

Tokenization and Word Embeddings

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Spring 2025



<https://dannagurari.colorado.edu/course/neural-networks-and-deep-learning-spring-2025/>

Review

- Last week:
 - Machine learning for sequential data
 - Recurrent neural networks (RNNs)
 - Problem: learning challenges
 - Solution: Gated RNNs
 - Programming tutorial
- Assignments (Canvas):
 - Lab assignment 1 grades are out
 - Review session will be held at 4pm today on Zoom
 - Email all regrade requests to our TA, Nick Cooper (a comment in Canvas is not sufficient)
 - Problem set 3 due earlier today
 - Lab assignment 2 due in a 1.5 weeks
- Questions?

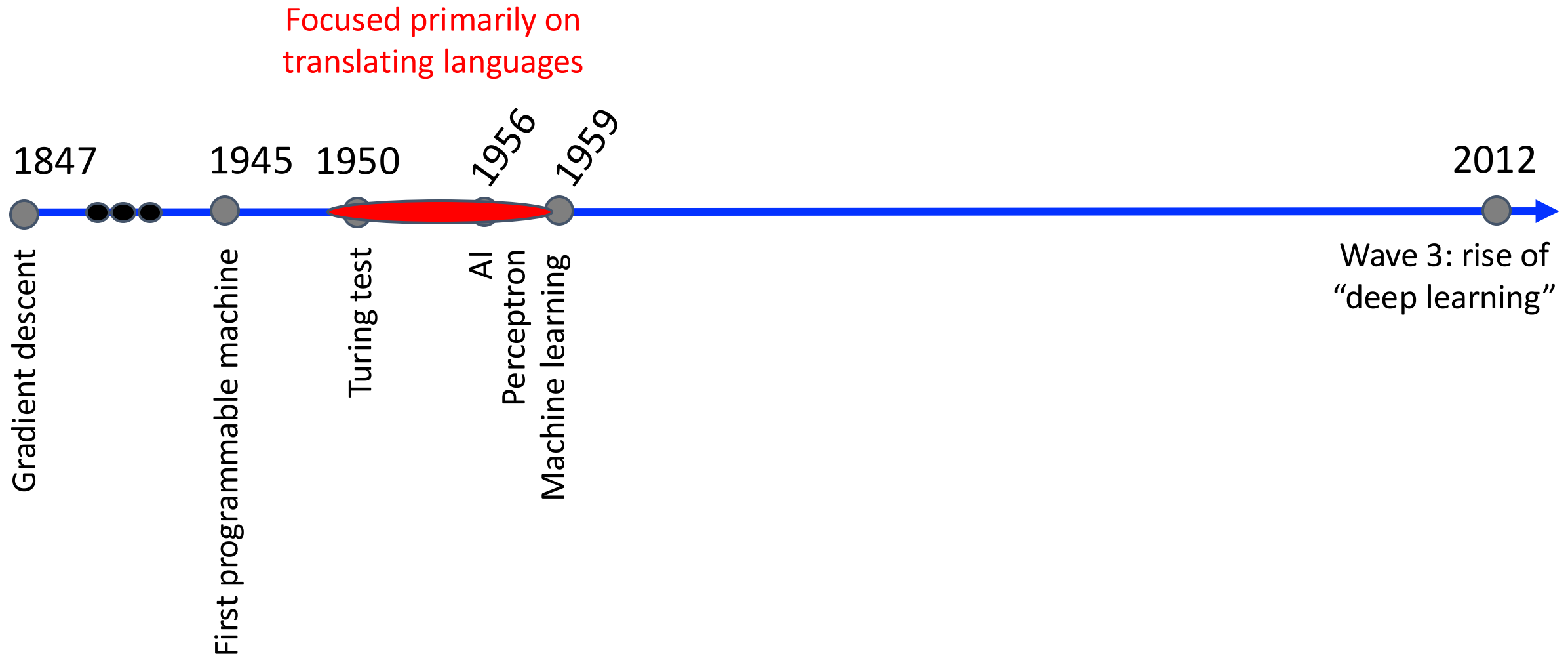
Today's Topics

- Motivation: numeric representation of natural language
- Tokenization: how to convert text into discrete units
- Neural word embeddings: how to create dense representation
- Programming tutorial

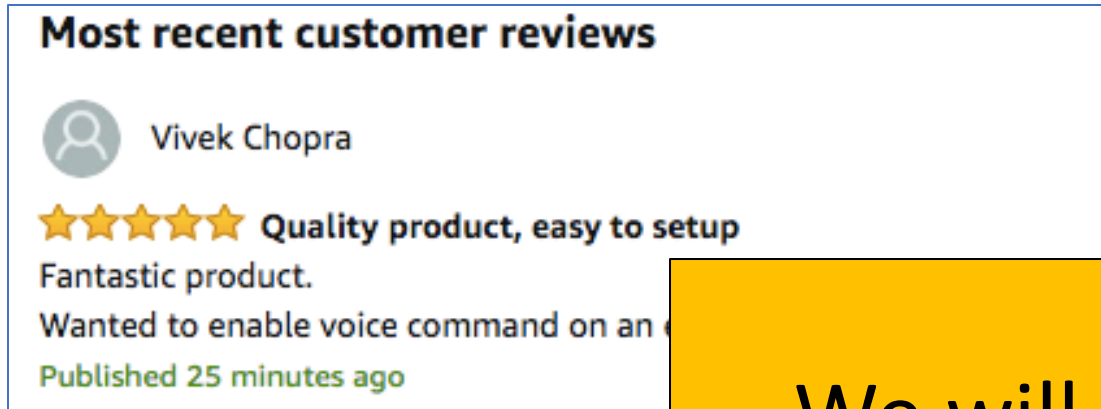
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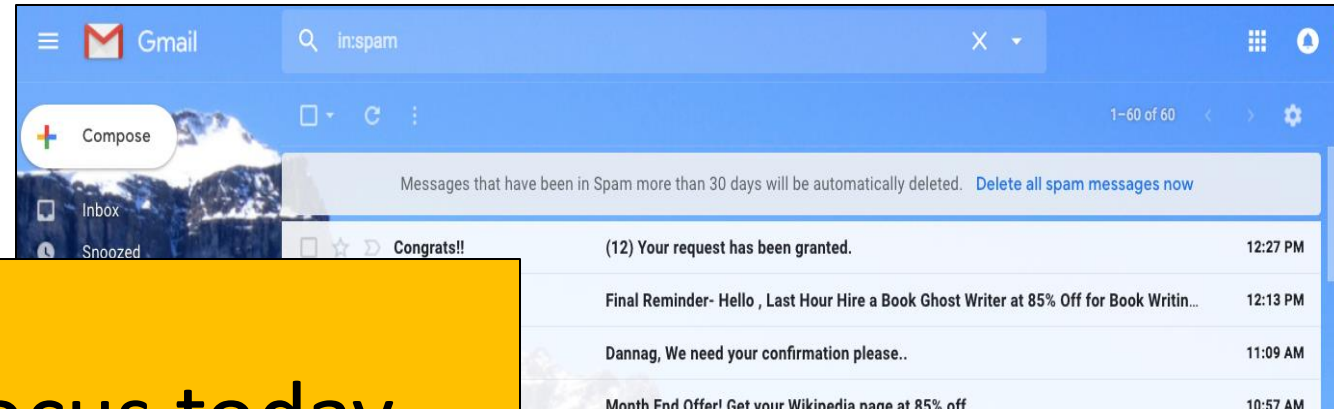
Origins of Natural Language Processing



Natural Language

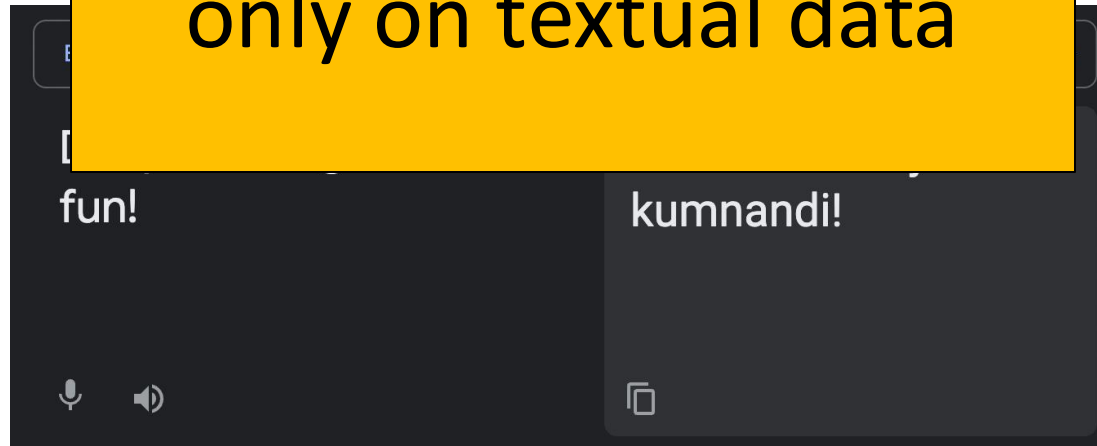


Opinion Mining



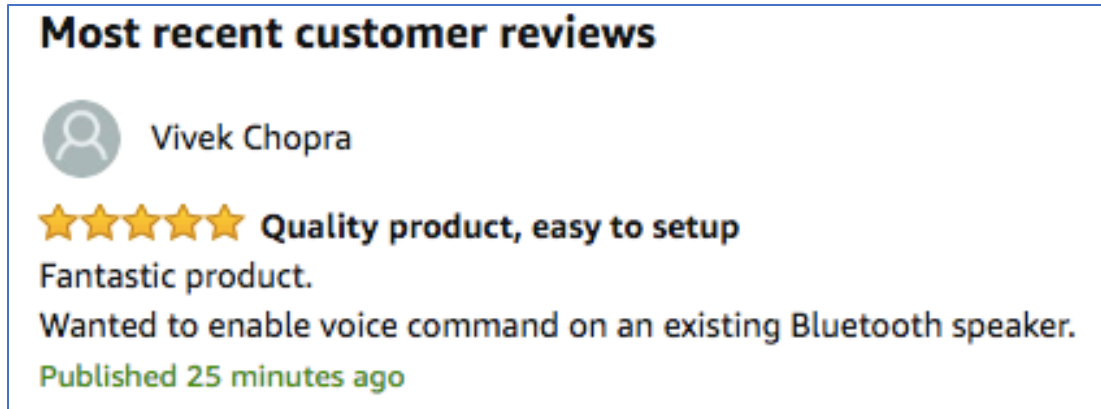
Spam Detection

We will focus today
only on textual data

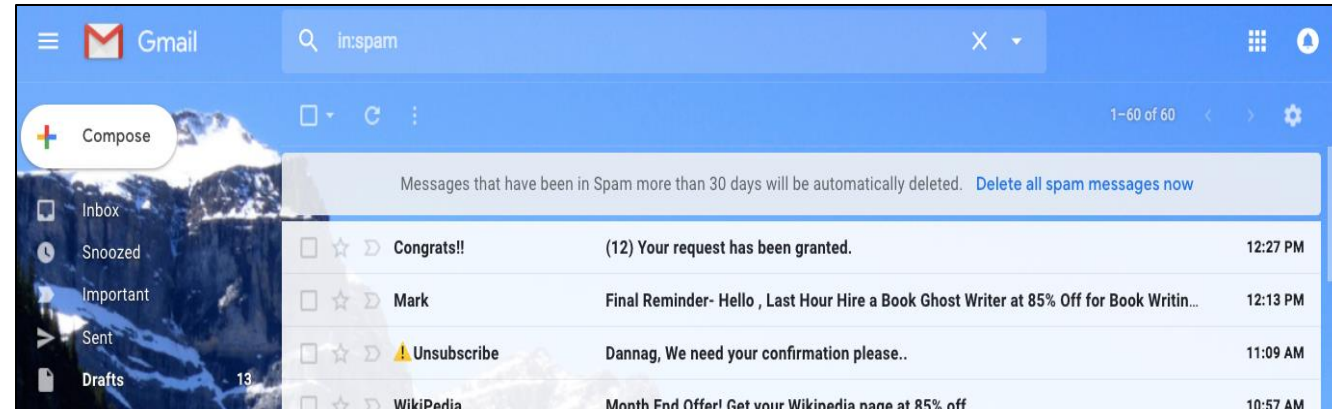


Language Translation

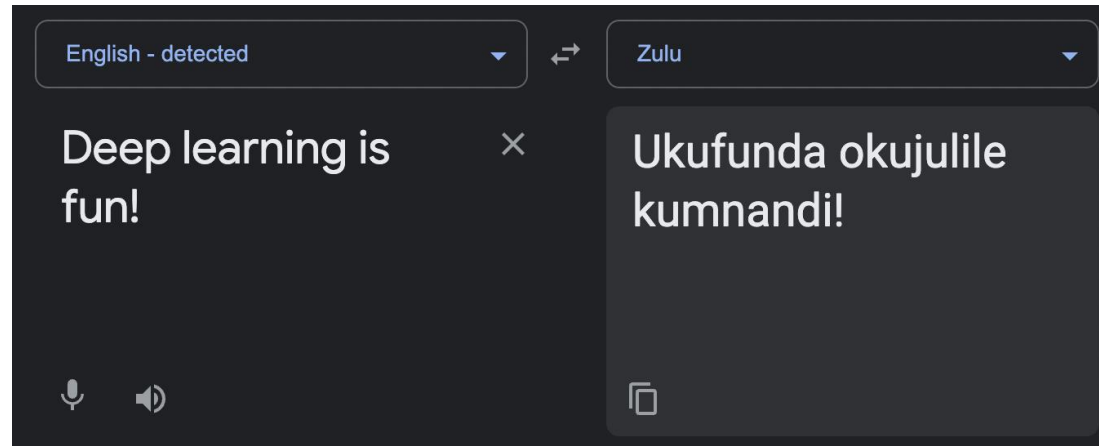
Input: String (Collection of Characters)



Opinion Mining



Spam Detection



Language Translation

Input: Which “String” Feature Types Apply?

- Categorical data
 - Comes from a fixed list (e.g., education level)
- Structured string data
 - e.g., addresses, dates, telephone numbers,

• Text data

How to Feed Computers Text in the Required Numeric Format? (Recall RNN Example)

1. **Tokenize** training data: “hello” -> “h”, “e”, “l”, “l”, “o”
2. **Learn vocabulary** by identifying all unique tokens: {h, e, l, o}
3. **Encode** data as vectors; e.g., one hot encoding

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1
h	e	l	l

Challenge: Represent 7000+ spoken languages including individual nuances in each language?



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Tokenizers: Converting Text to Numeric Value

"Machine",
"learning",
"is", "fun", "."

