# Introduction To Quantum Computing 

## PHYS/CSCl 3090

Prof. Alexandra Kolla

Alexandra.Kolla@Colorado.edu ECES 122

Prof. Graeme Smith
Graeme.Smith@Colorado.edu JILA S326

## Why are we here?

- The world obeys Quantum Theory (old news!)
- Computers that fully harness quantum effects could outperform classical ones.
- Building quantum computers is very hard, but not ridiculously, impossibly hard.
- We are at a special moment: beginning to build nontrivial quantum computers
- This class: you will learn what a quantum computer is, why we think it'd be useful (quantum algorithms), and why we think it can be built (quantum error correction).


## There are quantum computers



Superconducting qubits Yale, Google, IBM, Rigetti


Ion traps
ionQ/UMD, NIST Boulder, Honeywell

Significant industrial effort in both hardware and software:
Amazon, Google, IBM, Microsoft, Rigetti, PsiQuantum, ionQ, Intel, Lockheed-Martin, ColdQuanta, Zapata, QC Ware, Xanadu...

Our goal: What are these things (going to be) good for?

## Today

- Logistics
- Who are we?
- Who are you?
- Clickers
- Grading
- Outline
- Assignment 0
- Due next Monday
- Covers linear algebra


## Prof. Kolla



Affiliation: Computer Science Office: ECES 122
Previously:
4 yrs at UIUC
Postdoc at Microsoft,
IAS Princeton
Research:Theoretical computer science, spectral graph theory, statistical physic, quantum computing.

Teaching: Complexity, Algorithms, Discrete math

## Prof. Smith



Affiliation: Physics and JILA Office: JILA S326 Previously: 9 yrs at IBM Research Postdoc in CS, PhD Physics

Research:Theoretical quantum information, and quantum computing. Esp. Error correction.

Teaching:Anything with Quantum Mechanics!

## 3090 Team

- Prof. Kolla and Prof. Smith

Alternate lectures by chapter covered. Joint office hours Friday 3-4 JILA X3I7

Graders
Steven Kordonowy
Ariel Shlosberg (Phys Helproom 2-4pm Tues + Thurs) Matteo Wilczak

## Who Are You?

- Quantum Computing Enthusiasts!
- Majoring in: Physics, Computer Science, Engineering Physics, Computer Engineering, Math, Astrophysics, Applied Math, Aero, EE, ....
- Took one of APPM 2360, APPM 3310, CSCI 2820,MATH 2I30, MATH 2135 , or something else covering linear algebra.


## Clickers!

Audience participation system. Excellent way to get feedback. Helps us not to lose you!

Standard clicker at CU.


Some of you may have or have seen these.

## Fire 'em up!

(push the On/Off button)
Should get Green light
If not, hold power until flashing green, Then push DC. Should go green solid.
$\longrightarrow$ (c)

## Clicker warm-up!

## TRUE (A) or FALSE (B):

My clicker is set to $D C$, is on, and is working.

## Clicker experience.

I have used clickers before:
A) YES!
B) No
C) |YES>+|NO>
D) $E=m c^{2}$
E) Look, it's still not green!

## Your iClicker



Put your name and contact information on your clicker!

If you lose it, there is a chance it will be returned.

Pro tip: You can put your contact information on a piece of tape on the clicker if you plan to return the iClicker in the future

## Your iClicker

## iclicker $f$

Responding with another student's iClicker is a violation of the Honor Code and you are encouraged not to do it.

## Clicker Points!

Participation points for each question answered.

Clicker points count for up to $\mathbf{2 \%}$ bonus points.

## Grading Scheme

- 30\% Weekly Problem sets
- 20\% Midterm I
- 20\% Midterm 2
- 30\% Final
- +2\% bonus from clicking


## Exams

- Midterm I: February 12 (in class)
- Midterm 2: March 18 (in class)
- Final:TBD

There are no rescheduled exams, so please put this in your calendar now.
Extra time midterm exams begin at same time in another location.

