option (12% in both experiments), which makes this option not so attractive.

Discussion

In summary, the model fitting results are a clear demonstration of how mathematical modeling of the data can provide new and interesting interpretations. Without the modeling, one would be inclined to assume that the skew manipulation has less of an effect on the saving dimension, while now we can see that the higher weighting of rank and context for the saving dimension could be the main factor explaining the results. The position of the ideals on each dimension could also provide new interpretations. We were not able to clearly distinguish the performance of the two competing models. However, even if the modeling cannot provide answers to all our questions, the modeling process clarifies which classes of models can explain the data and which aspects of the data are model critical. We have found that each model can handle the data well, and that ideal point-based implementation of contextual judgment models can well explain context effects of the kind demonstrated in this article.

Here, we have built on prior work by Stewart et al. (2003) that demonstrates the relativity of evaluations of financial prospects. In prior work, estimating certainty equivalence was a more straightforward application of relativistic models like the range–frequency theory because the response function is monotonic. In the current work, participants select their preferred level of savings and risk, which is better modeled in terms of a single-peaked response function. Basically, what the modeling helped us clarify is how context affects choice. Here, there is clear evidence that the ideal shifts with context. Note that this shift is not implied at all in the original versions of range–frequency theory or adaptation level theory. However, range–frequency theory can predict such effects after it is combined with assumptions about the relationship of ideals to stimulus values transformed according to the model. Similarly, adaptation level theory can predict these effects with the assumption that ideals shift toward the stimulus adaptation level.

In summary, our approach was mainly aiming to see exactly which classes of models are inconsistent with the data and which are consistent. Apparently, ideal point relativistic models like range–frequency theory and adaptation level theory are both consistent with the context effects observed here. Note, however, that the experiments presented in this article were clearly not designed to test between specific models, but rather to demonstrate a phenomenon, which we referred to as prospect relativity—first observed in a choice between gambles by Stewart et al. (2003) and now applied to the context of financial decision-making under risk (we see it as part of the big family of choice set contextual effects demonstrated by other researchers in recent years).

GENERAL DISCUSSION

The results presented in this paper suggest that when people make financial decisions, the preferred option depends on the other available options. In Experiment 1, the set of options offered as potential savings and risk options was shown to have a large effect on the selected options. The same option was significantly overvalued or undervalued if it was presented in the low range or the high range condition, respectively. In Experiment 2, we demonstrated that the rank order of the options in the choice set affects the preferences for risky investment such that options with higher rank were considered as more risky and unattractive; while the saving dimension was affected by the rank only across all choice options, there was no effect on the common test option. Experiment 3 used a wider range of choice options and replicated the pattern of results shown in Experiment 2. Thus, in both Experiments 2 and 3, the risk dimension was affected both locally at the level of individual test item and also globally across all choice options. However, the saving dimension was affected only at a global level across all items, but the rank order did not appear to have a local effect on the comparison test option. One immediate interpretation of this result could be that the choice set had a stronger effect on the risk dimension. However, the modeling showed that the context (rank or stimulus set mean) had a higher weighting for saving than for risk. This model fitting result suggests the alternative, and more plausible, interpretation that due to the strong context effect on saving, the majority of choices in the positively skewed condition would be distributed across the lower options, while most choices in the negatively skewed condition would be distributed across the higher options. This skewed distribution of the choices across higher and lower options, respectively (clearly shown on Figures 5 and 7), resulted in the common test option being chosen with similar proportions across both context conditions. In summary, stronger context effects on savings, as suggested by our modeling, could better explain the lack of local context effects in the rank manipulation in Experiments 2 and 3. This interpretation is corroborated by the fact that in the negative skew condition, the proportion of choices above the common test option was 64% in Experiment 2 and 78% in Experiment 3. For risk, the choices above the common test option were 27% in Experiment 2 and 34% in Experiment 3. This implies that the set of alternatives affects saving choices by a factor of 2 (i.e., a doubled displacement for the saving choices compared to the risk choices).