Word-Based

"ma",
"chine",
"learn", "ing"

Subword-Based

"M", "a", "c",
"h", "i", "n",
"e", "l", "e",
"a", "r", "n",
"i", "n", "g"

Character-Based

Tokenizer: Word-Based

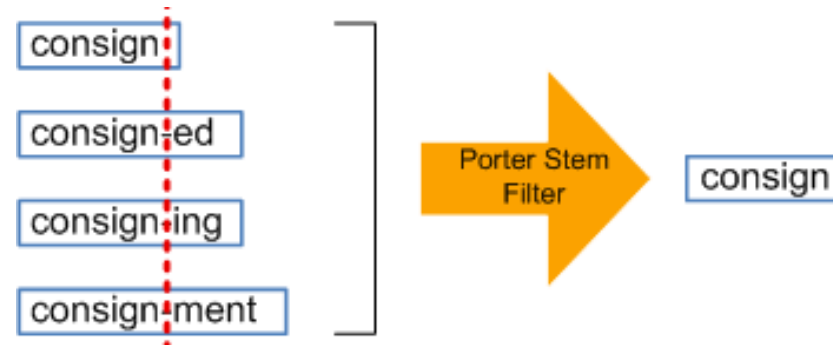
- Use **whitespace** and **punctuation** to split tokens and then assign id to each token

Token	a	an	at	***	bat	ball	***	zipper	zoo	***
Index	1	2	3	***	527	528	***	9,842	9,843	***

- e.g., How many tokens should we see for “This is tokenizing.”
- 4: [This] [is] [tokenizing] [.]
- What are limitations of this approach?
 - **Huge vocabulary**: ~1 million words in English alone according to Merriam- Webster (<https://www.merriam-webster.com/help/faq-how-many-english-words>)
 - **Novel words**: information is lost, because we use one token (e.g., “UNK”) for all instances

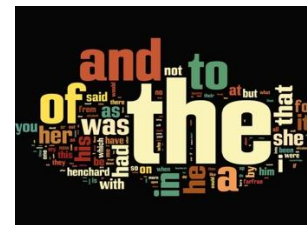
Pre-processing Ideas to Reduce Vocabulary

- Lower case all letters
- Use each word's "stem"; e.g., singular vs plural, reconcile different verb forms
 - e.g., stemming



<https://dzone.com/articles/using-lucene-grails>

- e.g., **lemmatizing** to get intended based word (e.g., caring -> care, not “car”)
- Only use most popular N words, assigning **UNK token** to the rest
- **Stop word removal**: discard frequent words



<https://github.com/topics/stopwords-removal>

Tokenizers: Converting Text to Numeric Value

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"is", "fun", "."

Word-Based

"ma",
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Subword-Based

"M", "a", "c",
"h", "i", "n",
"e", "l", "e",
"a", "r", "n",
"i", "n", "g"

Character-Based

Overcome word-based
limitations by using characters!

Tokenizer: Character-Based

- Id assigned to each unique character

Token	a	b	c	***	0	1	***	!	@	***
Index	1	2	3	***	27	28	***	119	120	***

- e.g., How many tokens should we see for “This is tokenizing.”
- 17: [T] [h] [i] [s] [i] [s] [t] [o] [k] [e] [n] [i] [z] [i] [n] [g] [.]
- Advantages of this approach:
 - **Smaller vocabulary** (e.g., 26 English letters plus punctuation and other symbols)
 - **More known tokens** (i.e., words are comprised of characters)
- What are limitations of this approach?
 - **Reduced semantics**: greater meaning ambiguity when we only see one character (e.g., “a”)
 - **Longer input**: greater computational expense; e.g., 17 characters vs 4 words for above example

Tokenizers: Converting Text to Numeric Value

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Subword-Based

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"h", "i", "n",
"e", "l", "e",
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"i", "n", "g"

Character-Based

Middle ground, widely used
in modern neural networks

Tokenizer: Subword-Based

- Id assigned to common entities with merges/decompositions of rarer entities
 - e.g., 5 tokens for decomposition of “This is tokenizing.”: [This] [is] [token] [izing] [.]
- Compared to word-based and character-based tokenizers:
 - Middle-sized input
 - Middle-sized vocabulary
 - Middling semantics
 - Unknown tokens are rare

Popular Example: Byte Pair Encoding

1. Identify all tokens in the training data with their frequency
2. Define vocabulary size; e.g., 14
3. Add all characters in the tokenized input to the vocabulary; e.g.,

Character sequence	Cost
C o s t	2
b e s t	2
m e n u	1
m e n	1
c a m e l	1

Popular Example: Byte Pair Encoding

1. Identify all tokens in the training data with their frequency
2. Define vocabulary size; e.g., 14
3. Add all characters in the tokenized input to the vocabulary; e.g.,
4. Until vocabulary is filled, add merged highest frequency symbol pairs

e.g., What are the highest frequency symbol pairs?

Character sequence	Cost	Vocabulary
C o s t	2	a, b, c, e, l, m, n, o, s, t, u
b e s t	2	
m e n u	1	
m e n	1	
c a m e l	1	

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C o s t	2	a, b, c, e, l, m, n, o, s, t, u, st
b e s t	2	
m e n u	1	
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Character sequence	Cost	Vocabulary
C o s t	2	a, b, c, e, l, m, n, o, s, t, u, st, me, men
b e s t	2	
m e n u	1	
m e n	1	
c a m e l	1	

Popular Focus Today: Improving Tokenization

Tiktokenizer

System

You are a helpful assistant

×

User

Content

×

Add message

```
<|im_start|>system<|im_sep|>You are a helpful assistant<|im_end|><|im_start|>user<|im_sep|><|im_end|><|im_start|>assistant<|im_sep|>
```

gpt-4o

Token count

16

```
<|im_start|>system<|im_sep|>You are a helpful assistant<|im_end|><|im_start|>user<|im_sep|><|im_end|><|im_start|>assistant<|im_sep|>
```

```
200264, 17360, 200266, 3575, 553, 261, 10297, 29186, 200265, 200264, 1428, 200266, 200265, 200264, 173781, 200266
```

<https://tiktokenizer.vercel.app/>

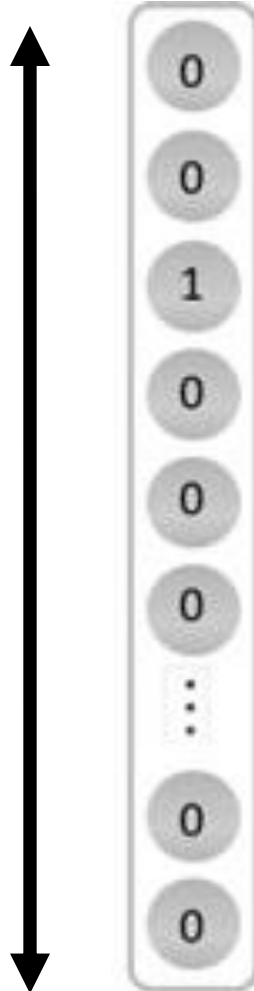
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Problems with One-Hot Encoding Words?

Dimensionality = vocabulary size

e.g., English has ~170,000 words
with ~10,000 commonly used words

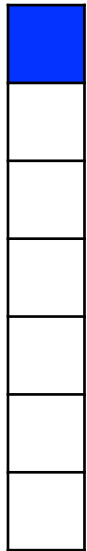


- Huge memory burden
- Computationally expensive

Limitation of One-Hot Encoding Words

- No notion of which words are similar, yet such understanding can improve generalization
 - e.g., “walking”, “running”, and “skipping” are all suitable for “He was ____ to school.”

Walking



Soap



Fire

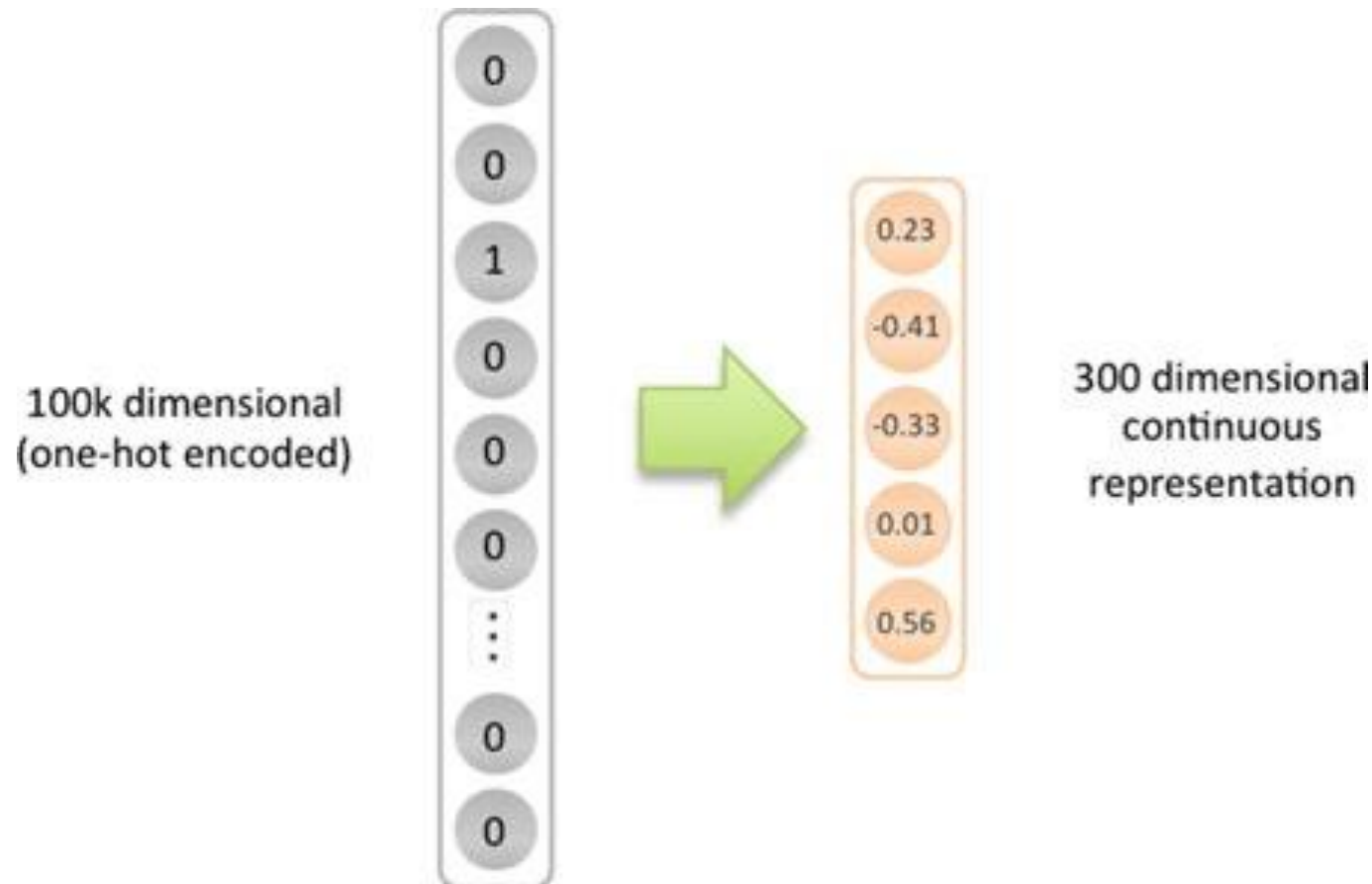


Skipping



The distance between
all words is equal!

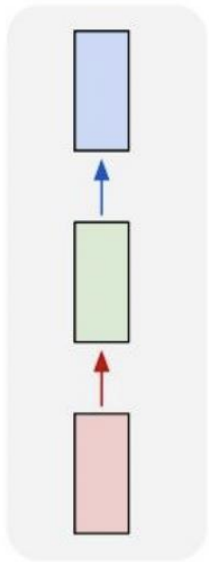
Idea: Represent Each Word Compactly in a Space Where Vector Distance Indicates Word Similarity



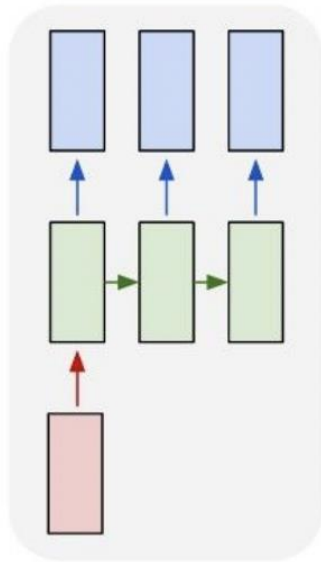
Potential Use (Of Numerous)

- Convert words into compact vectors as **input** to neural networks; e.g., RNNs

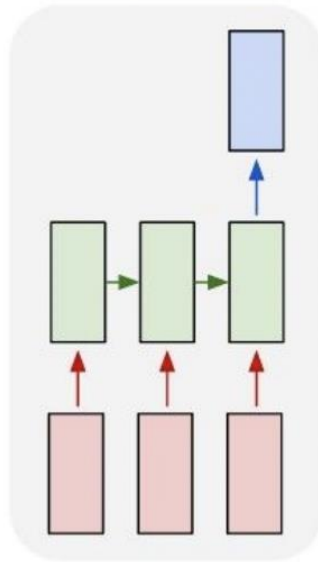
one to one



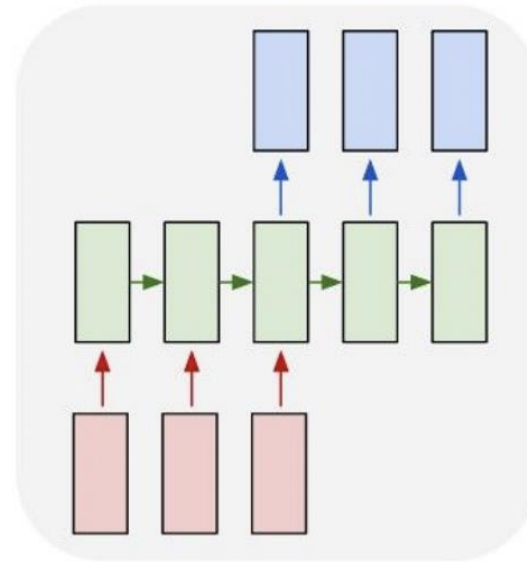
one to many



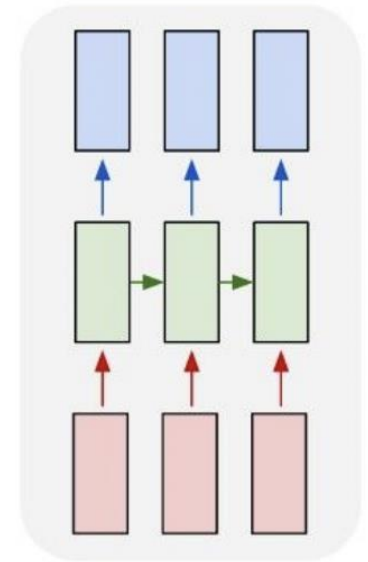
many to one



many to many



many to many



Inspiration: Distributional Semantics

“The distributional hypothesis says that the meaning of a word is derived from the context in which it is used, and words with similar meaning are used in similar contexts.”