## Typical Weekly Schedule

| Monday | Tuesday | Wednesday | Thursday | Friday |
| :---: | :---: | :---: | :---: | :---: |
| 12 noonHW due |  |  |  |  |
| 2-2:50pm Lecture <br> 4pm old HW sol'n posted; new HW posted | 2-4 <br> Ariel S. in <br> Physics <br> Helproom | 2-2:50pm - <br> Lecture | 2-4 <br> Ariel S. in <br> Physics <br> Helproom | 2-2:50pm - <br> Lecture <br> 3-4 Office <br> Hours <br> JILA X3I7 |

## Class website

- https://home.cs.colorado.edu/~alko5368/indexCSCI3090.html
- Has logistics, assignments, additional reading, etc
- Also, keep up to date on Canvas


## Weekly Assignments

- Submitted via Canvas
- Scanned pdfs


## Textbook



Expected in bookstore on 0I/I5

## What we'll cover

- Chapter I: Classical and Quantum Bits and Circuits
- Chapter 2: Simple Algorithms (Deutsch, B-V, Simon)
- Chapter 6: Few-qubit Protocols (teleportation, dense coding, quantum cryptography)
- Chapter 4: Quantum Search (Grover's Algorithm)
- Chapter 3: Quantum Factoring (Shor's Algorithm)
- Chapter 5: Quantum Error Correction


## This week

- Wednesday:What's a classical bit (c-bit), and what's a quantum bit (qubit)? Reading: Mermin I.I.-I. 6
- Friday: Manipulating Quantum systems, quantum circuits
Reading: Mermin I.7-I.I2


## To Do

- Get your book
- Get your clicker
- Do Assignment 0 (due in ~45 hrs)



## Why are we here?

- The world obeys Quantum Theory (old news!)
- Computers that fully harness quantum effects could outperform classical ones.
- Building quantum computers is very hard, but not ridiculously, impossibly hard.
- We are at a special moment: beginning to build nontrivial quantum computers
- This course: you will learn what a quantum computer is, why we think it'd be useful (quantum algorithms), and why we think it can be built (quantum error correction).


## What is a bit?

## Anything that can be in one of two states!



Binary Digit

## What is a bit?

- Anything that can be in one of two states!

Might as well call these two states 0 and I Abstractly, a bit is just a variable that's either 0 or I.

## What is a bit?

## Anything that can be in one of two states!

$U=0, D=I$


$$
L=0, R=I
$$

## What is a bit?

- Anything that can be in one of two states!

Might as well call these two states 0 and I Abstractly, a bit is just a variable that's either 0 or I.
$\mathrm{Q}: \mathrm{X}$ is a bit. How many states can it be in?

## What is a bit?

- Anything that can be in one of two states!

Might as well call these two states 0 and I Abstractly, a bit is just a variable that's either 0 or I.
$\mathrm{Q}: \mathrm{X}$ is a bit. How many different states could it be in?
A: two---either 0 or I

## Concept Question:Three Bits

- $X_{1}$ is a bit.
- $X_{2}$ is a bit.
- $X_{3}$ is a bit.
- Q: How many possible values are there for the bit string $X_{1} X_{2} X_{3}$ ?
A) 1
B) 3
C) 8
D) $\infty$


## Concept Question:Three Bits

- $X_{1}$ is a bit.
- $X_{2}$ is a bit.
- $X_{3}$ is a bit.
- Q: How many possible values are there for the bit string $X_{1} X_{2} X_{3}$ ?
A) 1
B) 3
C) 8
D) $\infty$


## Concept Question:Three Bits

Q: How many possible values are there for the bit string $X_{1} X_{2} X_{3}$ ?
A) 1
B) 3
C) 8
D) $\infty$

- Here are the possible states: 000, 00I, 010,01I, 100, IOI, IIO, III


## Representing bit-strings as vectors

- One bit: 0 or I

$$
|0\rangle \text { or }|1\rangle
$$

$$
\text { vectors: }|0\rangle=\left[\begin{array}{l}
1 \\
0
\end{array}\right] \text { or }|0\rangle=\left[\begin{array}{l}
0 \\
1
\end{array}\right]
$$

- Two Bits:00,01, IO, II

$$
|00\rangle=\left[\begin{array}{l}
1 \\
0 \\
0 \\
0
\end{array}\right],|01\rangle=\left[\begin{array}{l}
0 \\
1 \\
0 \\
0
\end{array}\right],|10\rangle=\left[\begin{array}{l}
0 \\
0 \\
1 \\
0
\end{array}\right],|11\rangle=\left[\begin{array}{l}
0 \\
0 \\
0 \\
1
\end{array}\right]
$$

