Artificial Neurons

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University of Colorado Boulder Fall 2022



Review

- Last lecture:
 - Deep learning applications
 - History of neural networks and deep learning
 - How does a machine learn?
 - Course logistics
- Assignments (Canvas):
 - Problem set 1 due next week
- Questions?

Today's Topics

Binary classification applications

Evaluating classification models

• Biological neurons: inspiration

Artificial neuron: Perceptron

Today's Topics

Binary classification applications

Evaluating classification models

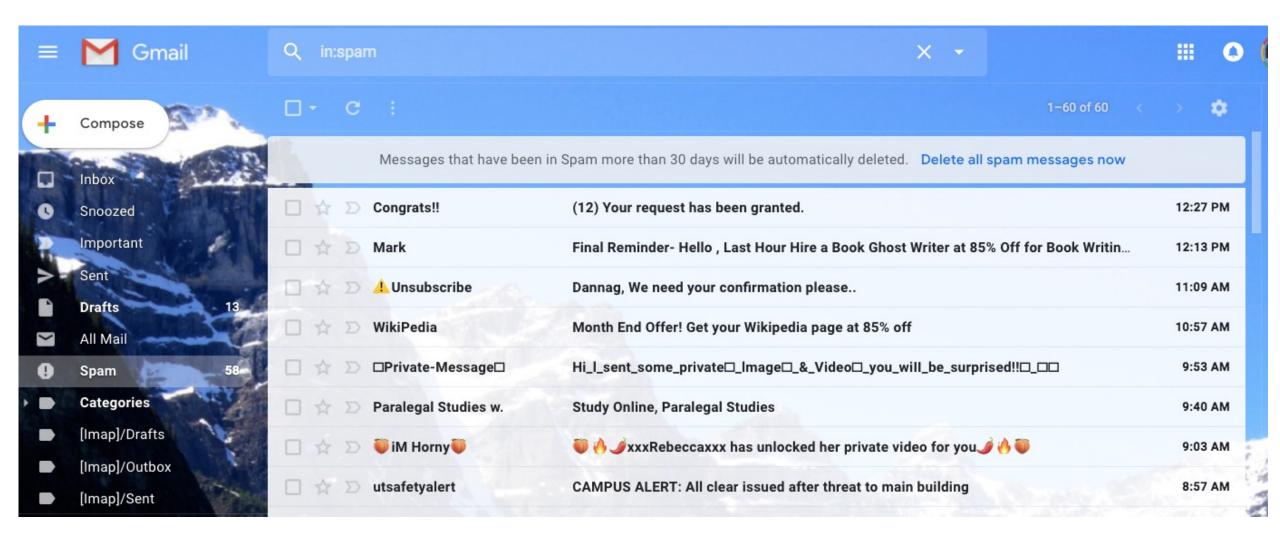
• Biological neurons: inspiration

Artificial neuron: Perceptron

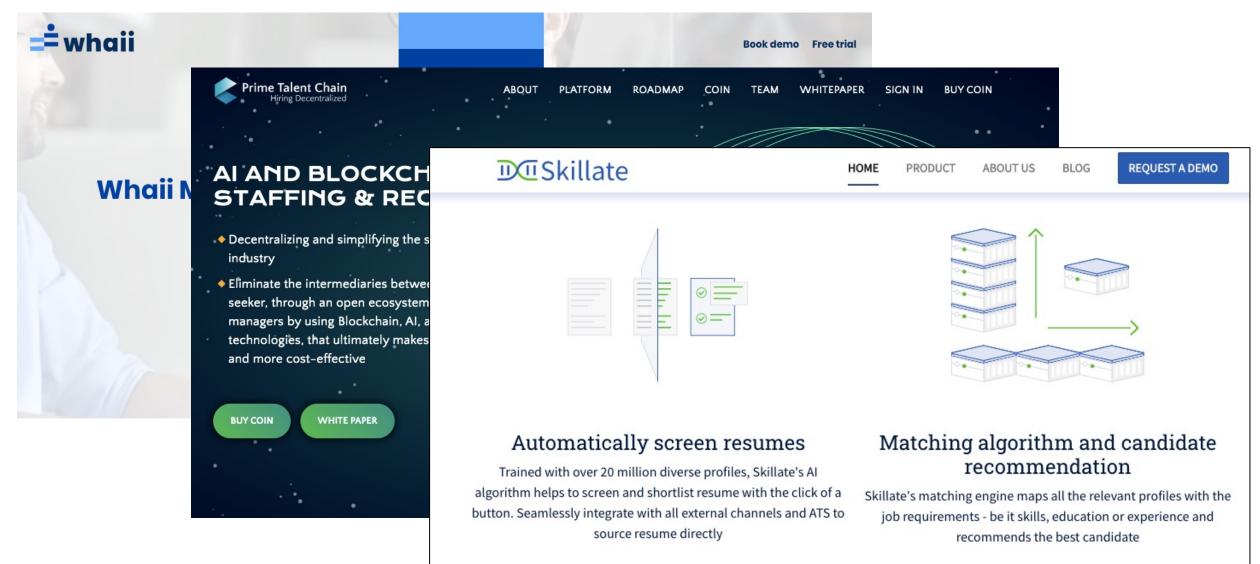
Today's Scope: Binary Classification

Distinguish 2 classes

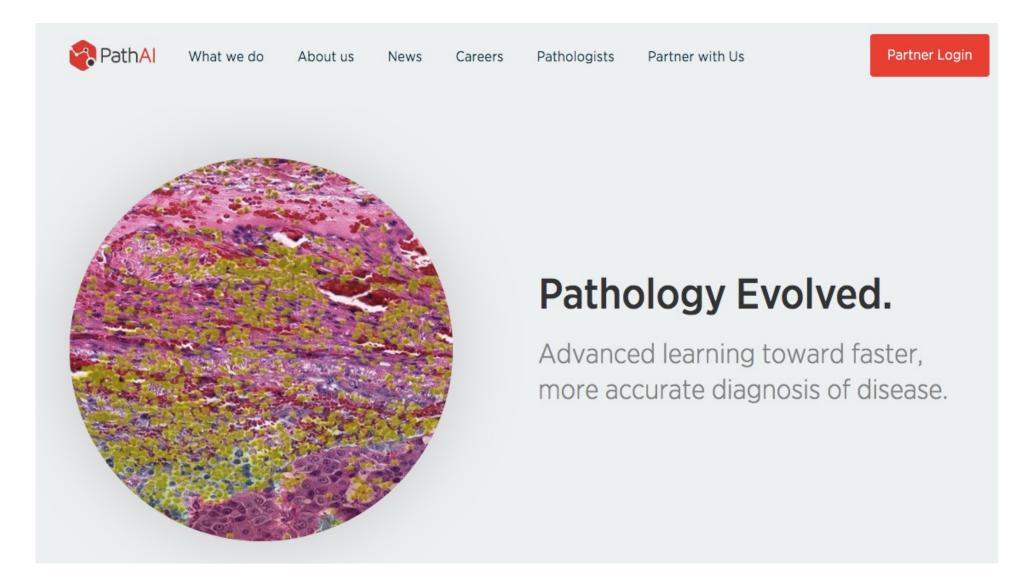
Binary Classification: Spam Detection



Binary Classification: Resume Pre-Screening



Binary Classification: Cancer Diagnosis



Binary Classification: Cognitive Impairment Recognition by Apple App Usage



Image Credit: https://www.techradar.com/news/the-10-best-phones-for-seniors https://www.technologyreview.com/f/615032/the-apps-you-use-on-your-phone-could-help-diagnose-your-cognitive-health/?utm_medium=tr_social&utm_campaign=site_visitor.unpaid.engagement&utm_source=Twitter#Echobox=1579899156