- Origins: Harris in 1954 and Firth in 1957

Inspiration: Distributional Semantics

“The distributional hypothesis says that **the meaning of a word is derived from the context in which it is used**, and words with similar meaning are used in similar contexts.”

Inspiration: Distributional Semantics

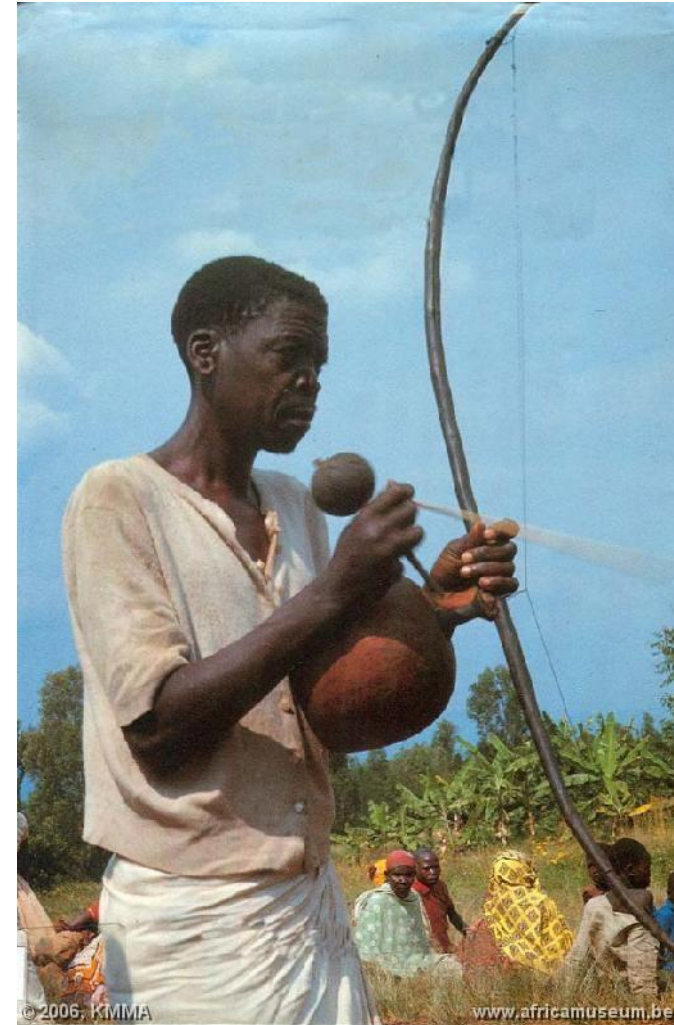
- What is the meaning of **berimbau** based on **context**?

Background music from a **berimbau** offers a beautiful escape.

Many people danced around the **berimbau** player.

I practiced for many years to learn how to play the **berimbau**.

- Idea: **context** makes it easier to understand a word's meaning



Inspiration: Distributional Semantics

“The distributional hypothesis says that the meaning of a word is derived from the context in which it is used, and words with similar meaning are used in similar contexts.”

Inspiration: Distributional Semantics

- What other words could fit into these contexts?
 1. Background music from a _____ offers a beautiful escape.
 2. Many people danced around the _____ player.
 3. I practiced for many years to learn how to play the _____.

Hypothesis is that words with similar row values have similar meanings

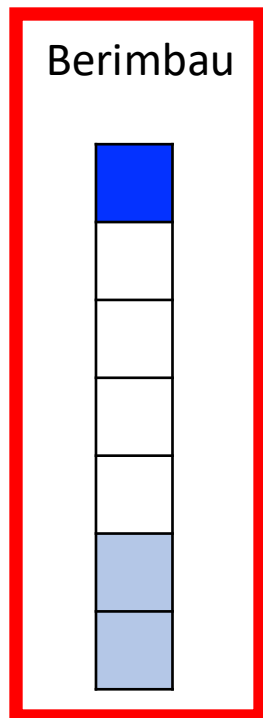
	1.	2.	3.	
Berimbau	1	1	1	} Contexts 1 if a word can appear in the context 0 otherwise
Soap	0	0	0	
Fire	0	0	0	
Guitar	1	1	1	

Inspiration: Distributional Semantics

“The distributional hypothesis says that the meaning of a word is derived from the context in which it is used, and words with similar meaning are used in similar contexts.”

Approach

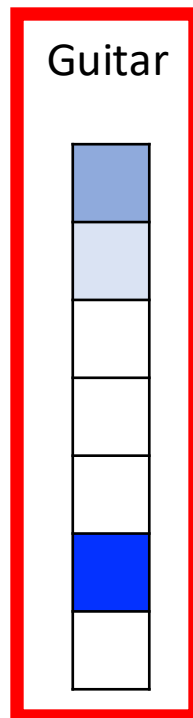
- Learn a dense (lower-dimensional) vector for each word by characterizing its **context**, which inherently will reflect similarity/differences to other words



Soap



Fire



Berimbau and guitar are the closest word pair

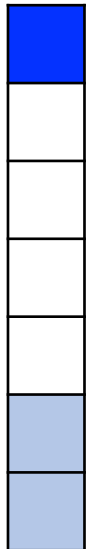
The distance between
each pair of words differs!

Note: many ways to measure
distance (e.g., cosine distance)

Approach

- Learn a dense (lower-dimensional) vector for each word by characterizing its **context**, which inherently will reflect similarity/differences to other words

Berimbau



Soap



Fire



Guitar



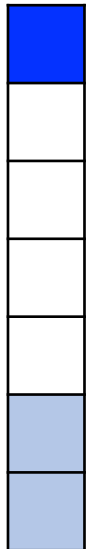
We embed words in a shared space so they can be compared with a few features

What features would discriminate these words?

Approach

- Learn a dense (lower-dimensional) vector for each word by characterizing its **context**, which inherently will reflect similarity/differences to other words

Berimbau



Soap



Fire



Guitar



Wooden

Commodity

Cleaner

Food

Temperature

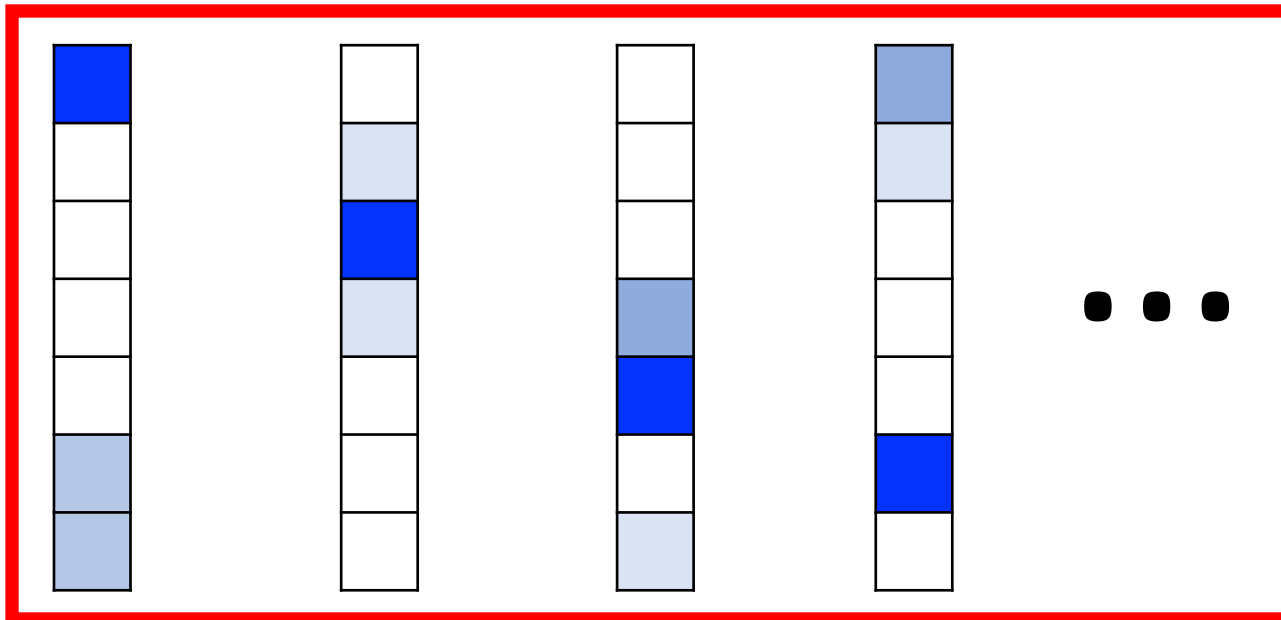
Noisy

Weapon

Potential, interpretable features

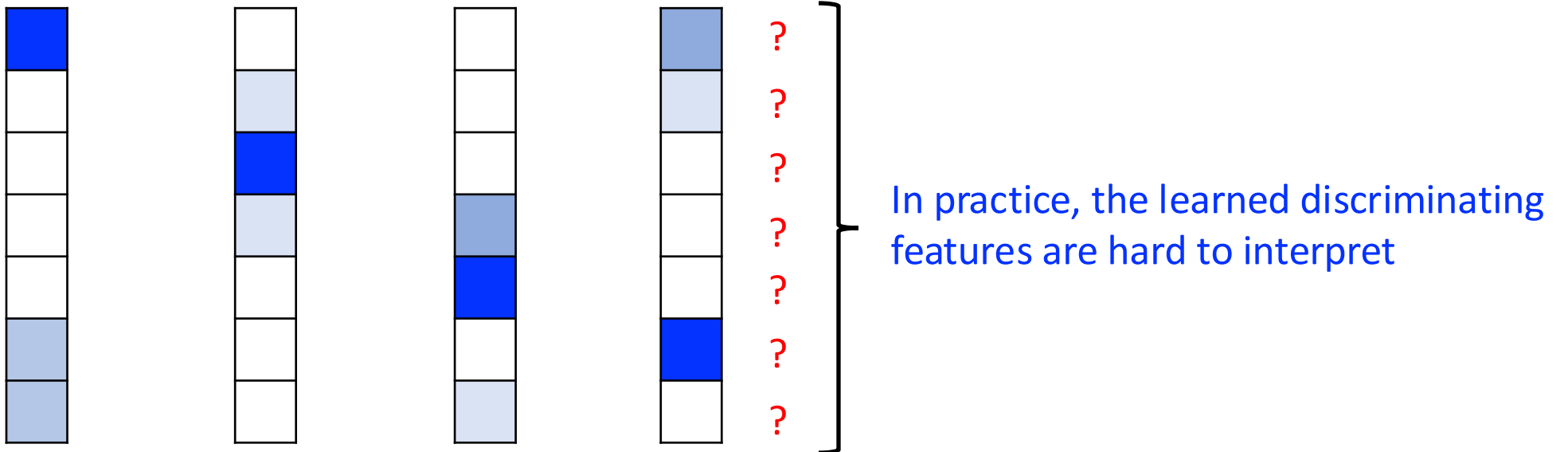
Approach: Learn Word Embedding Space

- An **embedding space** represents a finite number of words, decided in training
- A **word embedding** is represented as a vector indicating its context
- The dimensionality of all word embeddings in an embedding space match
 - What is the word embedding dimensionality for the shown example?