In general, it seems that the context provided by items that are considered simultaneously does affect decisions about saving and risk. These results could be considered as an example of the prospect relativity principle, which suggests that risky prospects are judged relative to accompanying prospects (Birnbaum, 1992; Stewart et al., 2003). Thus, this finding presents another challenge to standard normative models as descriptive theories of decision under risk and to other theories where prospects are independently valued.

Range–frequency theory has already been used to account for context effects in decision-making under risk. Birnbaum (1992) and Stewart et al. (2003) found their data to be consistent with the theory. The range and frequency (rank) principles are both consistent with the result in Experiment 1, which showed that preferences for saving and risk are very much determined by the set of offered choice options; in particular, preferences for the 12% (£3000) saving option and 50% risk option were different in the high- and low-context conditions in comparison with the full context condition. The frequency principle is consistent with the result in Experiments 2 and 3, which demonstrated that when the choice options were positively skewed (e.g., when the risk options 30% and 50% had higher ranks), then these options might have appeared unattractive because it was selected significantly less than in the negatively skewed distribution.

Our model fitting results showed that ideal point-based relativistic models such as range–frequency theory and adaptation level theory are both consistent with the context effects observed in our experiments. With the exception of Birnbaum's (1992) and Stewart et al.'s (2003) studies, range–frequency theory has not been applied explicitly to judgment of risk. We are not aware of an adaptation level-based model of risk decisions. To apply either of these two theories to judgments of risky options, we need to assume that people are poor at making judgments about the absolute risk attached to each choice option, choosing instead to judge the risky options relative to each other. Stewart et al. point out that such relative comparisons will allow people only to

evaluate which options are more risky relative to other options in the set. However, Stewart et al. also conclude that such comparison does not provide information on how risky the overall set is, because the options in the set may all be relatively low risk, relatively high risk, or represent the entire range of risk. Therefore, people will be unable to make a reliable judgment about the absolute level of risk attached to each option. Similarly, their ideal point will shift depending on the context, as our modeling results demonstrated.

As we stated at the beginning of this article, our main objective was to test the real-world validity of the prospect relativity principle and it seems that the results presented here support the results of Stewart et al. (2003) concerning the effects of the context as defined by the choice set.

However, there was also evidence that people have some stable preference for risk and variability as the participants seemed to prefer mostly low-risk investments (first, because all ideal points for risk were less than 50% and second, because saving choices are more rank dependent than risk choices). In this respect, Loomes (in personal correspondence) notes that if we ask people questions in familiar domains about which they have made frequent judgments, they will show less variability than if the domains were unfamiliar (all other things being equal). This might be due, for example, to more anchors from their memories. Note, however, that the notion that people do not possess clear and stable preferences is currently the focus of a great deal of research (see Loewenstein, 2003, for a review). One conclusion from such research is that a great many of these decision-making experiments do not show the presence of some pre-existing stable structure of people's preferences. Instead, as Loomes (1999) suggests, it might be the product of people's somewhat unclear basic values interacting with what appear to them to be the salient features of the decision task, as they try to construct some representation of the problem. So when people are faced with a particular range of values, they might implicitly try to adjust their responses in order to be consistent with the particular scale of values they are contemplating, which will produce the context effects reported here.

If the internal representation of preferences is different depending on the decision context (as also suggested by the prospect relativity phenomenon, Stewart et al., 2003), then this implies that most of the experimental results on decision-making might be caused by custom-built responses that are sensitive to the nature of the test tools designed to elicit them and also to the properties of the particular task. This also means that most of these experiments measure context effects instead of real preferences, which is analogous to Laming's (1997) claim that the psychophysical scaling methods measure context effects instead of some stable internal scales. Such a view also resonates with Loomes's (1999) conjecture that it is not clear whether the information about values and preferences elicited from members of the public in order to inform policy decisions reflects something about their "true" values or merely reflects the nature of the particular instruments used to elicit that information.