Binary Classification: Sentiment Analysis



Search movies, TV, actors, more...

Q

MOVIES

TV SHOWS

What's the Tomatometer®?

RT PODCAST

NEWS

SIGN UP

Critics

SHOWTIMES

LOG IN

CRITIC REVIEWS FOR *MULAN*

Its cast, its attitude, its overall eagerness to please -- all benefits, one would think -- don't add up to a good movie. They add up to a blueprint of the movie this ought to be.

October 23, 2020 | Rating: 2.5/5 | Full Review...



While glorious to look at, the movie still feels slightly hollow. All the right pieces are there, but an emotional connection to the characters is lacking.

September 10, 2020 | Rating: 6.8/10 | Full Review...



K. Austin Collins

Rolling Stone





Amy Amatangelo

Paste Magazine

★ TOP CRITIC

Binary Classification: Food Quality Control



Machine Learning: Using Algorithms to Sort Fruit

Demo: https://www.youtube.com/watch?v=Bl3XzBWpZbY

Can you think of other binary classification applications?

Today's Topics

Binary classification applications

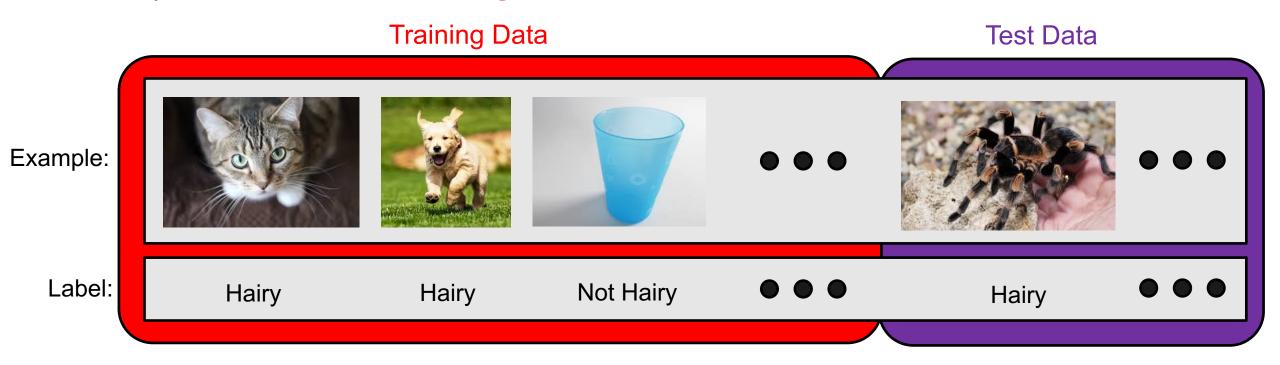
Evaluating classification models

• Biological neurons: inspiration

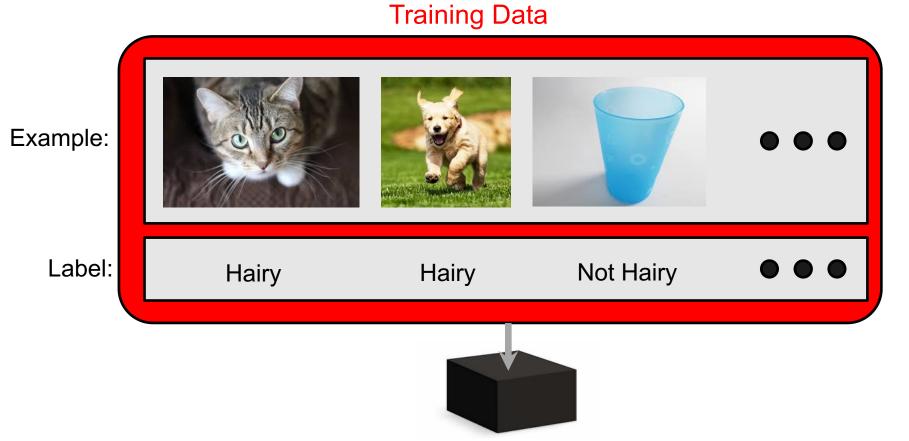
Artificial neuron: Perceptron



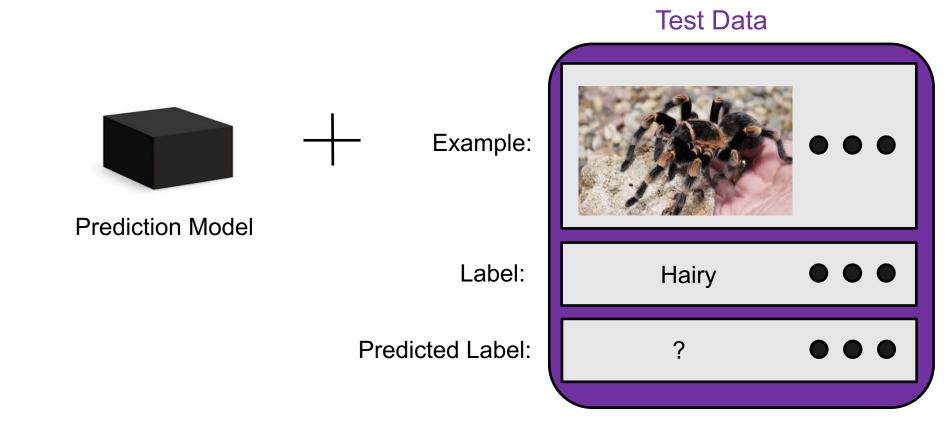
1. Split data into a "training set" and "test set"