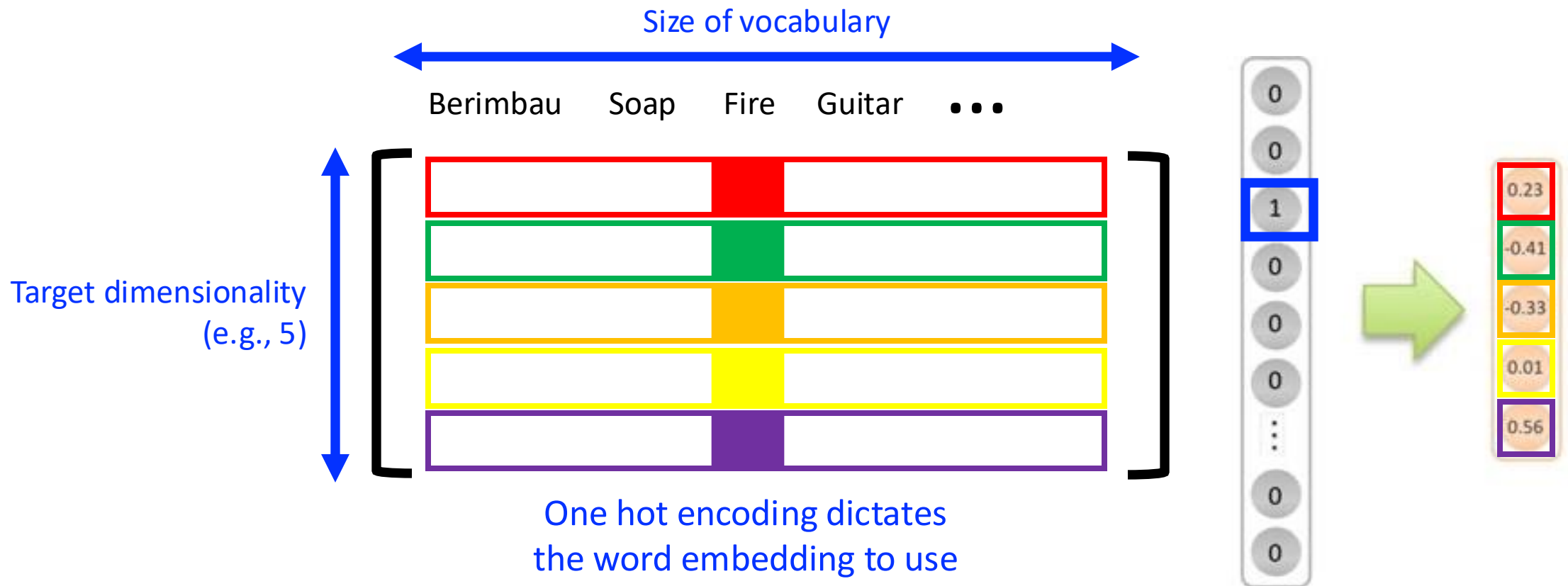
Approach: Learn Word Embedding Space

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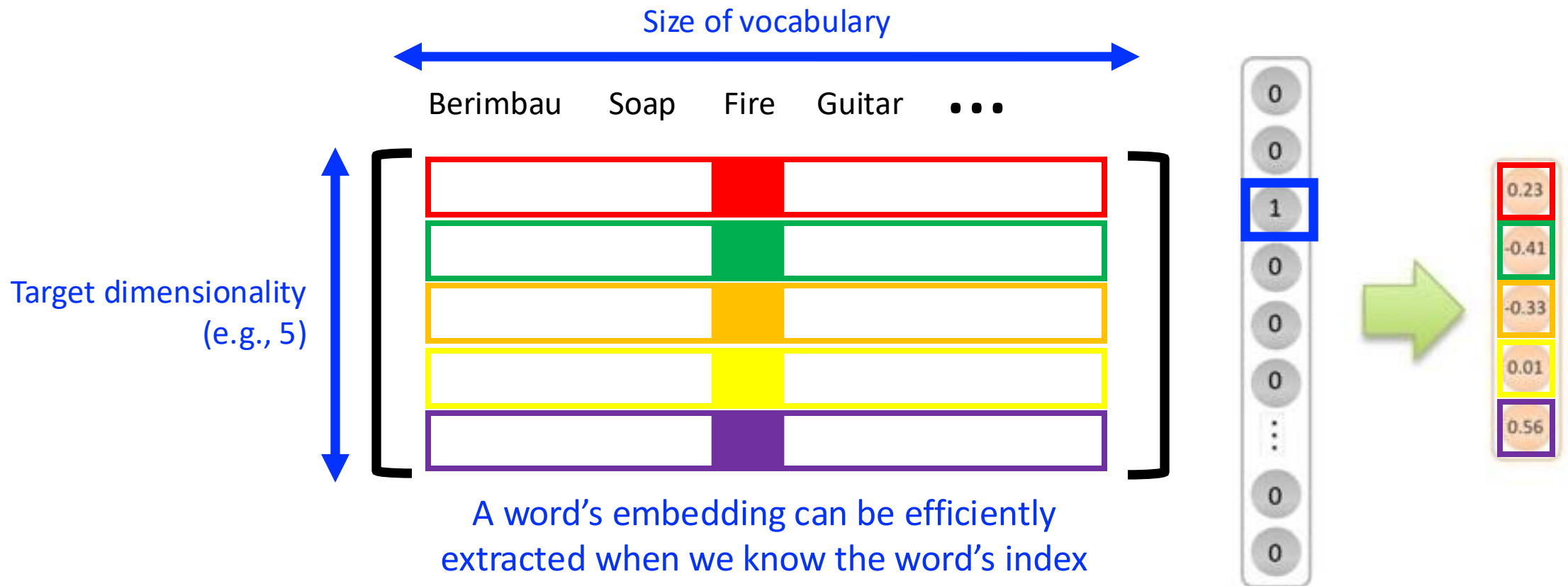
Embedding Matrix

- The embedding matrix converts an input word into a dense vector



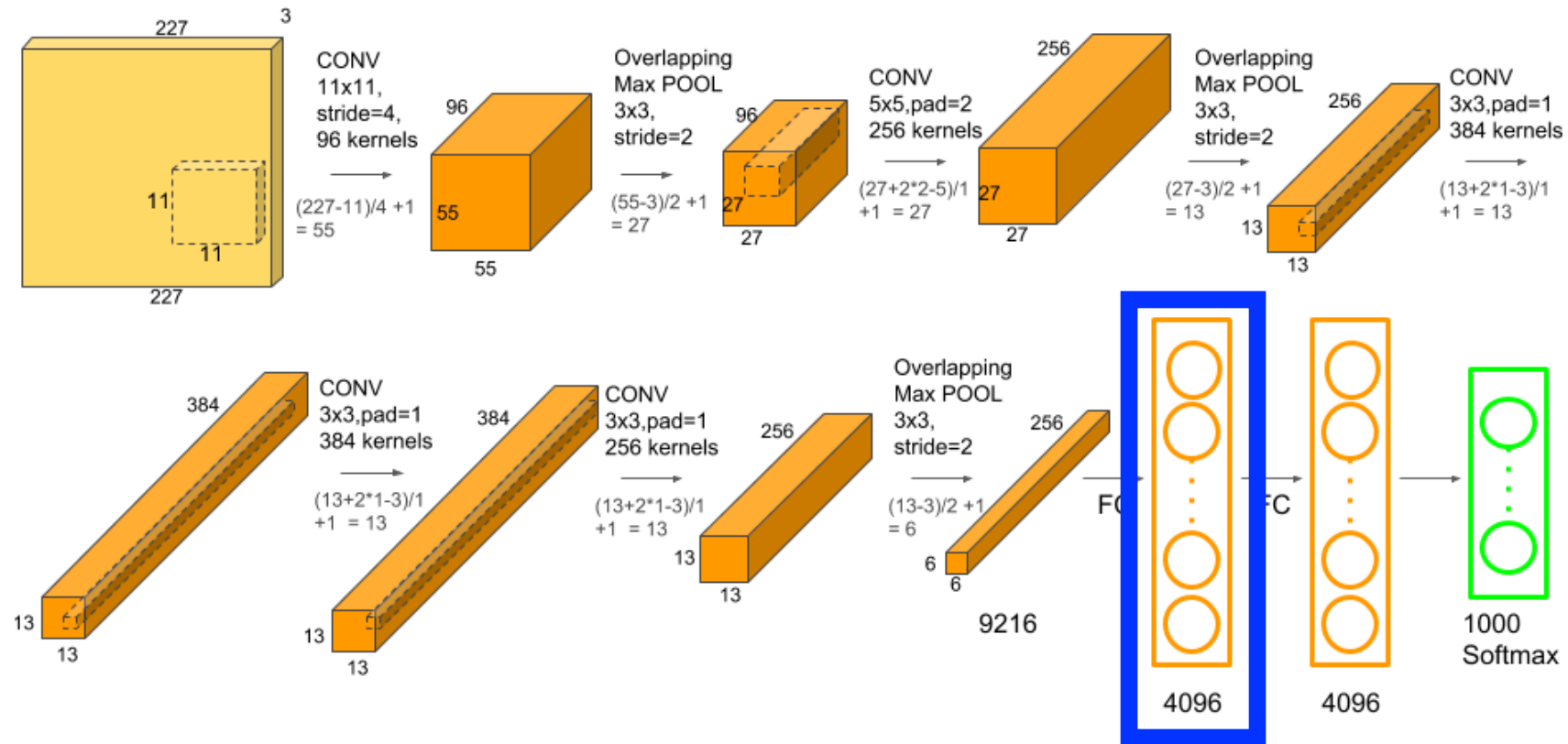
Embedding Matrix

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Word Embedding Analogous to a CNN Pretrained Feature

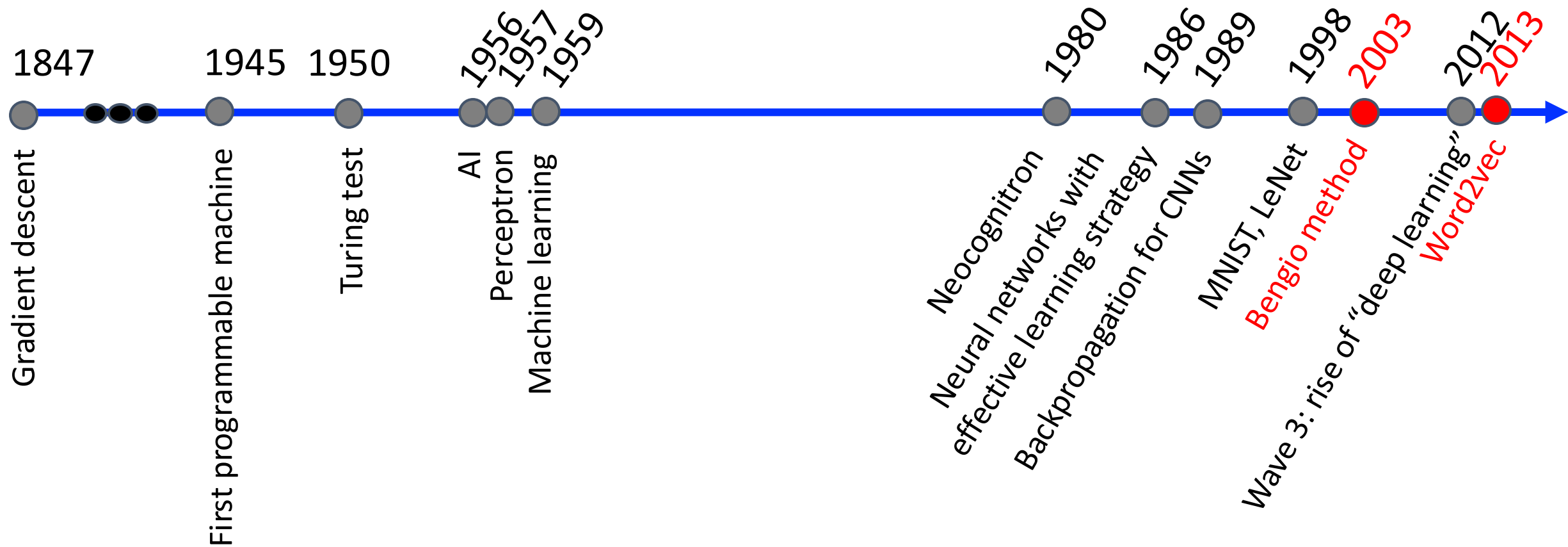
- e.g., FC6 layer of AlexNet



Popular Word Embeddings

- Bengio method
- Word2vec (skip-gram model)
- And more...

Historical Context



Popular Word Embeddings

- Bengio method
- Word2vec (skip-gram model)
- And more...

Idea: Learn Word Embeddings That Help Predict Viable Next Words

e.g.,

1. Background music from a _____
2. Many people danced around the _____
3. I practiced for many years to learn how to play the _____

Task: Predict Next Word Given Previous Ones

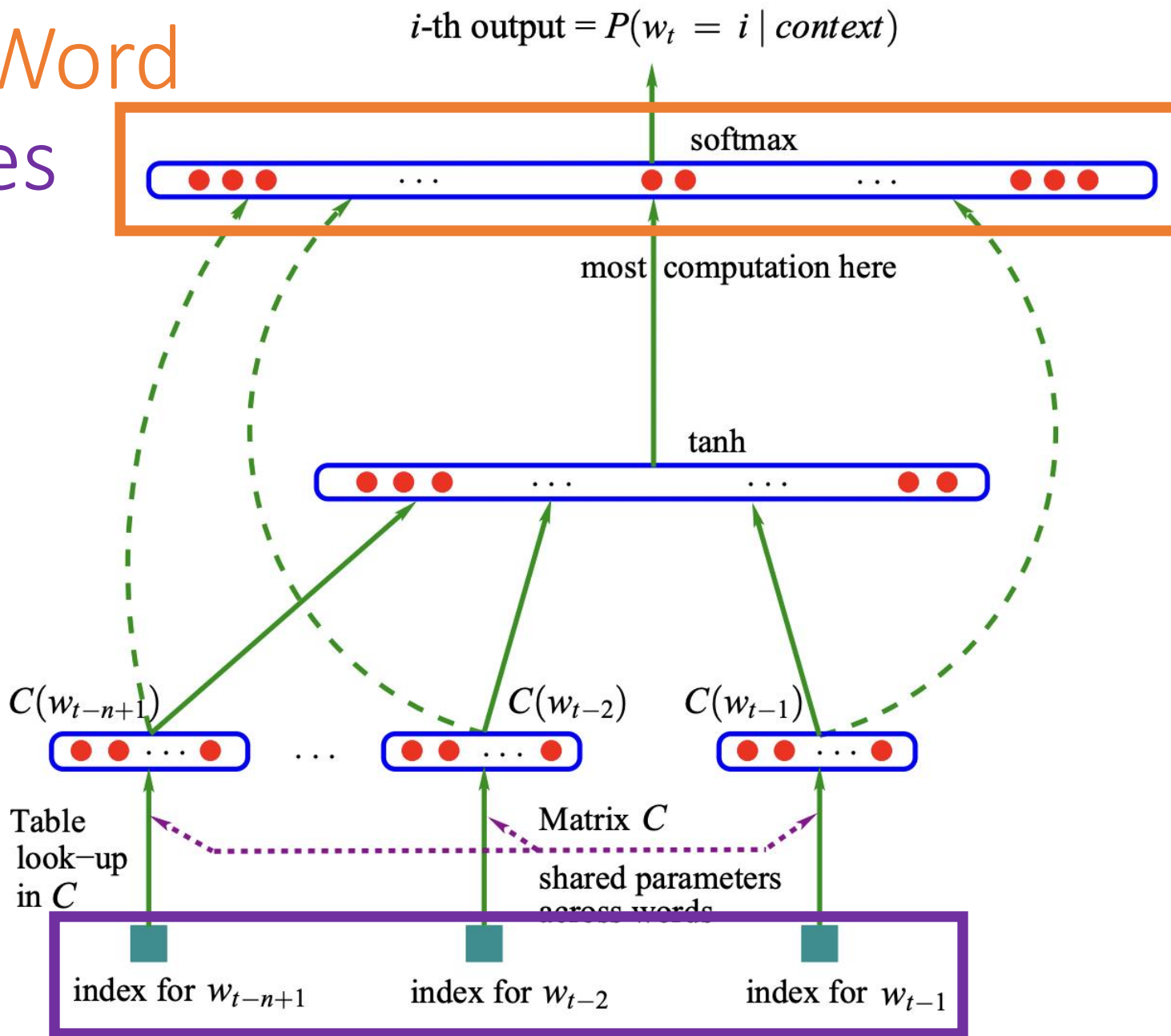
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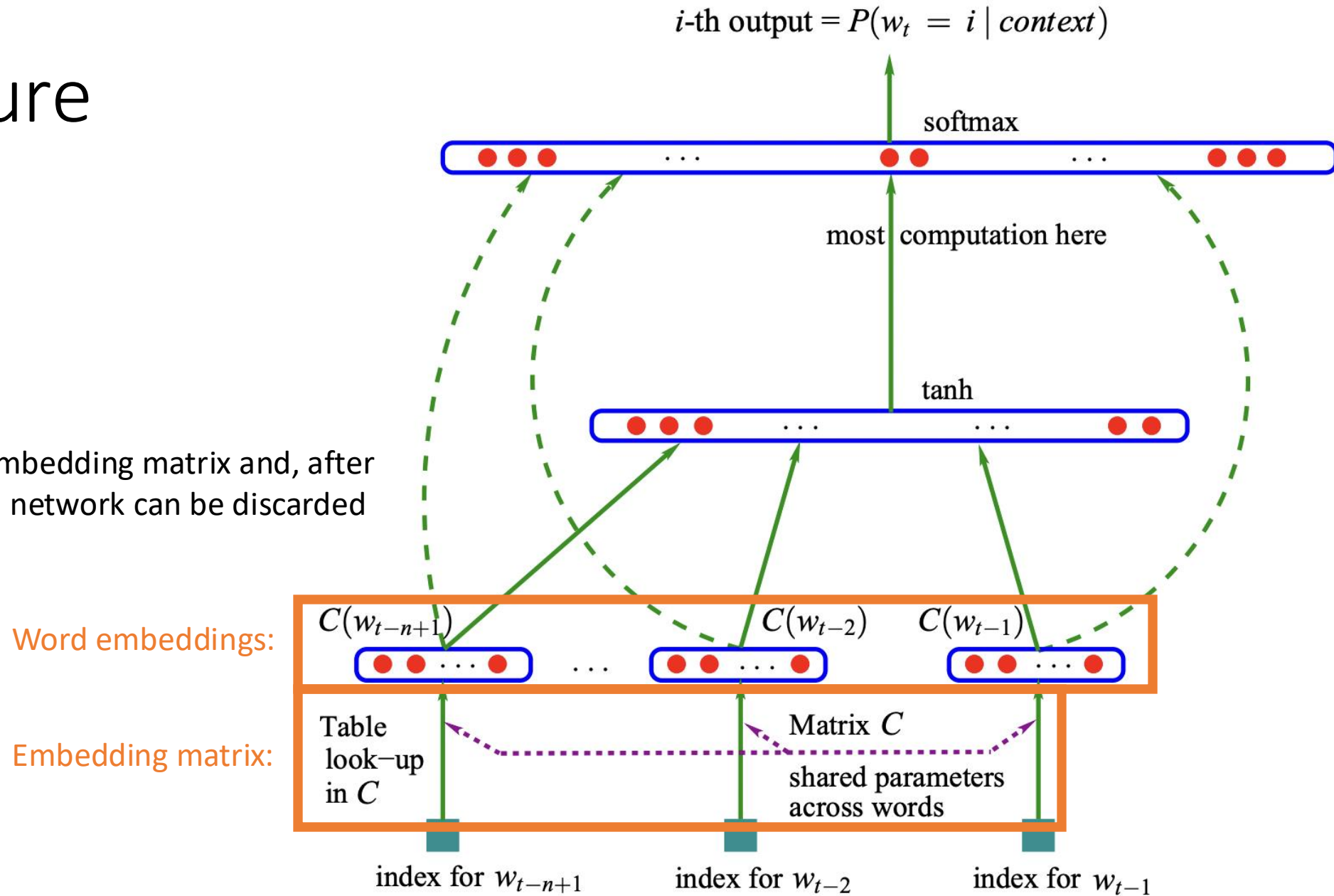
e.g., a vocabulary size of 17,000
was used in experiments