Final summary and comments

In this study, we investigated aspects of hypothetical decision behavior in only one particular situation—long-term retirement saving and investment, with the particular objective of seeing whether people can be motivated, by manipulating the decision context in which the options are presented, to increase their saving rates and to take more investment risk. This was a twofold goal—on the one hand, this study has attempted to answer some basic psychological research questions related to the context malleability of human decision behavior, and on the other, it has tried to address some urgent practical problems.

The results as presented here have demonstrated that people are highly context sensitive and influenced by the set of options on offer across all key dependent variables investigated in this study. Thus, Experiment 1 corroborated Stewart et al.'s finding that this dependence is in relation to the set of simultaneously available choice options. However, Experiments 2 and 3 additionally discovered that risky financial decisions are also dependent on the skew of the riskiness of the options in the set, among which the focal option appears, which was originally tested with abstract gambles by Birnbaum (1992). Hence, the effects of the choice set appear to be robust in the context of practically relevant and realistic financial scenarios concerning how people make

fundamental decisions about their financial futures. Finally, we did model fitting to the data using ideal point-based versions of range–frequency theory and adaptation level theory, which showed that such relativistic models can explain the data well. Both models inferred very similar ideal points in each condition, which shifted with context. The modeling also demonstrated that savings choices are more context dependent than risk choices.

The results presented here have also clearly illustrated that one could manipulate savings and risky investment by manipulating the context distribution (range and skew) of choice options. Therefore, we accomplished our practical goal—to show how to help people save as much as possible. This is both important and relevant as, within the UK, current rates of savings amongst the population are much lower than the level required by government and to ensure financial security (as projected in the report by Oliver, Wyman & Company, 2001, which details the UK savings gap). We also showed how to encourage people to invest at a higher risk, although the issue whether people should be stimulated in this direction is still controversial. This also means that people are in principle unable to independently and autonomously make optimal decisions about their financial future, which is what other existing empirical evidence demonstrates as well (e.g., Benartzi & Thaler, 2002). Consequently, the presented results are also a direct test of whether the various documented context effects can be used in combination to produce certain desirable social objectives, and thus serve as a good example of how psychological phenomena and decision-making theories could be applied to solve real-world problems. For example, financial advisers could manipulate people to behave in a direction that is expected to maximize their expected welfare. The flip side of our results, of course, is the danger of exploitation as people's preferences and choices are malleable. Therefore, such results should at least be made knowledgeable to public, so that consumers are aware of their malleability, and regulators of the financial service industry are provoked into designing appropriate policies to deal with yet another possible threat to consumer confidence in this market.

APPENDIX A

Description of each question in Experiments 1–3. The questions are grouped by the key variable that the participants were asked to select (savings or investment risk).

I. Savings. These were five questions asking people to choose between savings options formulated as percentage that is saved out of the hypothetical income of £25 000 per year:

1. Choose how much to save without information about other variables.
2. Choose how much to save and see expected retirement income.
3. Choose how much to save and trade it off with retiring at different age and see the expected retirement income.
4. Choose how much to save and see the retirement income and its minimum and maximum variability happening, because of the assumption that 50% of the savings are invested in the stock market.
5. Choose how much to save and take different levels of risk starting from low savings and investment risk, and then increase both in parallel.

II. Risk. Next are the five questions asking people to choose levels of risk formulated as percentage of saving invested in risky assets:

6. Choose how much to invest without information about other variables.
7. Choose how much to invest and see expected retirement income and its variability.

8. Choose how much to invest and trade-off it with retiring at different age and see the expected retirement income and its variability.
9. Choose how much to invest and trade-off it with amount to be saved (increasing investment corresponding to decreasing savings) and see the retirement income and its variability.
10. Choose between levels of variability of the retirement income. Variability reflects different investment strategies and is increasing with the income (higher variability corresponds to higher income).

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