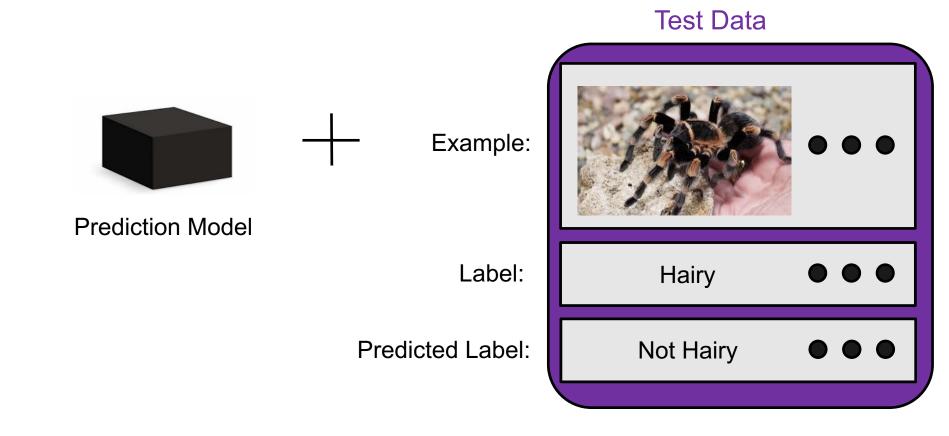
2. Train model on "training set" to try to minimize prediction error on it



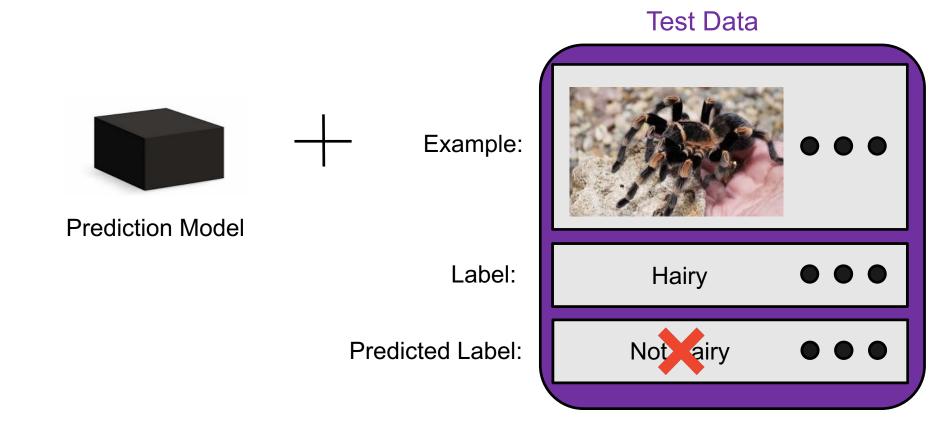
3. Apply trained model on "test set" to measure generalization error



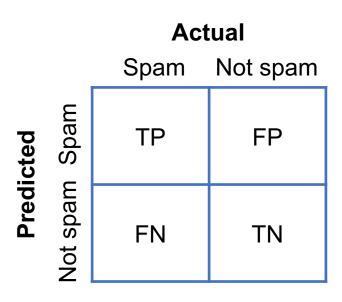
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3. Apply trained model on "test set" to measure generalization error



Evaluation Methods: Confusion Matrix



TP = true positive

TN = true negative

FP = false positive

FN = false negative

Evaluation Methods: Descriptive Statistics

e.g.,

Actual Spam Not spam Spam 20 Spam 30 Spam 10 Spam 10 Spam 30 Spam 30

Commonly-used statistical descriptions:

- How many actual spam results are there? 65
- How many actual trusted results are there? 110
- How many *correctly classified instances*? 150/175 ~ 86%
- How many *incorrectly classified instances*? 25/175 ~ 14%

• What is the *recall*?
$$\frac{TP}{TP + FN}$$

Group Discussion

- Which of these evaluation metrics would you use versus not use and why?
 - Accuracy (percentage of correctly classified examples)
 - Precision
 - Recall
- Scenario 1: Medical test for a rare disease affecting one in every million people.
- Scenario 2: Deciding which emails to flag as spam.

Today's Topics

Binary classification applications

Evaluating classification models

• Biological neurons: inspiration

Artificial neuron: Perceptron

Inspiration: Animal's Computing Machinery

Neuron

 basic unit in the nervous system for receiving, processing, and transmitting information; e.g., messages such as...

"hot"



https://www.clipart.email/clipart/don t-touch-hot-stove-clipart-73647.html

"loud"



https://kisselpaso.com/if-the-sun-city-music-fest-gets-too-loud-there-is-a-phone-number-you-can-call-to-complain/

"spicy"



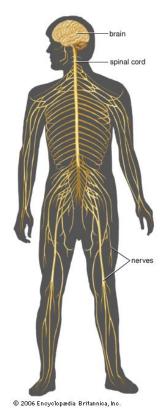
https://www.babycenter.com/404_when-can-my-baby-eat-spicy-foods_1368539.bc