What is the dimensionality of
the output layer?
- 17,000 (each indexed position
indicates probability of a word)



Architecture

Note: the goal is to learn an embedding matrix and, after training, the rest of the neural network can be discarded

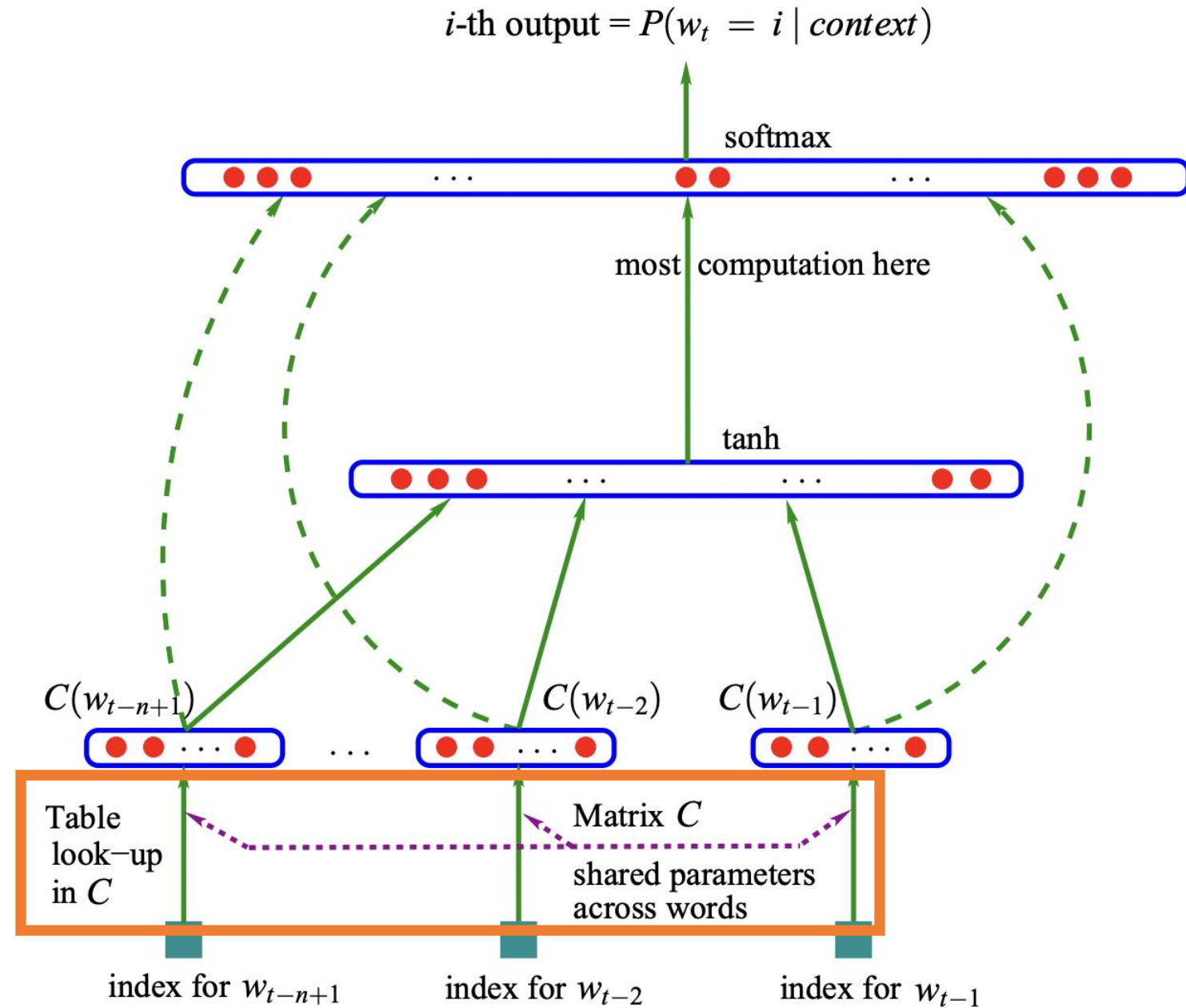


Architecture

e.g., a vocabulary size of 17,000 was used with embedding sizes of 30, 60, and 100 in experiments

Assume a 30-d word embedding
- what are the dimensions of the embedding matrix C ?

$30 \times 17,000$ (i.e., 510,000 weights)

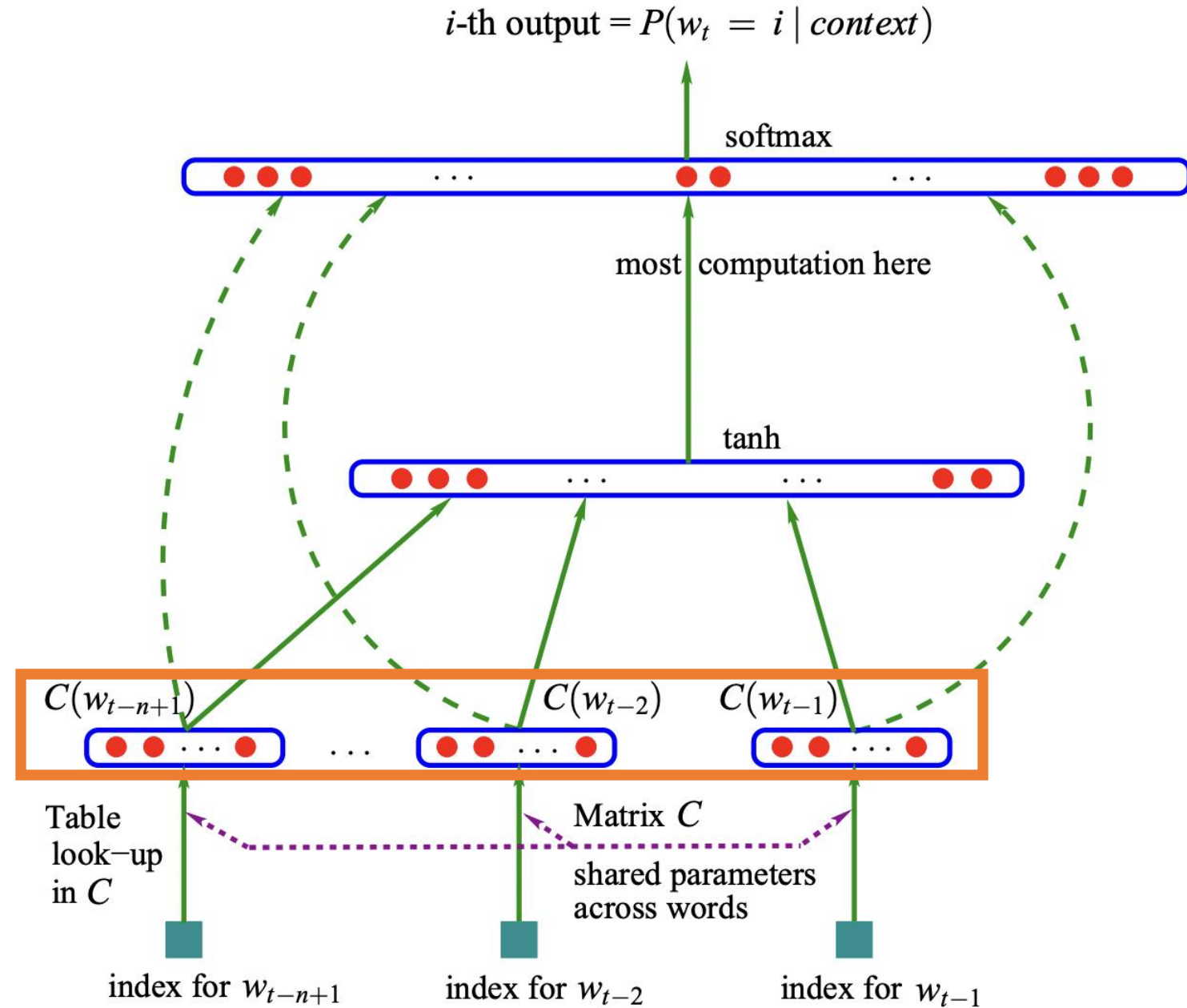


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30, 60, and 100 in experiments

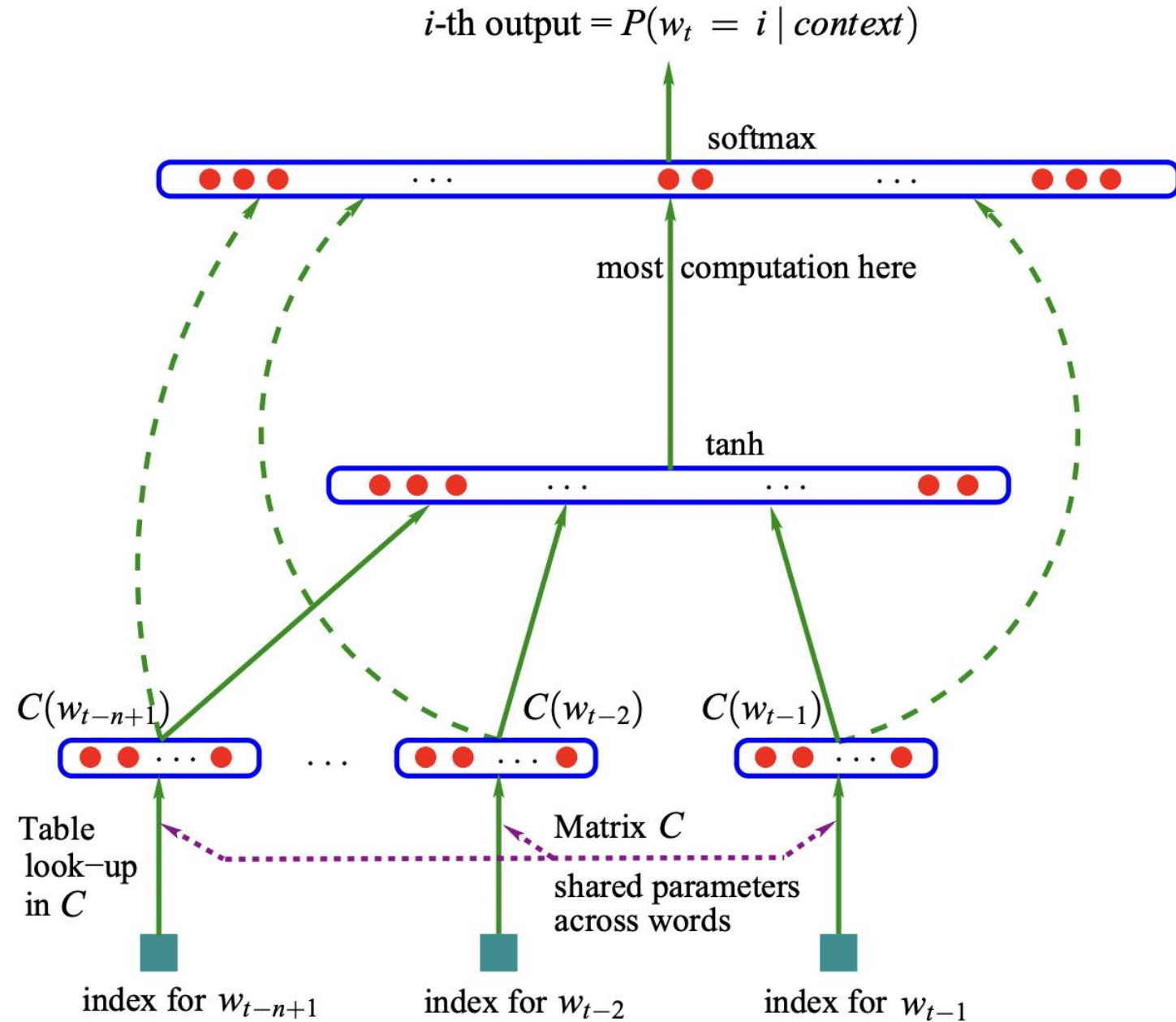
Assume a 30-d word embedding
- what are the dimensions of each
word embedding?