## Tensor Products

- $\left[\begin{array}{l}x_{0} \\ x_{1}\end{array}\right] \otimes\left[\begin{array}{l}y_{0} \\ y_{1}\end{array}\right] \otimes\left[\begin{array}{l}z_{0} \\ z_{1}\end{array}\right]=\left[\begin{array}{l}x_{0} y_{0} z_{0} \\ x_{0} y_{0} z_{1} \\ x_{0} y_{1} z_{0} \\ x_{0} y_{1} z_{1} \\ x_{1} y_{0} z_{0} \\ x_{1} y_{0} z_{1} \\ x_{1} y_{1} z_{0} \\ x_{1} y_{1} z_{1}\end{array}\right]$

Entries are 0's and I's
Exactly one I in each vector on LHS means exactly one I in big vector on RHS

## Manipulating Bits

One bit operation: NOT
$\operatorname{NOT}(x)=1$ if $x=0$

$$
0 \text { if } x=1
$$

NOT(x) just flips the bit x .

More compactly: $\operatorname{NOT}(x)=\bar{x}$

## Manipulating Bits

One bit operation: NOT
$\operatorname{NOT}(x)=1$ if $x=0$

$$
0 \text { if } x=1
$$

NOT(x) just flips the bit x .

More compactly: $\operatorname{NOT}(x)=\bar{x}$

## Manipulating Bits

- When represented as a vector
- $x \sim\left[\begin{array}{l}1 \\ 0\end{array}\right]$ or $\left[\begin{array}{l}0 \\ 1\end{array}\right]$
- $x \sim\left[\begin{array}{l}x_{0} \\ x_{1}\end{array}\right]$
- $\bar{x} \sim\left[\begin{array}{ll}0 & 1 \\ 1 & 0\end{array}\right]\left[\begin{array}{l}x_{0} \\ x_{1}\end{array}\right]=\left[\begin{array}{l}x_{1} \\ x_{0}\end{array}\right]$
- Call $X=\left[\begin{array}{ll}0 & 1 \\ 1 & 0\end{array}\right]$
- As Kets: $|\bar{x}\rangle=X|x\rangle$


## Flipping a bit: circuit diagram



## Manipulating one bit

- If someone hands you a bit, there are two ways you can process it to give another bit:

1) Leave it alone
2) Flip it

That's it. If we want more interesting computations, we'd better have more bits.

## Swapping Two bits

- Given two bits, what can we do? Swap them!



## Swapping Two bits

- Given two bits, what can we do? Swap them!



## Swapping Two bits

- Given two bits, what can we do? Swap them!

$$
S_{01}|x\rangle|y\rangle=|y\rangle|x\rangle
$$

As a matrix

$$
S_{01}=\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## Controlled NOT

CNOT: $|x\rangle|y\rangle \rightarrow|x\rangle|x \oplus y\rangle$
where $x \bigoplus y=(x+y) \bmod 2$

If $x=0$, leaves $y$ alone. If $x=I$, flips $y$ bit.


## Concept Test

CNOT: $|x\rangle|y\rangle \rightarrow|x\rangle|x \oplus y\rangle$
What matrix represents CNOT?
A) $\left[\begin{array}{llll}1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1\end{array}\right]$
В) $\left[\begin{array}{llll}1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1\end{array}\right]$
C) $\quad\left[\begin{array}{llll}1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0\end{array}\right]$
D) $\left[\begin{array}{llll}0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0\end{array}\right]$

## Concept Test

CNOT: $|x\rangle|y\rangle \rightarrow|x\rangle|x \oplus y\rangle$
What matrix represents CNOT?
A) $\left[\begin{array}{llll}1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1\end{array}\right]$
В) $\left[\begin{array}{llll}1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1\end{array}\right]$
C) $\quad\left[\begin{array}{llll}1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0\end{array}\right]$
D) $\left[\begin{array}{llll}0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0\end{array}\right]$

## Concept Test: solution

$\cdot\left[\begin{array}{l}00 \\ 01 \\ 10 \\ 11\end{array}\right.$ CNOT swaps 10 and II
$00 \rightarrow 00,0 \mathrm{O} \rightarrow 0 \mathrm{I}, \mathrm{IO} \rightarrow \mathrm{II}, \mathrm{II} \rightarrow \mathrm{IO}$
The matrix that does this is

$$
\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1 \\
0 & 0 & 1 & 0
\end{array}\right]
$$