Inspiration: Animal's Computing Machinery



https://en.wikipedia.org/wiki/Nematode#/media/File:CelegansGoldsteinLabUNC.jpg

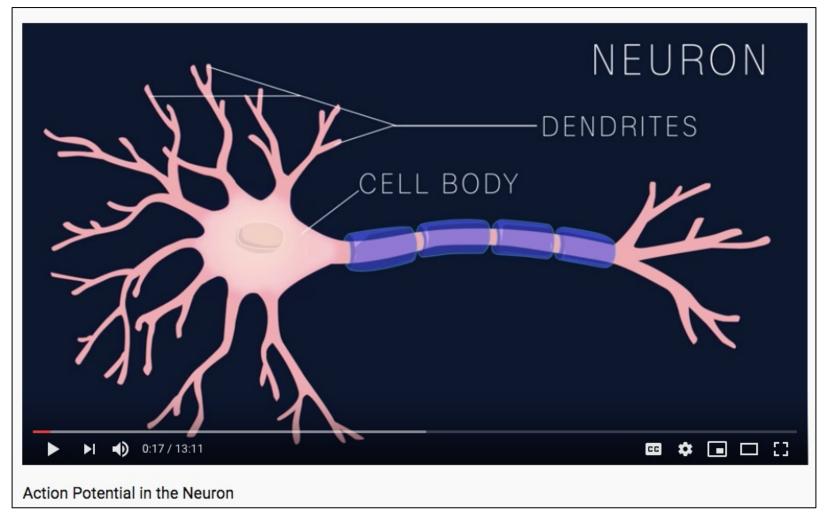
Nematode worm: 302 neurons



https://www.britannica.com/sci ence/human-nervous-system

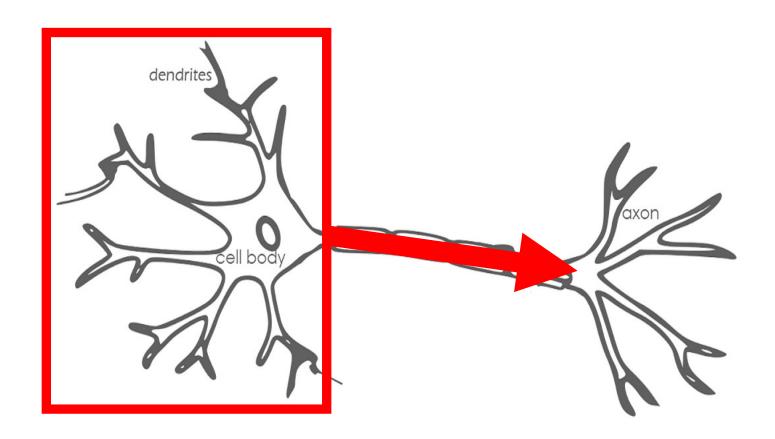
Human: ~100,000,000,000 neurons

Inspiration: Animal's Computing Machinery



Demo (0-1:14): https://www.youtube.com/watch?v=oa6rvUJlg7o

Inspiration: Basic Understanding of Neurons



- When the input signals exceed a certain threshold within a short period of time, a neuron "fires"
- Neuron "firing" is an "all-or-none" process, where either a signal is sent or nothing happens

Image Source: https://becominghuman.ai/introduction-to-neural-networks-bd042ebf2653

Sidenote: It Remains An Open Research Problem to Understand How Individual Neurons Work

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• Biological neurons: inspiration

• Artificial neuron: Perceptron

Historical Context: Artificial Neurons

First mathematical model of neuron

1943 1945 1950



First programmable machine

Turing test

Perceptron Machine



Warren McCulloch (Neurophysiologist)

http://web.csulb.edu/~cwallis/ar tificialn/warren_mcculloch.html

Emerges from interdisciplinary collaboration



Walter Pitts
(Mathematician)

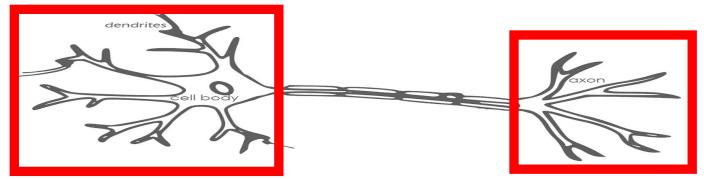
https://en.wikipedia.o rg/wiki/Walter_Pitts

"Input signals" "Output signal"

Artificial Neuron:

 X_1 W_1 X_2 W_2 X_3 X_4 X_4 X_5 X_6 X_7 X_8 X_8

Biological Neuron:

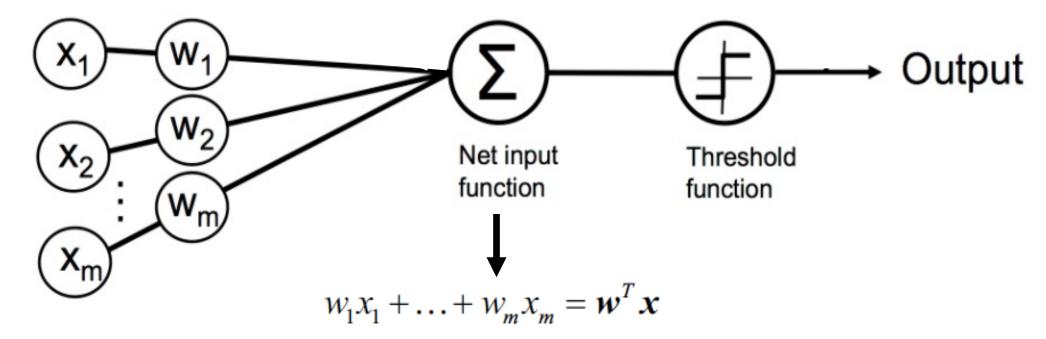


Python Machine Learning; Raschka & Mirjalili

Image Source: https://becominghuman.ai/introduction-to-neural-networks-bd042ebf2653

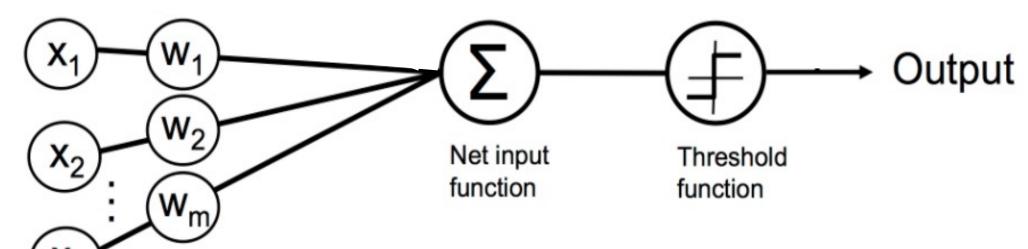
- inputs (x) and weights (w) can be 0 or 1
- weights (w) and threshold values are fixed

 outputs 1 or 0 (mimics neurons by "firing" only when aggregate value exceeds threshold)



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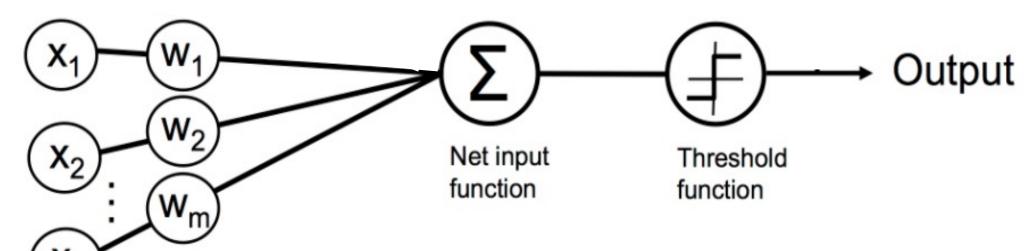
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This neuron representation supports propositional logic; e.g., if weights equal 1 and there are 3 inputs, how is the AND function achieved?