1×30



Architecture

Projection layer followed by a hidden layer with non-linearity

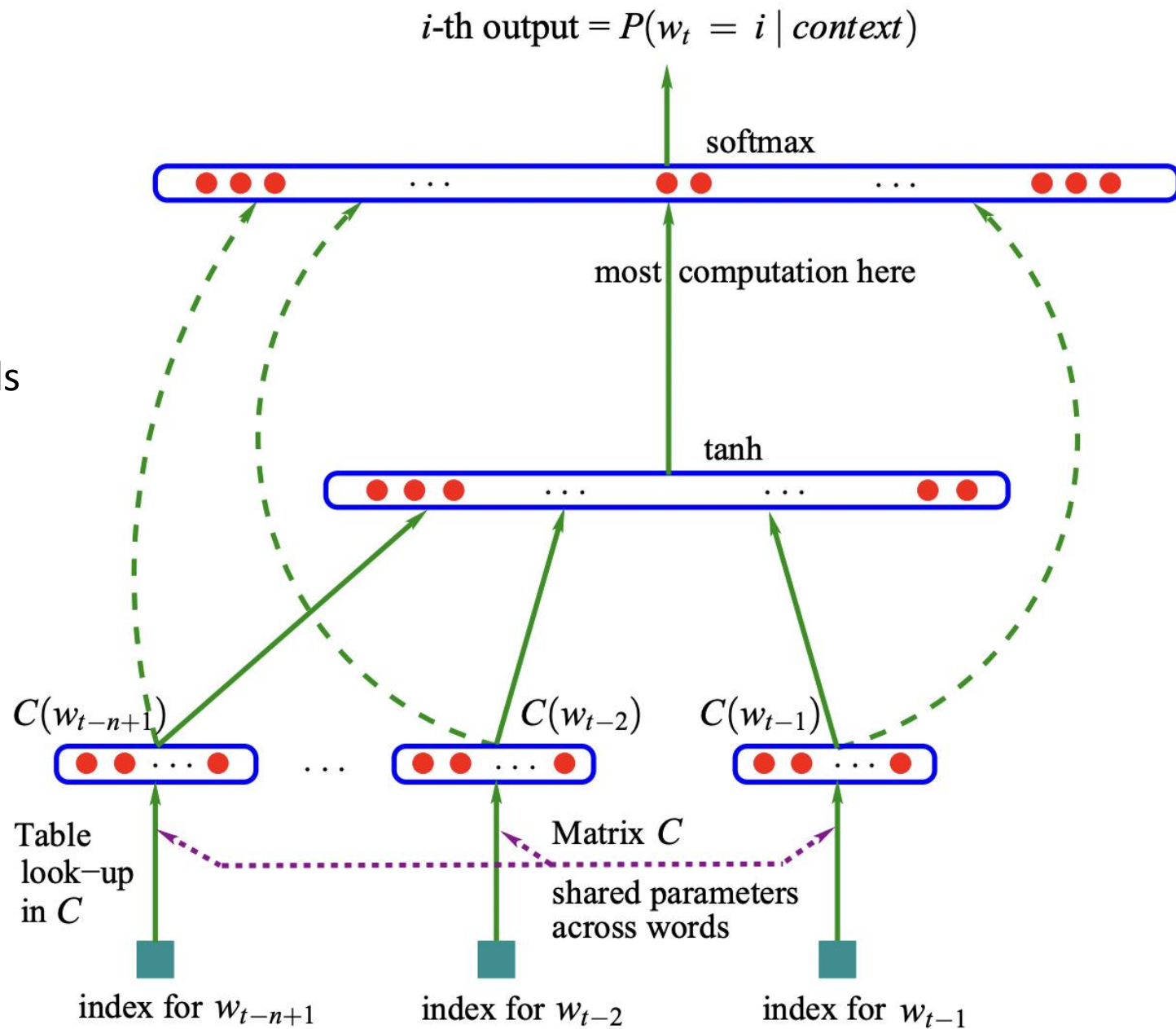


Training

Use sliding window on input data; e.g., 3 words

Background music from a berimbau offers a beautiful escape...

Input: tried 1, 3, 5, and 8 input words and used 2 datasets with ~1 million and ~34 million words respectively

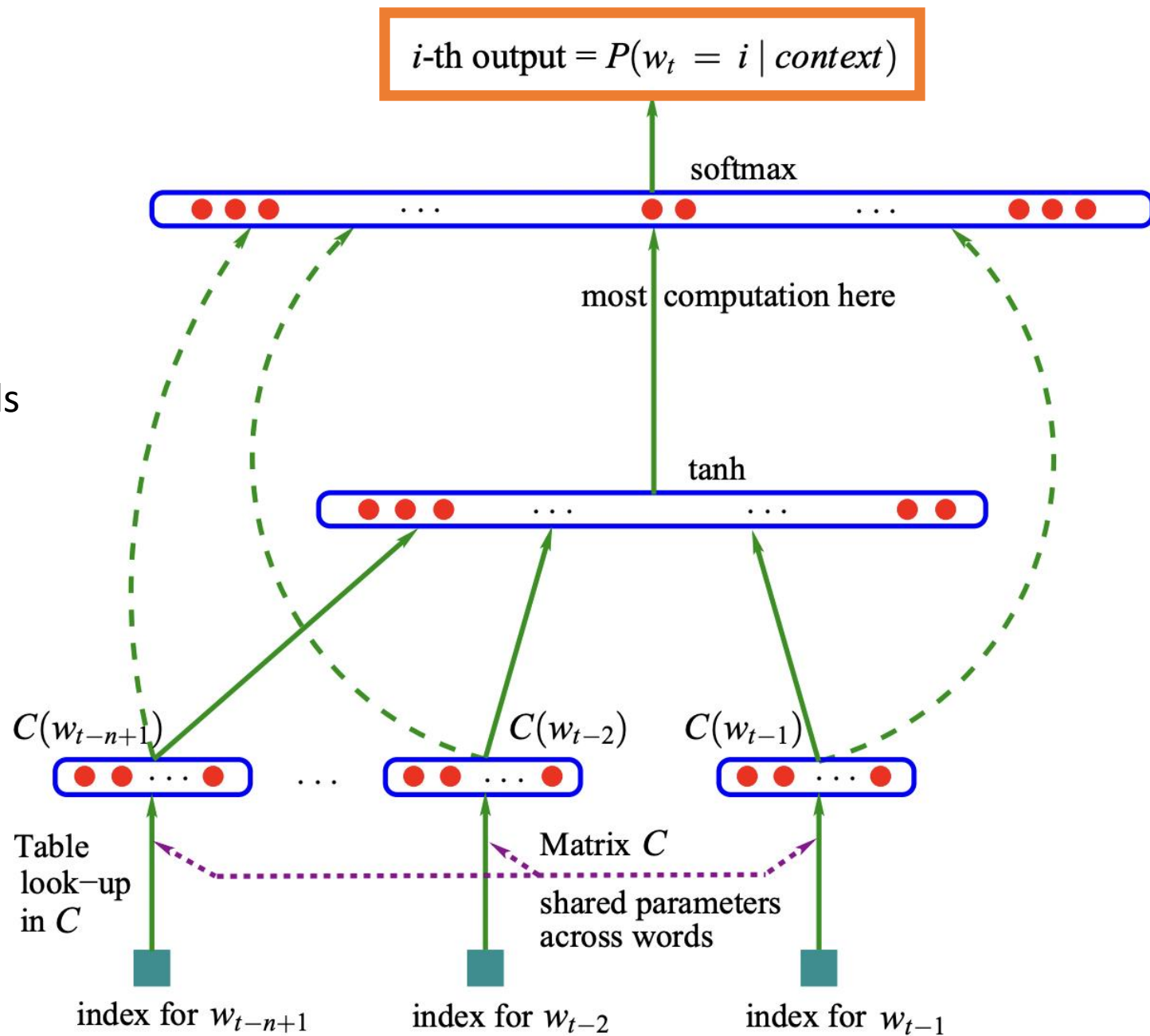


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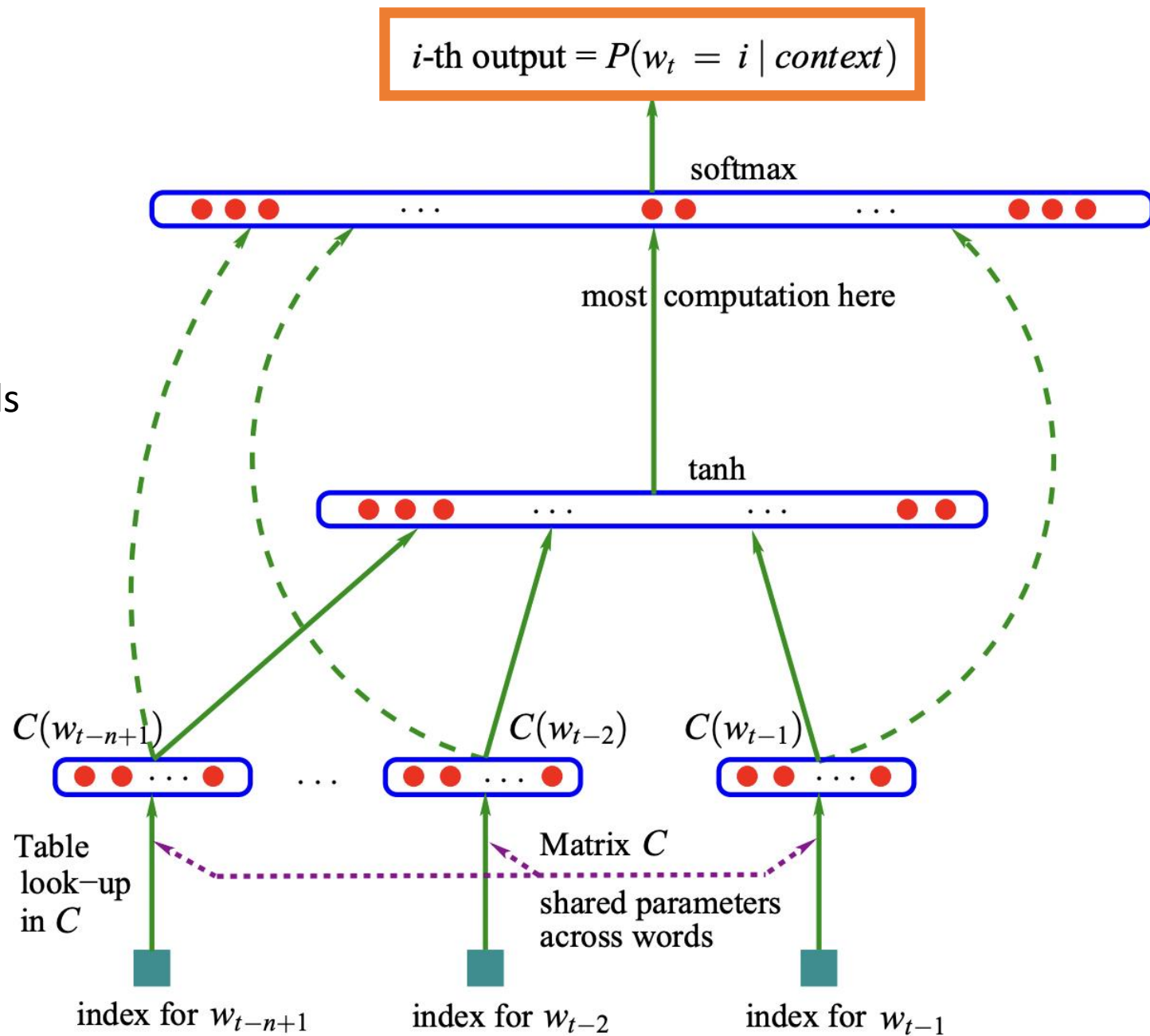


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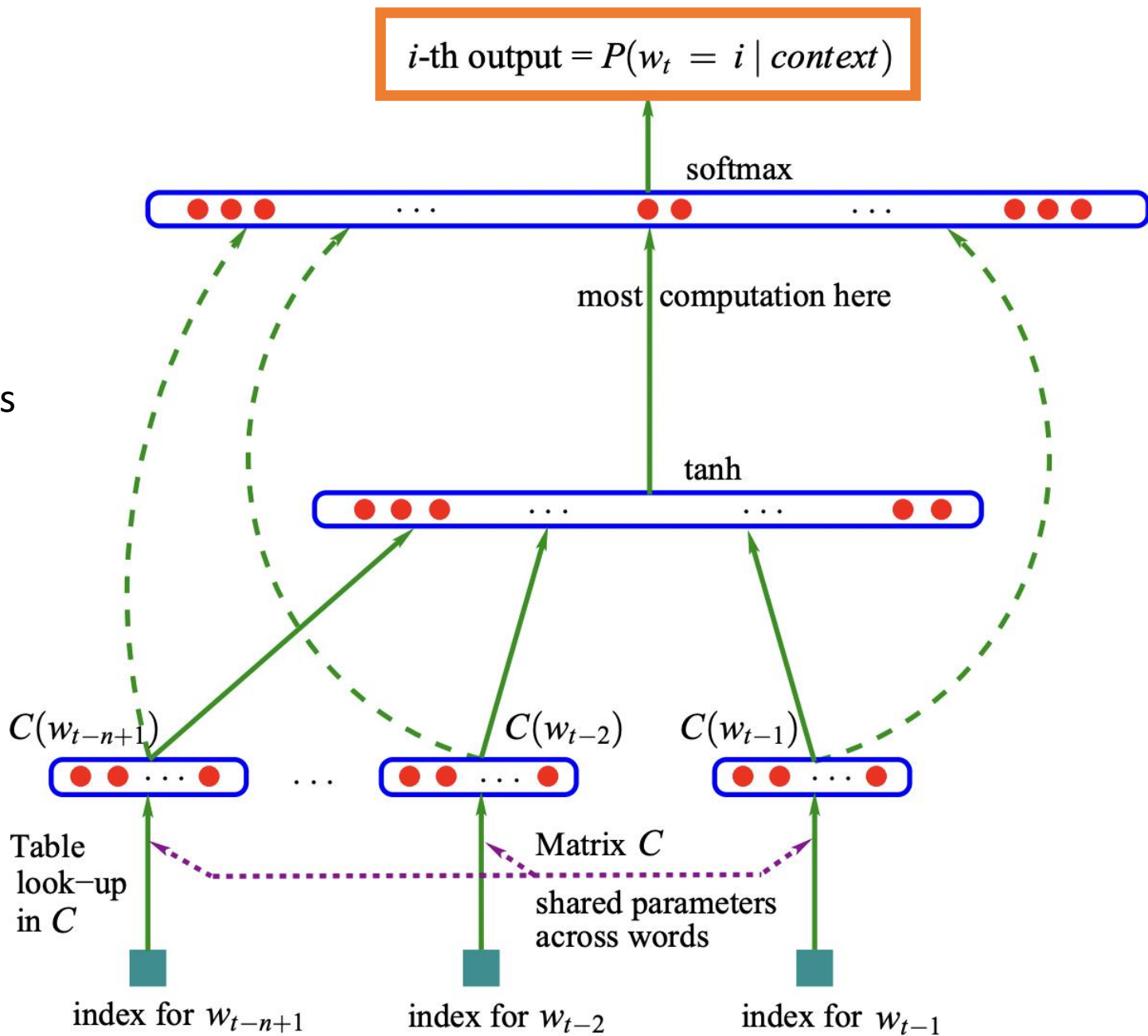


Training

Use sliding window on input data; e.g., 3 words

Background music **from a berimbau** **offers** a beautiful escape...