- inputs (x) and weights (w) can be 0 or 1
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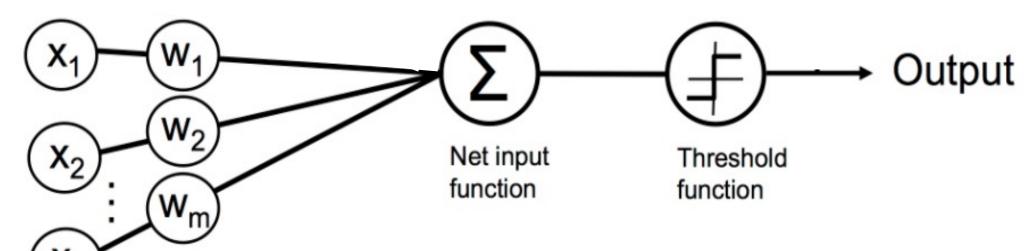
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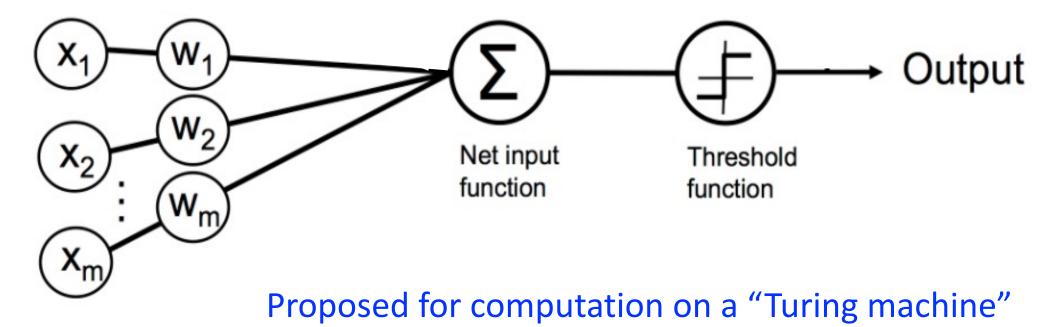
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This neuron representation supports propositional logic; more examples found at https://home.csulb.edu/~cwallis/artificialn/History.htm

- inputs (x) and weights (w) can be 0 or 1
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Historical Context: Artificial Neurons

First mathematical model of neuron

1943 1945 1950



First programmable machine

erceptron Machine

Turing test

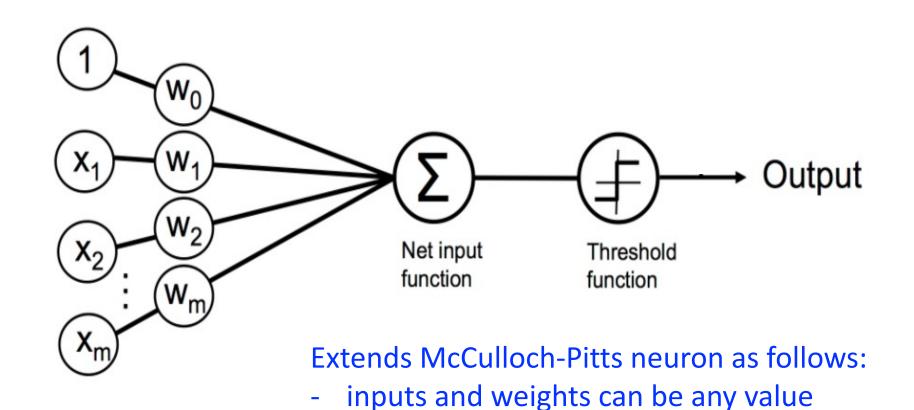
Perceptron: Innovator and Vision



Frank Rosenblatt (Psychologist)

"[The perceptron is] the embryo of an electronic computer that [the Navy] expects will be able to walk, talk, see, write, reproduce itself and be conscious of its existence.... [It] is expected to be finished in about a year at a cost of \$100,000."

1958 New York Times article: https://www.nytimes.com/1958/07/08/archives/new-navy-device-learns-by-doing-psychologist-shows-embryo-of.html



weights (W) are learned

• Function deciding output value ("fire" or not):

$$\phi(z) = \begin{cases} 1 & \text{if } z \ge \theta \\ -1 & \text{otherwise} \end{cases}$$

• Rewriting function:

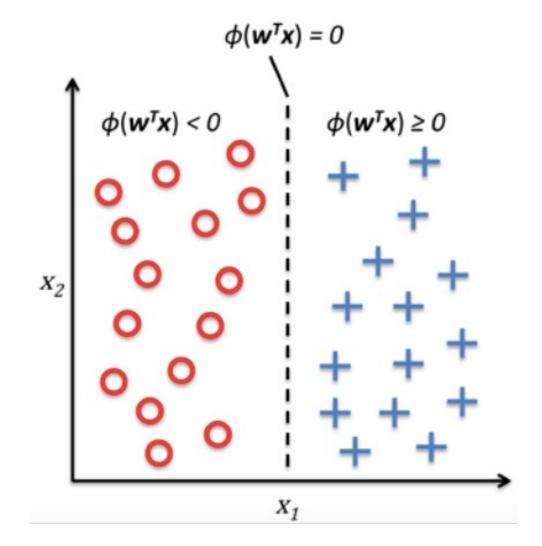
$$\phi(z) = \begin{cases} 1 & \text{if } z \ge 0 \\ -1 & \text{otherwise} \end{cases}$$

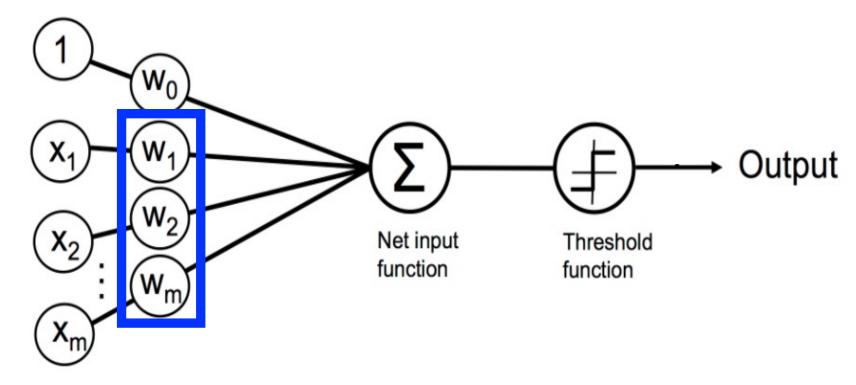
• Where:

$$z = w_0 x_0 + w_1 x_1 + \ldots + w_m x_m = w^T x$$
Bias $-\theta$ 1

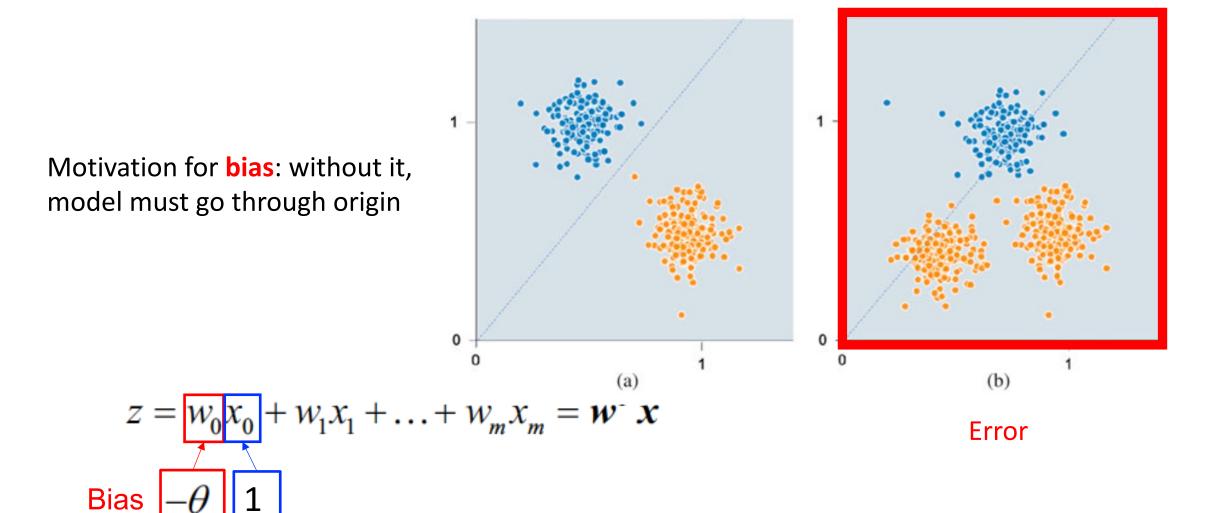
* Note: Kamath textbook offers two common conventions for Perceptrons of using two possible output values of {-1, 1} and {0, 1}, in Chapters 2.5 and 4. The output choice dictates whether the threshold should be set to 0.5 or 0.

Graphical representation:



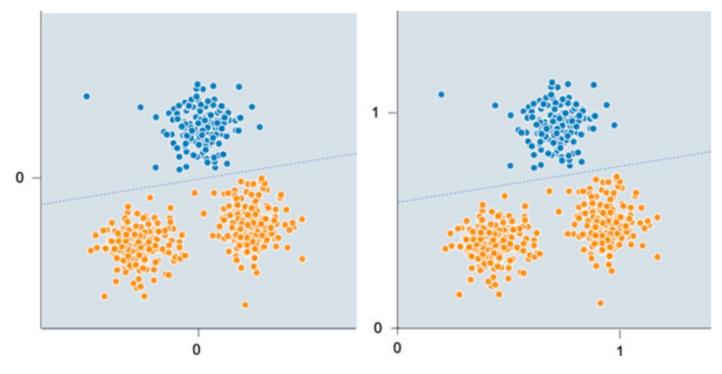


What is the motivation for weights? e.g., for predicting if you will like a movie?



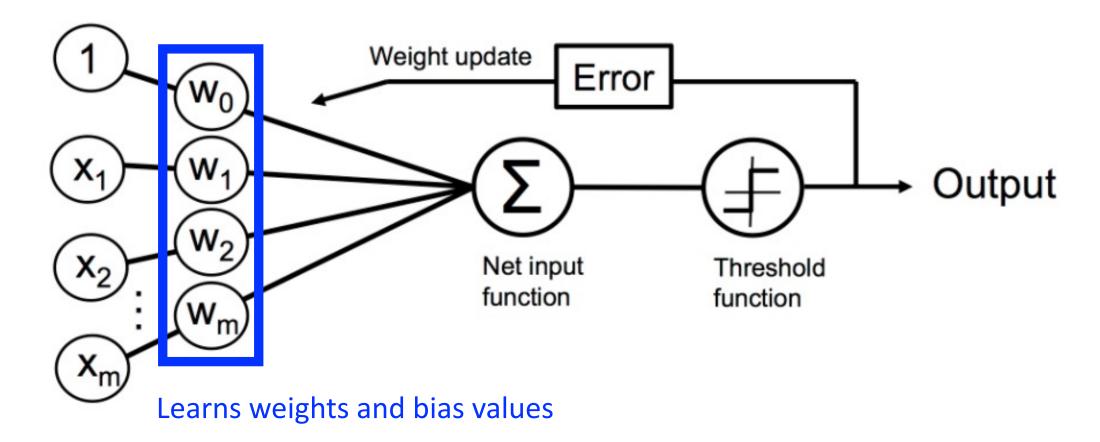
Uday Kamath, John Liu, and James Whitaker. Deep Learning for NLP and Speech Recognition. 2019.

Motivation for bias: with it, model does not have to go through origin

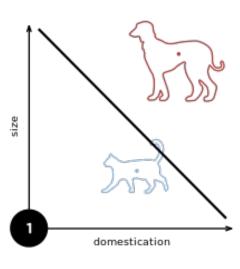


$$z = w_0 x_0 + w_1 x_1 + \ldots + w_m x_m = w^T x$$
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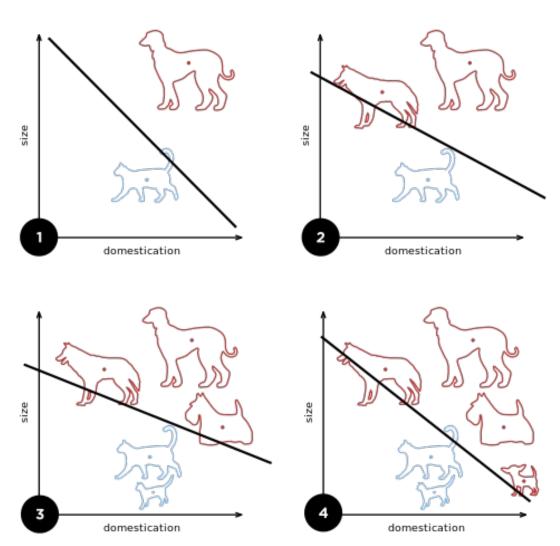
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Process: iteratively update boundary with observation of each additional example:

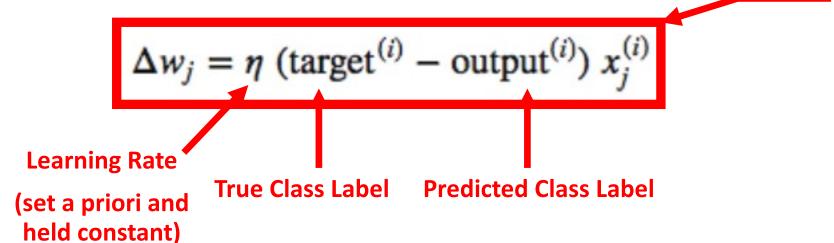


Process: iteratively update boundary with observation of each additional example:



https://en.wikipedia.org/wiki/Perceptron

- 1. Initialize weights/bias to 0 or small random numbers
- 2. For each training sample (i.e., i):
 - 1. Compute predicted value (i.e., {-1, 1}): $\sum_{j=0}^{m} x_j w_j = w^T x$
 - 2. Update parameters based on prediction success: $w_j := w_j + \Delta w_j$



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$$\Delta w_j = \eta \text{ (target}^{(i)} - \text{output}^{(i)}) x_j^{(i)}$$

What happens to the weights when the model predicts the **correct** class label?

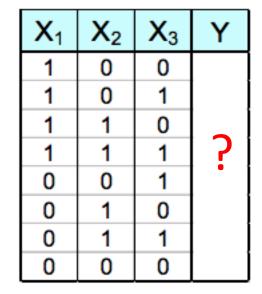
- no weight update since result is 0

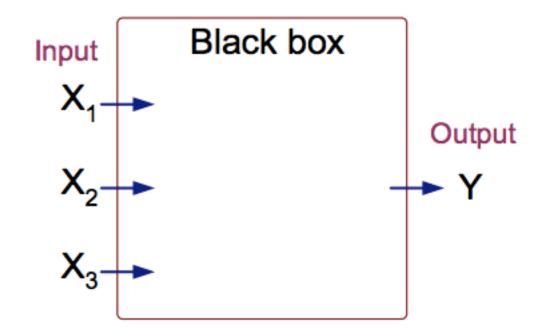
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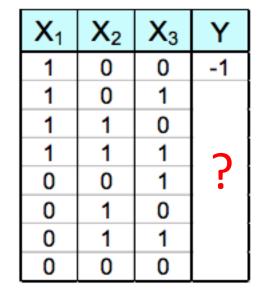
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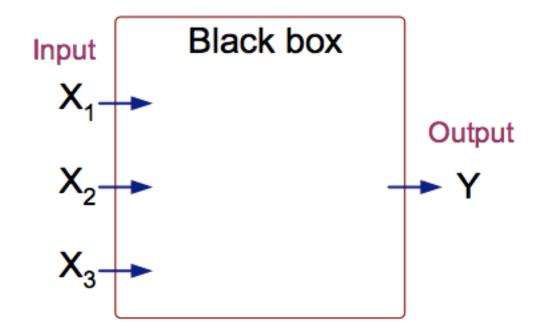
What happens to the weights when the model predicts the **wrong** class label?

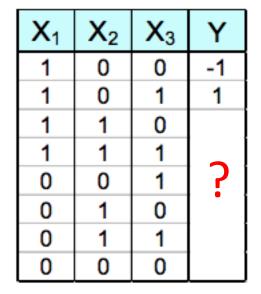
- weights change since result is "2" or "-2"

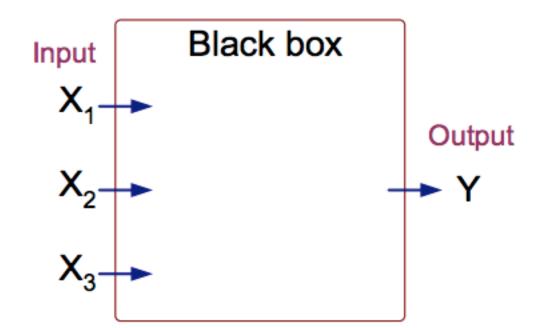




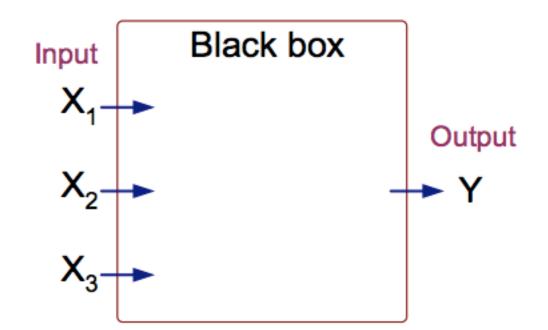






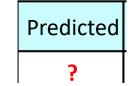


X ₁	X_2	X ₃	Υ
1	0	0	-1
1	0	1	1
1	1	0	1
1	1	1	1
0	0	1	-1
0	1	0	-1
0	1	1	1
0	0	0	-1



• Compute predicted value: $\sum_{j=0}^{m} x_j w_j = w^T x$; $\phi(w^T x) = \begin{cases} 1 \text{ if } \phi(w^T x) \ge 0 \\ -1 \text{ otherwise} \end{cases}$

X ₁	X_2	X_3	Υ
1	0	0	-1



w ₀	W ₁	W ₂	W ₃
0	0	0	0

• Update params: $w_j = w_j + \eta$ (target⁽ⁱ⁾ – output⁽ⁱ⁾) $x_i^{(i)}$; learning rate = 0.1

X_1	X_2	X_3	Υ
1	0	0	-1

Predicted	
1	Ī

W 0	W ₁	W ₂	W ₃
0	0	0	0
?	?	?	?

$$\Delta w_0 = \eta \text{ (target}^{(i)} - \text{output}^{(i)})$$

$$\Delta w_0 = \eta \text{ (target}^{(i)} - \text{output}^{(i)})$$

$$\Delta w_1 = \eta \text{ (target}^{(i)} - \text{output}^{(i)}) x_1^{(i)}$$

$$\Delta w_2 = \eta \text{ (target}^{(i)} - \text{output}^{(i)}) x_2^{(i)}$$

$$\Delta w_3 = \eta \text{ (target}^{(i)} - \text{output}^{(i)}) x_3^{(i)}$$

• Update params: $w_j = w_j + \eta$ (target⁽ⁱ⁾ – output⁽ⁱ⁾) $x_i^{(i)}$; learning rate = 0.1