Input: tried 1, 3, 5, and 8 input words and used 2 datasets with ~1 million and ~34 million words respectively

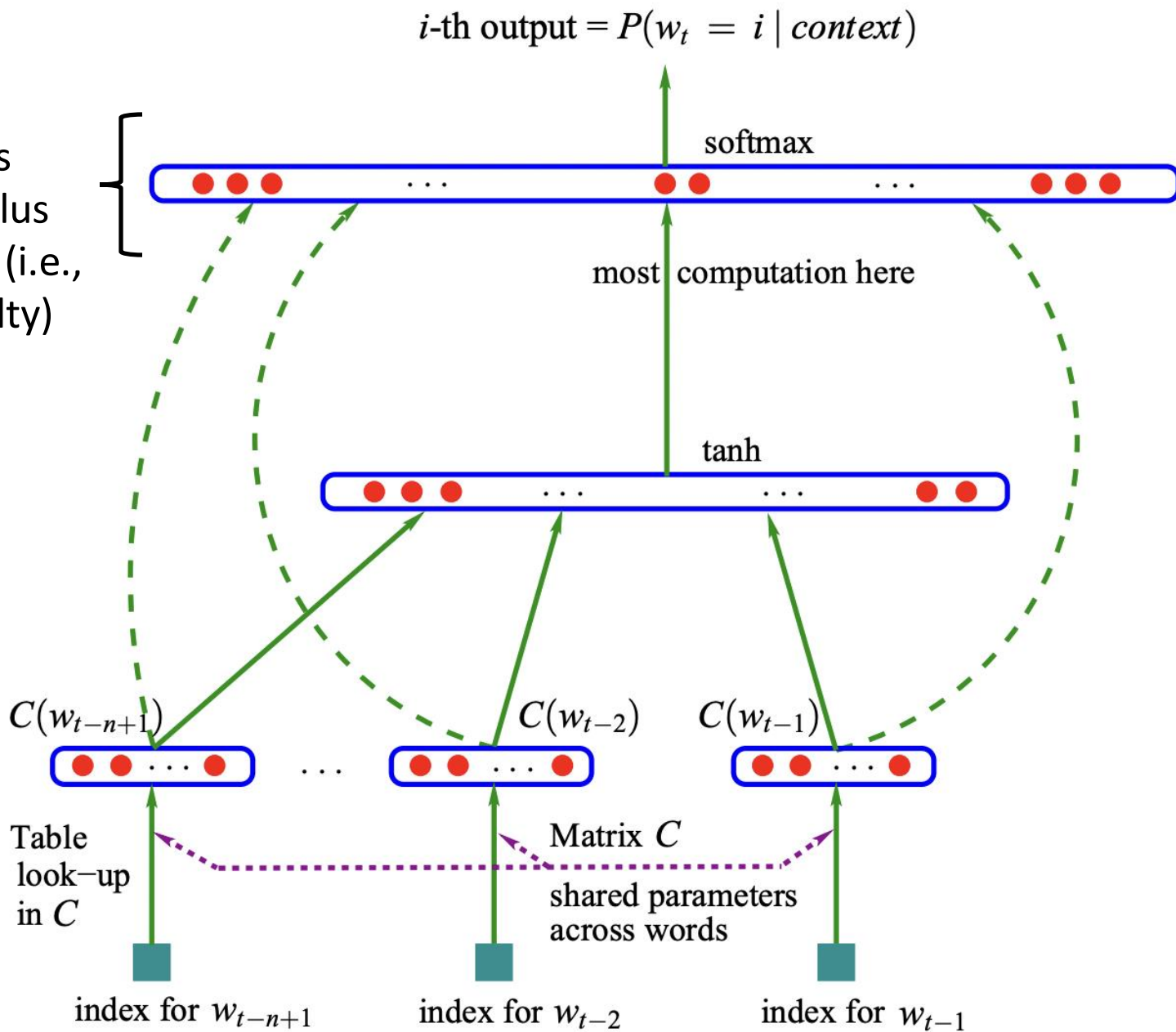


Training

Cost function:
minimize cross
entropy loss plus
regularization (i.e.,
L2 norm penalty)

Word embedding iteratively updated

Input: tried 1, 3, 5, and 8 input words
and used 2 datasets with ~1 million and
~34 million words respectively



Summary: Word Embeddings Learn Context of Previous Words Needed to Predict Next Word

e.g.,

1. Background music from a _____
2. Many people danced around the _____
3. I practiced for many years to learn how to play the _____

Popular Word Embeddings

- Bengio method
- Word2vec (skip-gram model)
- And more...

Idea: Learn Word Embeddings That Know What Are Viable Surrounding Words

e.g.,

1. _____ **berimbau** _____

2. _____ **berimbau** _____

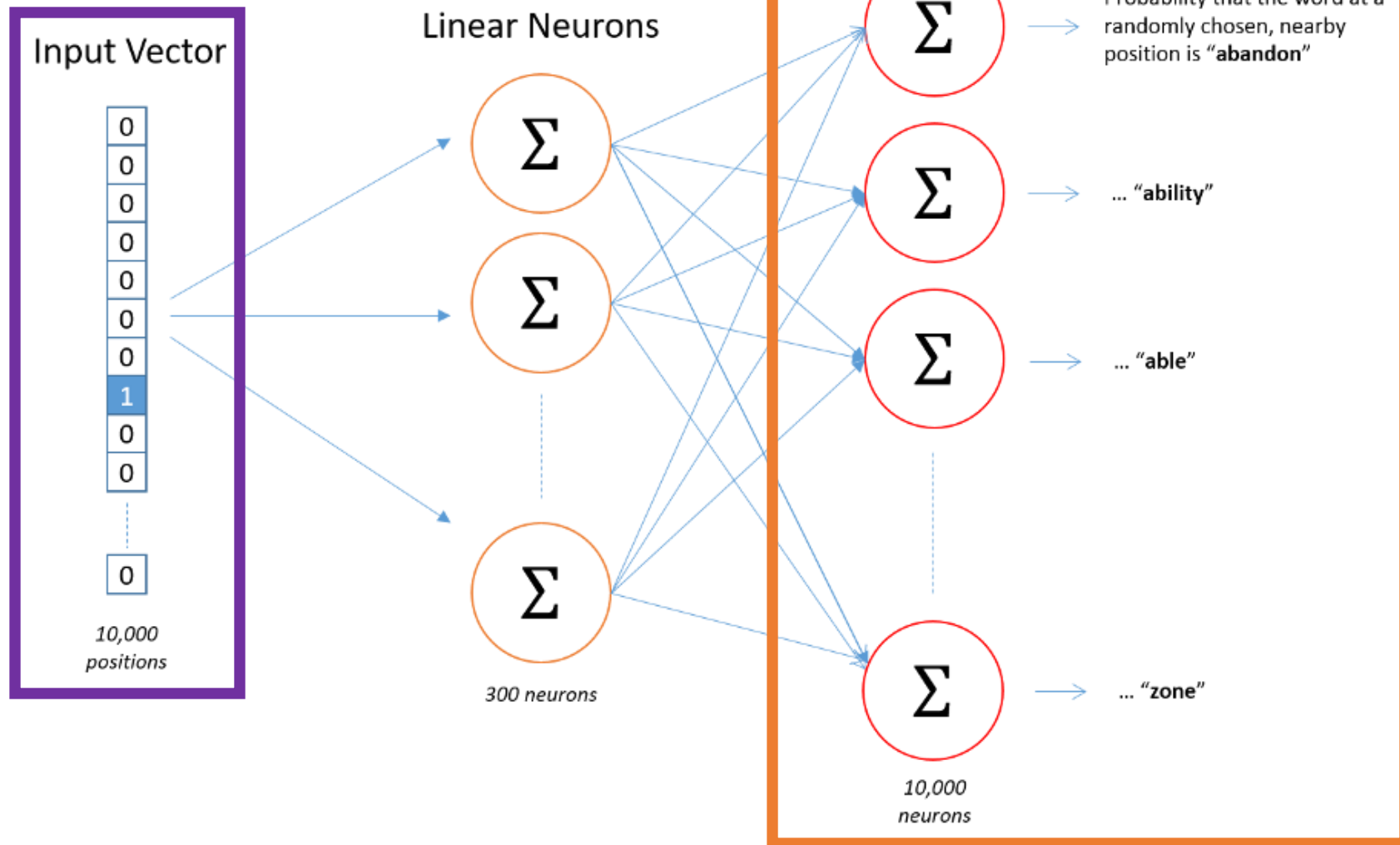
Task: Given Word, Predict a Nearby Word

e.g.,

1. _____ berimbau _____

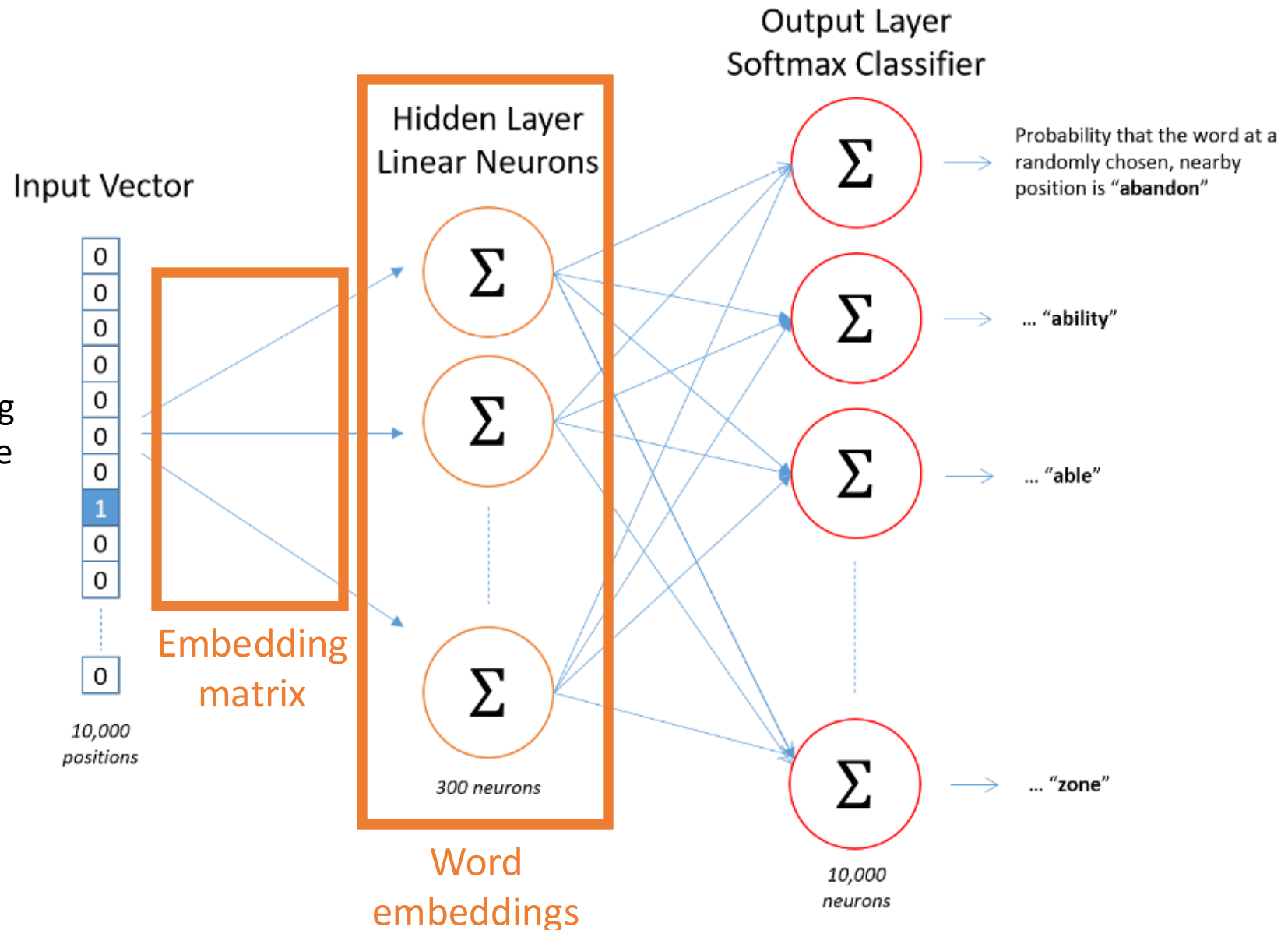
2. _____ berimbau _____

Task: Given Word, Predict a Nearby Word



Architecture

Recall: the goal is to learn an embedding matrix and, after training, the rest of the neural network can be discarded

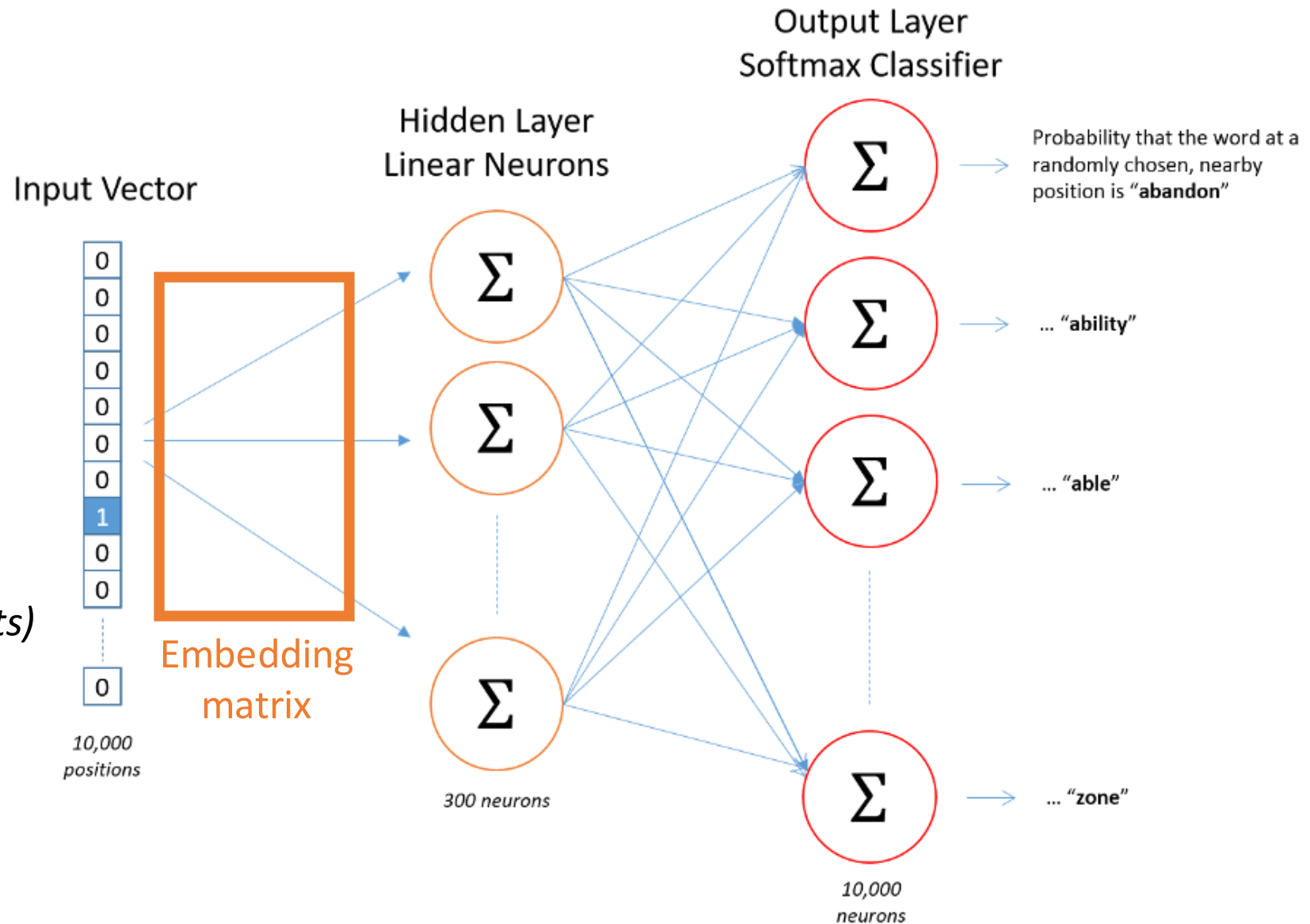


Architecture

e.g., a vocabulary size of 10,000 is used with embedding sizes of 300

What are the dimensions of the embedding matrix?

300 x 10,000 (i.e., 3,000,000 weights)

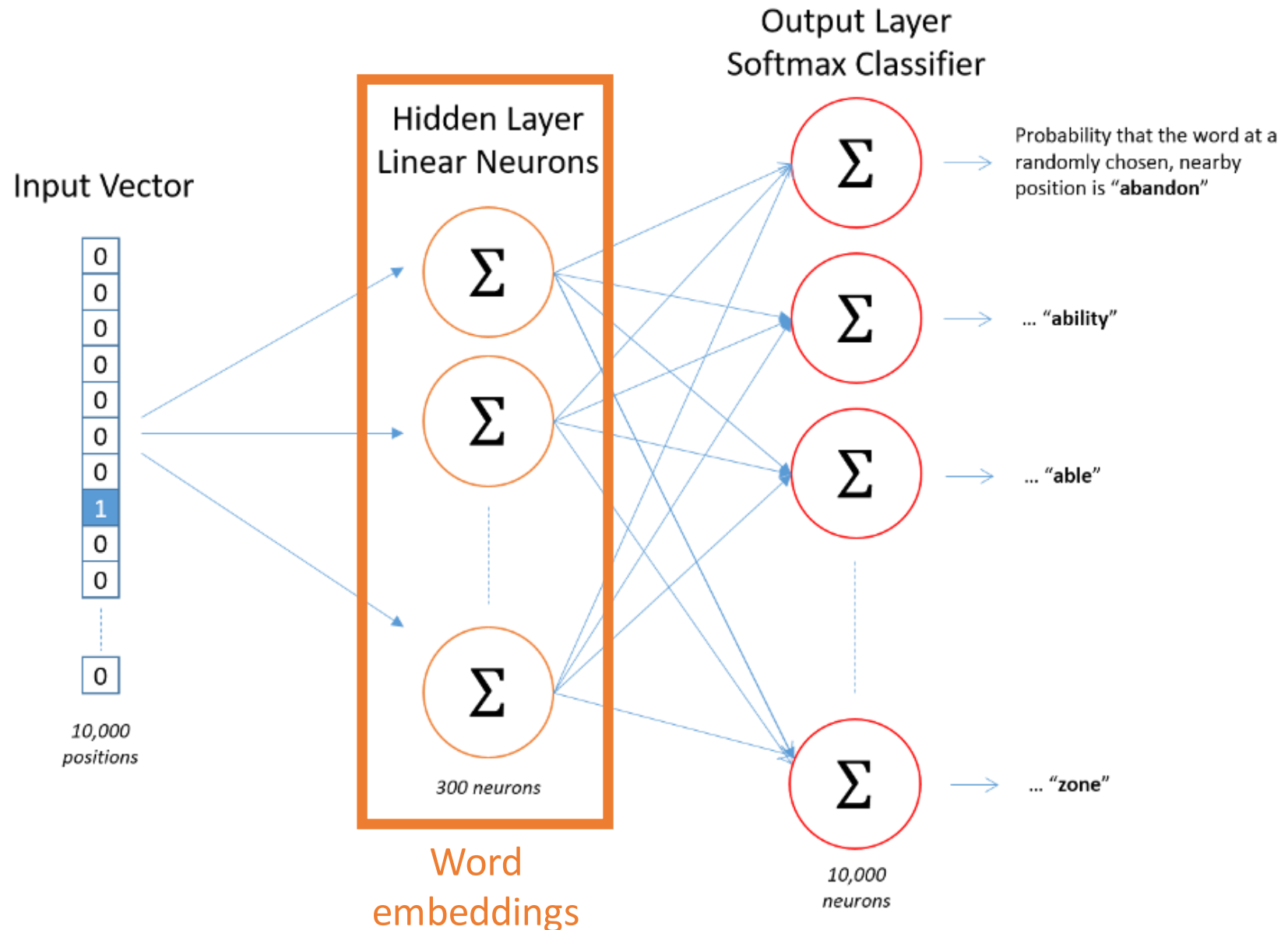


Architecture

e.g., a vocabulary size of 10,000 is used with embedding sizes of 300

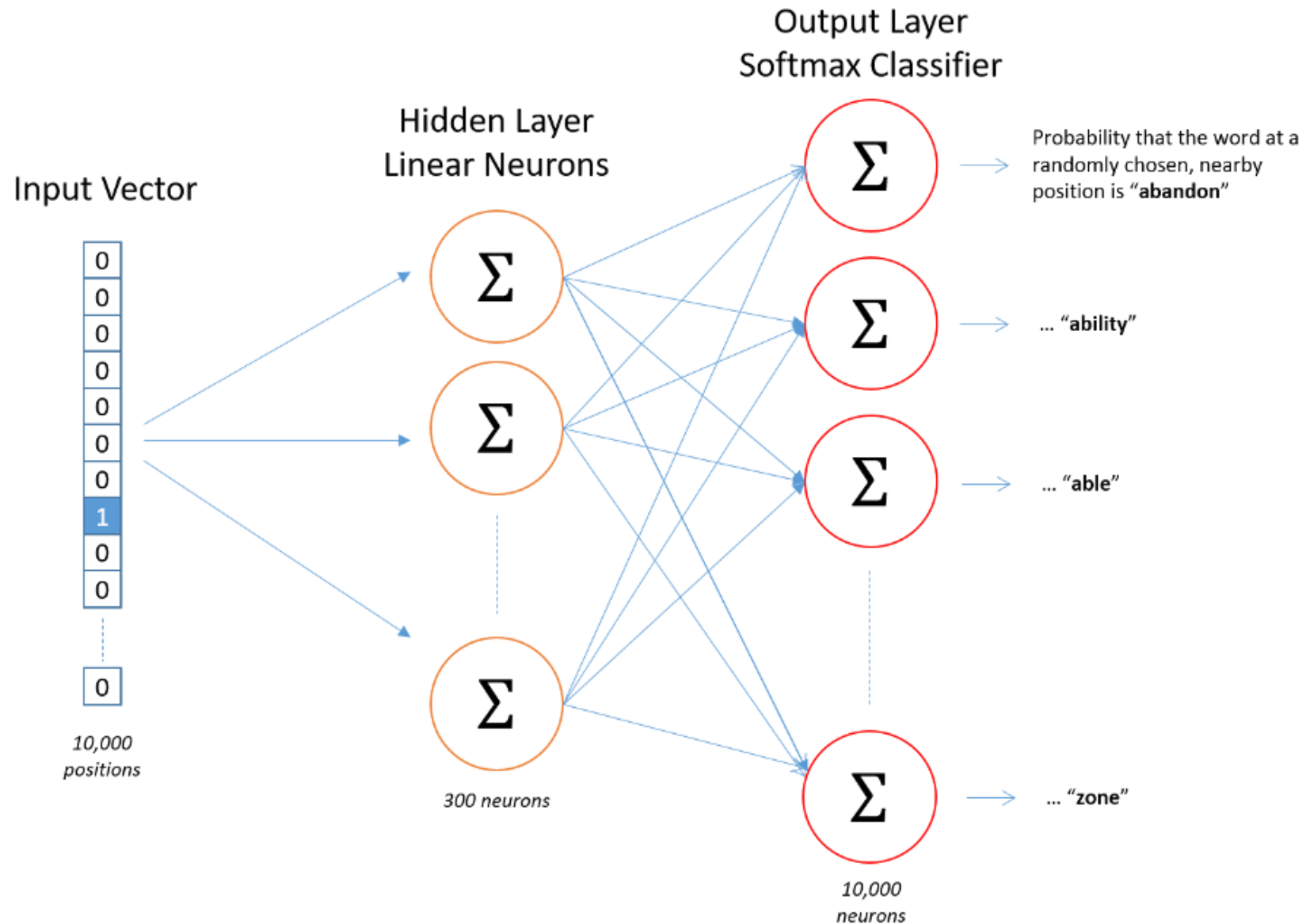
What are the dimensions of each word embedding?

1×300



Architecture

A **shallower, simpler architecture** than the Bengio approach (i.e., lacks a non-linear hidden layer)!



Training

Sliding window run over input
to sample neighbors of each
target word

Source Text	Training Samples						
<table><tr><td>The</td><td>quick</td><td>brown</td></tr></table> fox jumps over the lazy dog. ➡	The	quick	brown	(the, quick) (the, brown)			
The	quick	brown					
<table><tr><td>The</td><td>quick</td><td>brown</td><td>fox</td></tr></table> jumps over the lazy dog. ➡	The	quick	brown	fox	(quick, the) (quick, brown) (quick, fox)		
The	quick	brown	fox				
<table><tr><td>The</td><td>quick</td><td>brown</td><td>fox</td><td>jumps</td></tr></table> over the lazy dog. ➡	The	quick	brown	fox	jumps	(brown, the) (brown, quick) (brown, fox) (brown, jumps)	
The	quick	brown	fox	jumps			
<table><tr><td>The</td><td>quick</td><td>brown</td><td>fox</td><td>jumps</td><td>over</td></tr></table> the lazy dog. ➡	The	quick	brown	fox	jumps	over	(fox, quick) (fox, brown) (fox, jumps) (fox, over)
The	quick	brown	fox	jumps	over		

Hyperparameters: What Works Well?

- Word embedding dimensionality?
 - Dimensionality set between 100 and 1,000
- Context window size?
 - ~10

Very Exciting/Surprising Finding

- Vector arithmetic with word embeddings can solve many analogies

(Full test list: <http://download.tensorflow.org/data/questions-words.txt>)

- **Semantic** relationships (meaning of words in a sentence):

- Italy + (Paris - France) = Rome

- **Syntactic** relationships (rules for words in a sentence)

- smallest + (big - small) = biggest
- think + (read - reading) = thinking
- mouse + (dollars - dollar) = mice

Summary: Word Embeddings Are Learned that Support Predicting Viable Surrounding Words!

e.g.,

1. _____ **berimbau** _____

2. _____ **berimbau** _____

Popular Word Embeddings

- Bengio method
- Word2vec (skip-gram model)
- And more...

Variants for Learning Embeddings

- Capture **global context** rather than just local context of previous or surrounding words; e.g.,
 - GloVe for Global Vectors (Pennington et al., 2014)
- Capture that the **same word can have different meanings** under different contexts; e.g., The bat... ...swung? ...flew?
 - Elmo was a pioneer for language models (Peters et al., arXiv 2018)
- Support **multiple languages**; e.g.,
 - Fast-text (Bojanowski et al., 2016)

Word Embedding Limitations/Challenges

- Distinguish antonyms from synonyms
 - Antonyms are often close in embeddings space since they often occur in similar contexts: “I **hate** math” vs “I **love** math” or “Turn **right**” vs “Turn **left**”
- Gender bias:

Man is to Computer Programmer as Woman is to Homemaker? Debiasing Word Embeddings

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Extreme <i>she</i>	Extreme <i>he</i>		Gender stereotype <i>she-he</i> analogies	
1. homemaker	1. maestro	sewing-carpentry	registered nurse-physician	housewife-shopkeeper
2. nurse	2. skipper	nurse-surgeon	interior designer-architect	softball-baseball
3. receptionist	3. protege	blond-burly	feminism-conservatism	cosmetics-pharmaceuticals
4. librarian	4. philosopher	giggle-chuckle	vocalist-guitarist	petite-lanky
5. socialite	5. captain	sassy-snappy	diva-superstar	charming-affable
6. hairdresser	6. architect	volleyball-football	cupcakes-pizzas	lovely-brilliant
7. nanny	7. financier			
8. bookkeeper	8. warrior			
9. stylist	9. broadcaster	queen-king	Gender appropriate <i>she-he</i> analogies	
10. housekeeper	10. magician	waitress-waiter	sister-brother	mother-father
			ovarian cancer-prostate cancer	convent-monastery

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 - Antonyms are often close in embeddings space since they often occur in similar contexts: “I **hate** math” vs “I **love** math” or “Turn **right**” vs “Turn **left**”
- Gender bias
- What **additional language biases** do you think could be learned?
- Still not as compact as **phrase-level** or **sentence-level** embeddings

Today's Topics

- Motivation: numeric representation of natural language
- Tokenization: how to convert text into discrete units
- Neural word embeddings: how to create dense representation
- Programming tutorial

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The End