X ₁	X_2	X_3	Υ
1	0	0	-1

Predicted	
1	T

W ₀	W ₁	W ₂	W ₃
0	0	0	0
?	?	?_	_ ?_

$$\Delta w_0 = 0.1(-1-1)*1 = -0.2$$

$$\Delta w_1 = 0.1(-1-1)*1 = -0.2$$

$$\Delta w_2 = 0.1(-1-1)*0 = 0$$

$$\Delta w_3 = 0.1(-1-1)*0 = 0$$

$$\Delta w_1 = 0.1(-1-1)*1 = -0.2$$

$$\Delta w_2 = 0.1(-1-1)*0 = 0$$

$$\Delta w_3 = 0.1(-1-1)*0 = 0$$

Updates make weights more negative so that the model is more likely to classify the sample as -1 next time

• Compute output value: $\sum_{j=0}^{m} x_j w_j = w^T x$; $\phi(w^T x) = \begin{cases} 1 \text{ if } \phi(w^T x) \ge 0 \\ -1 \text{ otherwise} \end{cases}$

X ₁	X ₂	X ₃	Υ
1	0	0	-1
1	0	1	1

(3	Υ		Predicted	\mathbf{w}_0	W ₁	W ₂	W 3
0	-1		1	0	0	0	0
1	1		?	-0.2	-0.2	0	0
' '	•	ı	•				

• Update params: $w_j = w_j + \eta$ (target⁽ⁱ⁾ – output⁽ⁱ⁾) $x_i^{(i)}$; learning rate = 0.1

X ₁	X ₂	X ₃	Υ
1	0	0	-1
1	0	1	1

Predicted	
1	
-1	

w ₀	W 1	W ₂	W ₃
0	0	0	0
-0.2	-0.2	0	0
?	?	?	?

$$\Delta w_0 = \eta \text{ (target}^{(i)} - \text{output}^{(i)})$$

$$\Delta w_1 = \eta \text{ (target}^{(i)} - \text{output}^{(i)}) x_1^{(i)}$$

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$$\Delta w_3 = \eta \text{ (target}^{(i)} - \text{output}^{(i)}) x_3^{(i)}$$

• Update params: $w_j = w_j + \eta$ (target⁽ⁱ⁾ – output⁽ⁱ⁾) $x_i^{(i)}$; learning rate = 0.1

X ₁	X_2	X ₃	Υ
1	0	0	-1
1	0	1	1

Predicted	
1	
-1	

W 0	W 1	W ₂	W 3
0	0	0	0
-0.2	-0.2	0	0
?	?	?	?

$$\Delta w_0 = 0.1(1--1)*1 = 0.2$$

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$$\Delta w_3 = 0.1(1--1)*1 = 0.2$$

Updates make weights more positive so that the model is more likely to classify the sample as 1 next time

• Update params: $w_j = w_j + \eta$ (target⁽ⁱ⁾ – output⁽ⁱ⁾) $x_i^{(i)}$; learning rate = 0.1

X ₁	X ₂	X ₃	Υ
1	0	0	-1
1	0	1	1

Predicted	
1	
-1	

w ₀	W ₁	W ₂	W 3
0	0	0	0
-0.2	-0.2	0	0
0	0	0	0.2

$$\Delta w_0 = 0.1(1--1)*1 = 0.2$$

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$$\Delta w_1 = 0.1(1--1)*1 = 0.2$$

$$\Delta w_2 = 0.1(1--1)*0 = 0$$

$$\Delta w_3 = 0.1(1--1)*1 = 0.2$$

$$\Delta w_2 = 0.1(1--1)*0 = 0$$

$$\Delta w_3 = 0.1(1--1)*1 = 0.2$$

What is the influence of the learning rate? i.e., what would happen if the value was larger/smaller?

Perceptron: Example – One Epoch (Training with All Samples)

•
$$w_j = w_j + \eta$$
 (target⁽ⁱ⁾ – output⁽ⁱ⁾) $x_j^{(i)}$; learning rate = 0.1

X_1	X_2	X_3	Υ
1	0	0	-1
1	0	1	1
1	1	0	1
1	1	1	1
0	0	1	-1
0	1	0	-1
0	1	1	1
0	0	0	-1

	\mathbf{w}_0	W ₁	W ₂	W ₃
0	0	0	0	0
1	-0.2	-0.2	0	0
2	0	0	0	0.2
3	0	0	0	0.2
4	0	0	0	0.2
5	-0.2	0	0	0
6	-0.2	0	0	0
7	0	0	0.2	0.2
8	-0.2	0	0.2	0.2

Perceptron: Example – Six Epochs

• $w_j = w_j + \eta$ (target⁽ⁱ⁾ – output⁽ⁱ⁾) $x_j^{(i)}$; learning rate = 0.1

X ₁	X ₂	X ₃	Υ
1	0	0	-1
1	0	1	1
1	1	0	1
1	1	1	1
0	0	1	-1
0	1	0	-1
0	1	1	1
0	0	0	-1

Epoch	W ₀	\mathbf{W}_1	W_2	w_3
0	0	0	0	0

Perceptron: Example – Six Epochs

• $w_j = w_j + \eta$ (target⁽ⁱ⁾ – output⁽ⁱ⁾) $x_j^{(i)}$; learning rate = 0.1

X_1	X_2	X_3	Υ
1	0	0	-1
1	0	1	1
1	1	0	1
1	1	1	1
0	0	1	-1
0	1	0	-1
0	1	1	1
0	0	0	-1

	W ₀	W ₁	W ₂	W ₃
0	0	0	0	0
1	-0.2	-0.2	0	0
2	0	0	0	0.2
3	0	0	0	0.2
4	0	0	0	0.2
5	-0.2	0	0	0
6	-0.2	0	0	0
7	0	0	0.2	0.2
8	-0.2	0	0.2	0.2

Epoch	\mathbf{w}_0	\mathbf{W}_1	W_2	W ₃
0	0	0	0	0
1	-0.2	0	0.2	0.2
2	-0.2	0	0.4	0.2
3	-0.4	0	0.4	0.2
4	-0.4	0.2	0.4	0.4
5	-0.6	0.2	0.4	0.2
6	-0.6	0.4	0.4	0.2

Perceptron: Learning Algorithm Choices

- Learning rate
- Number of epochs (passes over the dataset)

Today's Topics

Binary classification applications

Evaluating classification models

• Biological neurons: inspiration

Artificial neuron: Perceptron

The End

Credits

- Image of Boulder: http://boulderrunning.com/where2run/five-trails-for-hill-running-and-mountain-training/
- Stick person figure: <u>https://drawception.com/game/AsPNcppPND/draw-yourself-blindfolded-pio/</u>
- Figure: https://www.quora.com/What-is-meant-by-gradient-descent-in-laymen-terms
- Figure and great reference:
 https://beamandrew.github.io/deeplearning/2017/02/23/deep_learning_101_part1.html